

14.5: Equilibrium Calculations for Gas-Phase and Heterogenous Reactions

Learning Objectives

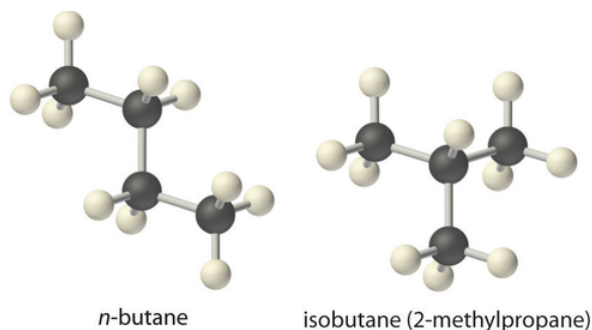
- To solve quantitative problems involving chemical equilibriums.

There are two fundamental kinds of equilibrium problems:

- those in which we are given the concentrations of the reactants and the products at equilibrium (or, more often, information that allows us to calculate these concentrations), and we are asked to calculate the equilibrium constant for the reaction; and
- those in which we are given the equilibrium constant and the initial concentrations of reactants, and we are asked to calculate the concentration of one or more substances at equilibrium. In this section, we describe methods for solving both kinds of problems.

Calculating an Equilibrium Constant from Equilibrium Concentrations

The equilibrium constant for the decomposition of $\text{CaCO}_{3(s)}$ to $\text{CaO}_{(s)}$ and $\text{CO}_{2(g)}$ is $K = [\text{CO}_2]$. At 800°C , the concentration of CO_2 in equilibrium with solid CaCO_3 and CaO is $2.5 \times 10^{-3} \text{ M}$. Thus K at 800°C is 2.5×10^{-3} (remember that equilibrium constants are unitless). A more complex example of this type of problem is the conversion of n-butane, an additive used to increase the volatility of gasoline, into isobutane (2-methylpropane).



This reaction can be written as follows:



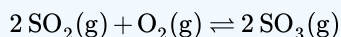
and the equilibrium constant $K = [\text{isobutane}]/[\text{n-butane}]$. At equilibrium, a mixture of n-butane and isobutane at room temperature was found to contain 0.041 M isobutane and 0.016 M n-butane. Substituting these concentrations into the equilibrium constant expression,

$$\begin{aligned}
 K &= \frac{[\text{isobutane}]}{[\text{n-butane}]} \\
 &= \frac{0.041 \text{ M}}{0.016 \text{ M}} \\
 &= 2.6
 \end{aligned}$$

Thus the equilibrium constant for the reaction as written is 2.6.

✓ Example 14.5.1

The reaction between gaseous sulfur dioxide and oxygen is a key step in the industrial synthesis of sulfuric acid:



A mixture of SO_2 and O_2 was maintained at 800 K until the system reached equilibrium. The equilibrium mixture contained

- $5.0 \times 10^{-2} \text{ M SO}_3$,

- $3.5 \times 10^{-3} \text{ M } O_2$, and
- $3.0 \times 10^{-3} \text{ M } SO_2$.

Calculate K and K_p at this temperature.

Given: balanced equilibrium equation and composition of equilibrium mixture

Asked for: equilibrium constant

Strategy

Write the equilibrium constant expression for the reaction. Then substitute the appropriate equilibrium concentrations into this equation to obtain K .

Solution

Substituting the appropriate equilibrium concentrations into the equilibrium constant expression,

$$K = \frac{[SO_3]^2}{[SO_2]^2[O_2]} = \frac{(5.0 \times 10^{-2})^2}{(3.0 \times 10^{-3})^2(3.5 \times 10^{-3})} = 7.9 \times 10^4$$

To solve for K_p , we need to identify Δn where $\Delta n = 2 - 3 = -1$ and then

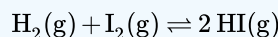
$$K_p = K(RT)^{\Delta n}$$

$$K_p = 7.9 \times 10^4 [(0.08206 \text{ L} \cdot \text{atm/mol} \cdot \text{K})(800\text{K})]^{-1}$$

$$K_p = 1.2 \times 10^3$$

? Exercise 14.5.1

Hydrogen gas and iodine react to form hydrogen iodide via the reaction



A mixture of H_2 and I_2 was maintained at 740 K until the system reached equilibrium. The equilibrium mixture contained

- $1.37 \times 10^{-2} \text{ M } HI$,
- $6.47 \times 10^{-3} \text{ M } H_2$, and
- $5.94 \times 10^{-4} \text{ M } I_2$.

