

## 14.1: Introduction to Vectors

In this chapter we will review a few concepts you probably know from your physics courses. This chapter does not intend to cover the topic in a comprehensive manner, but instead touch on a few concepts that you will use in your physical chemistry classes.

A vector is a quantity that has both a magnitude and a direction, and as such they are used to specify the position, velocity and momentum of a particle, or to specify a force. Vectors are usually denoted by boldface symbols (e.g.  $\mathbf{u}$ ) or with an arrow above the symbol (e.g.  $\vec{u}$ ). A tilde placed above or below the name of the vector is also commonly used in shorthand ( $\tilde{u}, \underset{\sim}{u}$ ).

If we multiply a number  $a$  by a vector  $\mathbf{v}$ , we obtain a new vector that is parallel to the original but with a length that is  $a$  times the length of  $\mathbf{v}$ . If  $a$  is negative  $a\mathbf{v}$  points in the opposite direction than  $\mathbf{v}$ . We can express any vector in terms of the so-called unit vectors. These vectors, which are designated  $\hat{\mathbf{i}}$ ,  $\hat{\mathbf{j}}$  and  $\hat{\mathbf{k}}$ , have unit length and point along the positive  $x$ ,  $y$  and  $z$  axis of the cartesian coordinate system (Figure 14.1.1). The symbol  $\hat{\mathbf{i}}$  is read "i-hat". Hats are used to denote that a vector has unit length.

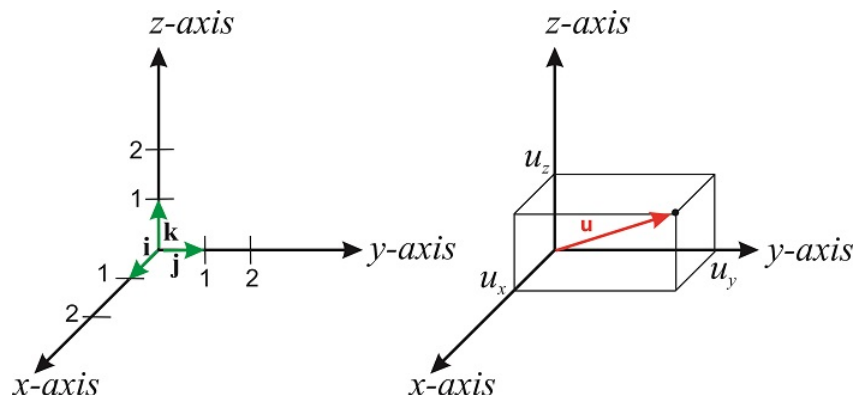


Figure 14.1.1: Left: The unit vectors. Right: A vector  $\mathbf{u}$  can be expressed in terms of the unit vectors as  $\mathbf{u} = u_x \hat{\mathbf{i}} + u_y \hat{\mathbf{j}} + u_z \hat{\mathbf{k}}$  (CC BY-NC-SA; Marcia Levitus)

The length of  $\mathbf{u}$  is its magnitude (or modulus), and is usually denoted by  $u$ :

$$u = |\mathbf{u}| = (u_x^2 + u_y^2 + u_z^2)^{1/2} \quad (14.1.1)$$

If we have two vectors  $\mathbf{u} = u_x \hat{\mathbf{i}} + u_y \hat{\mathbf{j}} + u_z \hat{\mathbf{k}}$  and  $\mathbf{v} = v_x \hat{\mathbf{i}} + v_y \hat{\mathbf{j}} + v_z \hat{\mathbf{k}}$ , we can add them to obtain

$$\mathbf{u} + \mathbf{v} = (u_x + v_x) \hat{\mathbf{i}} + (u_y + v_y) \hat{\mathbf{j}} + (u_z + v_z) \hat{\mathbf{k}}$$

or subtract them to obtain:

$$\mathbf{u} - \mathbf{v} = (u_x - v_x) \hat{\mathbf{i}} + (u_y - v_y) \hat{\mathbf{j}} + (u_z - v_z) \hat{\mathbf{k}}$$

When it comes to multiplication, we can perform the product of two vectors in two different ways. The first, which gives a scalar (a number) as the result, is called scalar product or dot product. The second, which gives a vector as a result, is called the vector (or cross) product. Both are important operations in physical chemistry.

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