

1.2.2: Significant Figures in Calculations

Learning Objectives

- Use significant figures correctly in arithmetical operations.

Rounding

Before dealing with the specifics of the rules for determining the significant figures in a calculated result, we need to be able to round numbers correctly. To **round** a number, first decide how many significant figures the number should have. Once you know that, round to that many digits, starting from the left. If the number immediately to the right of the last significant digit is less than 5, it is dropped and the value of the last significant digit remains the same. If the number immediately to the right of the last significant digit is greater than or equal to 5, the last significant digit is increased by 1.

Consider the measurement 207.518 m. Right now, the measurement contains six significant figures. How would we successively round it to fewer and fewer significant figures? Follow the process as outlined in Table 1.2.2.1.

Table 1.2.2.1: Rounding examples

Number of Significant Figures	Rounded Value	Reasoning
6	207.518	All digits are significant
5	207.52	8 rounds the 1 up to 2
4	207.5	2 is dropped
3	208	5 rounds the 7 up to 8
2	210	8 is replaced by a 0 and rounds the 0 up to 1
1	200	1 is replaced by a 0

Notice that the more rounding that is done, the less reliable the figure is. An approximate value may be sufficient for some purposes, but scientific work requires a much higher level of detail.

It is important to be aware of significant figures when you are mathematically manipulating numbers. For example, dividing 125 by 307 on a calculator gives 0.4071661238... to an infinite number of digits. But do the digits in this answer have any practical meaning, especially when you are starting with numbers that have only three significant figures each? When performing mathematical operations, there are two rules for limiting the number of significant figures in an answer—one rule is for addition and subtraction, and one rule is for multiplication and division.

*In operations involving significant figures, the answer is reported in such a way that it reflects the reliability of the **least precise** operation. An answer is no more precise than the least precise number used to get the answer.*

Multiplication and Division

For multiplication or division, the rule is to count the number of significant figures in each number being multiplied or divided and then limit the significant figures in the answer to the lowest count. An example is as follows:

$$\underbrace{38.65}_{4 \text{ sig figs}} \times \underbrace{105.93}_{5 \text{ sig figs}} = \underbrace{4,094.1945}_{\text{reduce to 4 sig figs}}$$

The final answer, limited to four significant figures, is 4,094. The first digit dropped is 1, so we do not round up.

Scientific notation provides a way of communicating significant figures without ambiguity. You simply include all the significant figures in the leading number. For example, the number 450 has two significant figures and would be written in scientific notation as 4.5×10^2 , whereas 450.0 has four significant figures and would be written as 4.500×10^2 . In scientific notation, all significant figures are listed explicitly.

✓ Example 1.2.2.1

Write the answer for each expression using scientific notation with the appropriate number of significant figures.

a. 23.096×90.300

b. 125×9.000

Solution

a

Explanation	Answer
The calculator answer is 2,085.5688, but we need to round it to five significant figures. Because the first digit to be dropped (in the tenths place) is greater than 5, we round up to 2,085.6.	2.0856×10^3

b

Explanation	Answer
The calculator gives 1,125 as the answer, but we limit it to three significant figures.	1.13×10^3

Addition and Subtraction

How are significant figures handled in calculations? It depends on what type of calculation is being performed. If the calculation is an addition or a subtraction, the rule is as follows: limit the reported answer to the rightmost column that all numbers have significant figures in common. For example, if you were to add 1.2 and 4.71, we note that the first number stops its significant figures in the tenths column, while the second number stops its significant figures in the hundredths column. We therefore limit our answer to the tenths column.

$$\begin{array}{r}
 1.2 \\
 4.41 \\
 \hline
 5.61 \\
 \uparrow \text{ limit final answer to the tenths column: } 5.6
 \end{array}$$

We drop the last digit—the 1—because it is not significant to the final answer.

The dropping of positions in sums and differences brings up the topic of rounding. Although there are several conventions, in this text we will adopt the following rule: the final answer should be rounded up if the first dropped digit is 5 or greater, and rounded down if the first dropped digit is less than 5.

$$\begin{array}{r}
 77.2 \\
 10.46 \\
 \hline
 87.66 \\
 \uparrow \text{ limit final answer to the tenths column and round up: } 87.7
 \end{array}$$

✓ Example 1.2.2.2

a. $13.77 + 908.226$

b. $1,027 + 611 + 363.06$

Solution

a

Explanation	Answer
The calculator answer is 921.996, but because 13.77 has its farthest-right significant figure in the hundredths place, we need to round the final answer to the hundredths position. Because the first digit to be dropped (in the thousandths place) is greater than 5, we round up to 922.00	$922.00 = 9.2200 \times 10^2$

b

Explanation	Answer
The calculator gives 2,001.06 as the answer, but because 611 and 1027 has its farthest-right significant figure in the ones place, the final answer must be limited to the ones position.	$2,001.06 = 2.001 \times 10^3$

? Exercise 1.2.2.2

Write the answer for each expression using scientific notation with the appropriate number of significant figures.