Calculate K and K_p for this reaction.

Answer (K)

$$K = 48.8$$

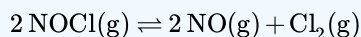
Answer (K_p)

$$K_p = 48.8$$

Chemists are not often given the concentrations of all the substances, and they are not likely to measure the equilibrium concentrations of all the relevant substances for a particular system. In such cases, we can obtain the equilibrium concentrations from the initial concentrations of the reactants and the balanced chemical equation for the reaction, as long as the equilibrium concentration of one of the substances is known. Example 14.5.2 shows one way to do this.

✓ Example 14.5.2

A 1.00 mol sample of $NOCl$ was placed in a 2.00 L reactor and heated to 227°C until the system reached equilibrium. The contents of the reactor were then analyzed and found to contain 0.056 mol of Cl_2 . Calculate K at this temperature. The equation for the decomposition of $NOCl$ to NO and Cl_2 is as follows:



Given: balanced equilibrium equation, amount of reactant, volume, and amount of one product at equilibrium

Asked for: K

Strategy:

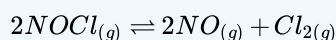
- Write the equilibrium constant expression for the reaction. Construct a table showing the initial concentrations, the changes in concentrations, and the final concentrations (as initial concentrations plus changes in concentrations).
- Calculate all possible initial concentrations from the data given and insert them in the table.
- Use the coefficients in the balanced chemical equation to obtain the changes in concentration of all other substances in the reaction. Insert those concentration changes in the table.
- Obtain the final concentrations by summing the columns. Calculate the equilibrium constant for the reaction.

Solution

A The first step in any such problem is to balance the chemical equation for the reaction (if it is not already balanced) and use it to derive the equilibrium constant expression. In this case, the equation is already balanced, and the equilibrium constant expression is as follows:

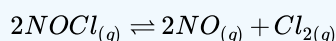
$$K = \frac{[NO]^2 [Cl_2]}{[NOCl]^2}$$

To obtain the concentrations of $NOCl$, NO , and Cl_2 at equilibrium, we construct a table showing what is known and what needs to be calculated. We begin by writing the balanced chemical equation at the top of the table, followed by three lines corresponding to the initial concentrations, the changes in concentrations required to get from the initial to the final state, and the final concentrations.



ICE	$[NOCl]$	$[NO]$	$[Cl_2]$
Initial			
Change			
Final			

B Initially, the system contains 1.00 mol of $NOCl$ in a 2.00 L container. Thus $[NOCl]_i = 1.00 \text{ mol}/2.00 \text{ L} = 0.500 \text{ M}$. The initial concentrations of NO and Cl_2 are 0 M because initially no products are present. Moreover, we are told that at equilibrium the system contains 0.056 mol of Cl_2 in a 2.00 L container, so $[Cl_2]_f = 0.056 \text{ mol}/2.00 \text{ L} = 0.028 \text{ M}$. We insert these values into the following table:



ICE	$[NOCl]$	$[NO]$	$[Cl_2]$
Initial	0.500	0	0
Change			
Final			0.028

C We use the stoichiometric relationships given in the balanced chemical equation to find the change in the concentration of Cl_2 , the substance for which initial and final concentrations are known:

$$\Delta[Cl_2] = 0.028 \text{ M}_{(final)} - 0.00 \text{ M}_{(initial)} = +0.028 \text{ M}$$

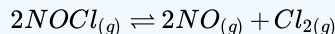
According to the coefficients in the balanced chemical equation, 2 mol of NO are produced for every 1 mol of Cl_2 , so the change in the NO concentration is as follows:

$$\Delta[NO] = \left(\frac{0.028 \text{ mol } \cancel{Cl_2}}{L} \right) \left(\frac{2 \text{ mol } NO}{1 \text{ mol } \cancel{Cl_2}} \right) = 0.056 \text{ M}$$

Similarly, 2 mol of $NOCl$ are consumed for every 1 mol of Cl_2 produced, so the change in the $NOCl$ concentration is as follows:

$$\Delta[NOCl] = \left(\frac{0.028 \text{ mol } \cancel{Cl_2}}{L} \right) \left(\frac{-2 \text{ mol } NOCl}{1 \text{ mol } \cancel{Cl_2}} \right) = -0.056 \text{ M}$$

We insert these values into our table:



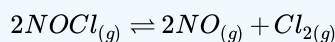
ICE	$[NOCl]$	$[NO]$	$[Cl_2]$
Initial	0.500	0	0
Change	-0.056	+0.056	+0.028
Final			0.028

D We sum the numbers in the $[NOCl]$ and $[NO]$ columns to obtain the final concentrations of NO and $NOCl$:

$$[NO]_f = 0.000 \text{ M} + 0.056 \text{ M} = 0.056 \text{ M}$$

$$[NOCl]_f = 0.500 \text{ M} + (-0.056 \text{ M}) = 0.444 \text{ M}$$

We can now complete the table:



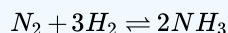
ICE	$[NOCl]$	$[NO]$	$[Cl_2]$
initial	0.500	0	0
change	-0.056	+0.056	+0.028
final	0.444	0.056	0.028

We can now calculate the equilibrium constant for the reaction:

$$K = \frac{[NO]^2[Cl_2]}{[NOCl]^2} = \frac{(0.056)^2(0.028)}{(0.444)^2} = 4.5 \times 10^{-4}$$

? Exercise 14.5.2

The German chemist Fritz Haber (1868–1934; Nobel Prize in Chemistry 1918) was able to synthesize ammonia (NH_3) by reacting 0.1248 M H_2 and 0.0416 M N_2 at about 500°C. At equilibrium, the mixture contained 0.00272 M NH_3 . What is K for the reaction



at this temperature? What is K_p ?

Answer (K)

$$K = 0.105$$

Answer (K_p)

$$K_p = 2.61 \times 10^{-5}$$

Calculating Equilibrium Concentrations from the Equilibrium Constant

To describe how to calculate equilibrium concentrations from an equilibrium constant, we first consider a system that contains only a single product and a single reactant, the conversion of n-butane to isobutane (Equation 14.5.1), for which $K = 2.6$ at 25°C . If we begin with a 1.00 M sample of n-butane, we can determine the concentration of n-butane and isobutane at equilibrium by constructing a table showing what is known and what needs to be calculated, just as we did in Example 14.5.2



ICE	[n-butane _(g)]	[isobutane _(g)]
Initial		
Change		
Final		

The initial concentrations of the reactant and product are both known: $[\text{n-butane}]_i = 1.00\text{ M}$ and $[\text{isobutane}]_i = 0\text{ M}$. We need to calculate the equilibrium concentrations of both n-butane and isobutane. Because it is generally difficult to calculate final concentrations directly, we focus on the change in the concentrations of the substances between the initial and the final (equilibrium) conditions. If, for example, we define the change in the concentration of isobutane ($\Delta[\text{isobutane}]$) as $+x$, then the change in the concentration of n-butane is $\Delta[\text{n-butane}] = -x$. This is because the balanced chemical equation for the reaction tells us that 1 mol of n-butane is consumed for every 1 mol of isobutane produced. We can then express the final concentrations in terms of the initial concentrations and the changes they have undergone.



ICE	[n-butane _(g)]	[isobutane _(g)]
Initial	1.00	0
Change	-x	+x
Final	$(1.00 - x)$	$(0 + x) = x$

Substituting the expressions for the final concentrations of n-butane and isobutane from the table into the equilibrium equation,

$$K = \frac{[\text{isobutane}]}{[\text{n-butane}]} = \frac{x}{1.00 - x} = 2.6 \quad (14.5.4)$$

Rearranging and solving for x ,

$$\begin{aligned} x &= 2.6(1.00 - x) = 2.6 - 2.6x \\ x + 2.6x &= 2.6 \\ x &= 0.72 \end{aligned}$$

We obtain the final concentrations by substituting this x value into the expressions for the final concentrations of n-butane and isobutane listed in the table:

$$[\text{n-butane}]_f = (1.00 - x)\text{M} = (1.00 - 0.72)\text{M} = 0.28\text{ M} \quad (14.5.5)$$

$$[\text{isobutane}]_f = (0.00 + x)\text{M} = (0.00 + 0.72)\text{M} = 0.72\text{ M} \quad (14.5.6)$$

We can check the results by substituting them back into the equilibrium constant expression to see whether they give the same K that we used in the calculation:

$$K = \frac{[\text{isobutane}]}{[\text{n-butane}]} = \left(\frac{0.72 \cancel{\text{M}}}{0.28 \cancel{\text{M}}} \right) = 2.6 \quad (14.5.7)$$

This is the same K we were given, so we can be confident of our results.