- $217 \div 903$
- $13.77 + 908.226 + 515$
- $255.0 - 99$
- 0.00666×321

Answer a:

$$0.240 = 2.40 \times 10^{-1}$$

Answer b:

$$1,437 = 1.437 \times 10^3$$

Answer c:

$$156 = 1.56 \times 10^2$$

Answer d:

$$2.14 = 2.14 \times 10^0$$

Remember that calculators do not understand significant figures. *You* are the one who must apply the rules of significant figures to a result from your calculator.

Calculations Involving Multiplication/Division and Addition/Subtraction

In practice, chemists generally work with a calculator and carry all digits forward through subsequent calculations. When working on paper, however, we often want to minimize the number of digits we have to write out. Because successive rounding can compound inaccuracies, intermediate rounding needs to be handled correctly. When working on paper, always round an intermediate result so as to retain at least one more digit than can be justified and carry this number into the next step in the calculation. The final answer is then rounded to the correct number of significant figures at the very end.



Video 1.2.2.1: Significant figures in mixed operations (<https://www.youtube.com/watch?v=yBntMndXQWA>).



Video 1.2.2.2: https://www.youtube.com/watch?v=__csP0NtlGI

In the worked examples in this text, we will often show the results of intermediate steps in a calculation. In doing so, we will show the results to only the correct number of significant figures allowed for that step, in effect treating each step as a separate calculation. This procedure is intended to reinforce the rules for determining the number of significant figures, but in some cases it may give a final answer that differs in the last digit from that obtained using a calculator, where all digits are carried through to the last step.

✓ Example 1.2.2.3

- $2(1.008 \text{ g}) + 15.99 \text{ g}$
- $137.3 \text{ s} + 2(35.45 \text{ s})$
- $\frac{118.7 \text{ g}}{2} - 35.5 \text{ g}$

Solution

a.

Explanation	Answer

$$2(1.008 \text{ g}) + 15.99 \text{ g} =$$

Perform multiplication first.

$$2(1.008 \text{ g } 4 \text{ sig figs}) = 2.016 \text{ g } 4 \text{ sig figs}$$

The number with the least number of significant figures is 1.008 g; *the number 2 is an exact number and therefore has an infinite number of significant figures.*

Then, perform the addition.

$$2.016 \text{ g thousandths place} + 15.99 \text{ g hundredths place (least precise)} = 18.006 \text{ g}$$

Round the final answer.

Round the final answer to the hundredths place since 15.99 has its farthest right significant figure in the hundredths place (least precise).

18.01 g (rounding up)

b.

Explanation	Answer
$137.3 \text{ s} + 2(35.45 \text{ s}) =$ Perform multiplication first. $2(35.45 \text{ s } 4 \text{ sig figs}) = 70.90 \text{ s } 4 \text{ sig figs}$ The number with the least number of significant figures is 35.45; <i>the number 2 is an exact number and therefore has an infinite number of significant figures.</i> Then, perform the addition. $137.3 \text{ s tenths place (least precise)} + 70.90 \text{ s hundredths place} = 208.20 \text{ s}$ Round the final answer. Round the final answer to the tenths place based on 137.3 s.	208.2 s

c.

Explanation	Answer
$\frac{118.7 \text{ g}}{2} - 35.5 \text{ g} =$ Perform division first. $\frac{118.7 \text{ g}}{2} 4 \text{ sig figs} = 59.35 \text{ g } 4 \text{ sig figs}$ The number with the least number of significant figures is 118.7 g; <i>the number 2 is an exact number and therefore has an infinite number of significant figures.</i> Perform subtraction next. $59.35 \text{ g hundredths place} - 35.5 \text{ g tenths place (least precise)} = 23.85 \text{ g}$ Round the final answer. Round the final answer to the tenths place based on 35.5 g.	23.9 g (rounding up)

? Exercise 1.2.2.3

Complete the calculations and report your answers using the correct number of significant figures.

a. $5(1.008 \text{ s}) - 10.66 \text{ s}$

b. $99.0 \text{ cm} + 2(5.56 \text{ cm})$

Answer a

-5.62 s

Answer b

110.2 cm

Summary

- Rounding
 - If the number to be dropped is greater than or equal to 5, increase the number to its left by 1 (e.g. 2.9699 rounded to three significant figures is 2.97).
 - If the number to be dropped is less than 5, there is no change (e.g. 4.00443 rounded to four significant figures is 4.004).
- The rule in multiplication and division is that the final answer should have the same number of significant figures as there are in the number with the fewest significant figures.
- The rule in addition and subtraction is that the answer is given the same number of decimal places as the term with the fewest decimal places.

This page titled [1.2.2: Significant Figures in Calculations](#) is shared under a [mixed](#) license and was authored, remixed, and/or curated by [Anonymous](#).

- **2.4: Significant Figures in Calculations** by Henry Agnew, Marisa Alviar-Agnew is licensed [CK-12](#). Original source: <https://www.ck12.org/c/chemistry/>.