Example 14.5.3 illustrates a common type of equilibrium problem that you are likely to encounter.

✓ Example 14.5.3

The water–gas shift reaction is important in several chemical processes, such as the production of H_2 for fuel cells. This reaction can be written as follows:



$K = 0.106$ at 700 K. If a mixture of gases that initially contains 0.0150 M H_2 and 0.0150 M CO_2 is allowed to equilibrate at 700 K, what are the final concentrations of all substances present?

Given: balanced equilibrium equation, K , and initial concentrations

Asked for: final concentrations

Strategy:

- Construct a table showing what is known and what needs to be calculated. Define x as the change in the concentration of one substance. Then use the reaction stoichiometry to express the changes in the concentrations of the other substances in terms of x . From the values in the table, calculate the final concentrations.
- Write the equilibrium equation for the reaction. Substitute appropriate values from the ICE table to obtain x .
- Calculate the final concentrations of all species present. Check your answers by substituting these values into the equilibrium constant expression to obtain K .

Solution

A The initial concentrations of the reactants are $[H_2]_i = [CO_2]_i = 0.0150\text{ M}$. Just as before, we will focus on the change in the concentrations of the various substances between the initial and final states. If we define the change in the concentration of H_2O as x , then $\Delta[H_2O] = +x$. We can use the stoichiometry of the reaction to express the changes in the concentrations of the other substances in terms of x . For example, 1 mol of CO is produced for every 1 mol of H_2O , so the change in the CO concentration can be expressed as $\Delta[CO] = +x$. Similarly, for every 1 mol of H_2O produced, 1 mol each of H_2 and CO_2 are consumed, so the change in the concentration of the reactants is $\Delta[H_2] = \Delta[CO_2] = -x$. We enter the values in the following table and calculate the final concentrations.



ICE	$[H_2]$	$[CO_2]$	$[H_2O]$	$[CO]$
Initial	0.0150	0.0150	0	0
Change	$-x$	$-x$	$+x$	$+x$
Final	$(0.0150 - x)$	$(0.0150 - x)$	x	x

B We can now use the equilibrium equation and the given K to solve for x :

$$K = \frac{[H_2O][CO]}{[H_2][CO_2]} = \frac{(x)(x)}{(0.0150 - x)(0.0150 - x)} = \frac{x^2}{(0.0150 - x)^2} = 0.106$$

We could solve this equation with the quadratic formula, but it is far easier to solve for x by recognizing that the left side of the equation is a perfect square; that is,

$$\frac{x^2}{(0.0150 - x)^2} = \left(\frac{x}{0.0150 - x} \right)^2 = 0.106$$

Taking the square root of the middle and right terms,

$$\begin{aligned} \frac{x^2}{(0.0150 - x)^2} &= (0.106)^{1/2} = 0.326 \\ x &= (0.326)(0.0150) = 0.00489 \end{aligned}$$

$$1.326x = 0.00489$$

$$x = 0.00369 = 3.69 \times 10^{-3}$$

C The final concentrations of all species in the reaction mixture are as follows:

- $[H_2]_f = [H_2]_i + \Delta[H_2] = (0.0150 - 0.00369) M = 0.0113 M$
- $[CO_2]_f = [CO_2]_i + \Delta[CO_2] = (0.0150 - 0.00369) M = 0.0113 M$
- $[H_2O]_f = [H_2O]_i + \Delta[H_2O] = (0 + 0.00369) M = 0.00369 M$
- $[CO]_f = [CO]_i + \Delta[CO] = (0 + 0.00369) M = 0.00369 M$

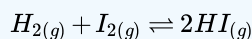
We can check our work by inserting the calculated values back into the equilibrium constant expression:

$$K = \frac{[H_2O][CO]}{[H_2][CO_2]} = \frac{(0.00369)^2}{(0.0113)^2} = 0.107$$

To two significant figures, this K is the same as the value given in the problem, so our answer is confirmed.

? Exercise 14.5.3

Hydrogen gas reacts with iodine vapor to give hydrogen iodide according to the following chemical equation:



$K = 54$ at 425°C . If $0.172 M H_2$ and I_2 are injected into a reactor and maintained at 425°C until the system equilibrates, what is the final concentration of each substance in the reaction mixture?

Answer

$$[HI]_f = 0.270 M \quad [H_2]_f = [I_2]_f = 0.037 M$$

In Example 14.5.3 the initial concentrations of the reactants were the same, which gave us an equation that was a perfect square and simplified our calculations. Often, however, the initial concentrations of the reactants are not the same, and/or one or more of the products may be present when the reaction starts. Under these conditions, there is usually no way to simplify the problem, and we must determine the equilibrium concentrations with other means. Such a case is described in Example 14.5.4

✓ Example 14.5.4

In the water–gas shift reaction shown in Example 14.5.3 a sample containing $0.632 M CO_2$ and $0.570 M H_2$ is allowed to equilibrate at $700 K$. At this temperature, $K = 0.106$. What is the composition of the reaction mixture at equilibrium?

Given: balanced equilibrium equation, concentrations of reactants, and K

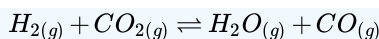
Asked for: composition of reaction mixture at equilibrium

Strategy:

- Write the equilibrium equation. Construct a table showing the initial concentrations of all substances in the mixture. Complete the table showing the changes in the concentrations (x) and the final concentrations.
- Write the equilibrium constant expression for the reaction. Substitute the known K value and the final concentrations to solve for x .
- Calculate the final concentration of each substance in the reaction mixture. Check your answers by substituting these values into the equilibrium constant expression to obtain K .

Solution

A $[CO_2]_i = 0.632 M$ and $[H_2]_i = 0.570 M$. Again, x is defined as the change in the concentration of H_2O : $\Delta[H_2O] = +x$. Because 1 mol of CO is produced for every 1 mol of H_2O , the change in the concentration of CO is the same as the change in the concentration of H_2O , so $\Delta[CO] = +x$. Similarly, because 1 mol each of H_2 and CO_2 are consumed for every 1 mol of H_2O produced, $\Delta[H_2] = \Delta[CO_2] = -x$. The final concentrations are the sums of the initial concentrations and the changes in concentrations at equilibrium.



ICE	$H_{2(g)}$	$CO_{2(g)}$	$H_2O_{(g)}$	$CO_{(g)}$
Initial	0.570	0.632	0	0
Change	-x	-x	+x	+x
Final	(0.570 - x)	(0.632 - x)	x	x

B We can now use the equilibrium equation and the known K value to solve for x :

$$K = \frac{[H_2O][CO]}{[H_2][CO_2]} = \frac{x^2}{(0.570 - x)(0.632 - x)} = 0.106$$

In contrast to Example 14.5.3 however, there is no obvious way to simplify this expression. Thus we must expand the expression and multiply both sides by the denominator:

$$x^2 = 0.106(0.360 - 1.20x + x^2)$$

Collecting terms on one side of the equation,

$$0.894x^2 + 0.127x - 0.0382 = 0$$

This equation can be solved using the quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-0.127 \pm \sqrt{(0.127)^2 - 4(0.894)(-0.0382)}}{2(0.894)}$$

$$x = 0.148 \text{ and } -0.290$$

Only the answer with the positive value has any physical significance, so $\Delta[H_2O] = \Delta[CO] = +0.148M$, and $\Delta[H_2] = \Delta[CO_2] = -0.148M$.

C The final concentrations of all species in the reaction mixture are as follows:

- $[H_2]_f = [H_2]_i + \Delta[H_2] = 0.570M - 0.148M = 0.422M$
- $[CO_2]_f = [CO_2]_i + \Delta[CO_2] = 0.632M - 0.148M = 0.484M$
- $[H_2O]_f = [H_2O]_i + \Delta[H_2O] = 0M + 0.148M = 0.148M$
- $[CO]_f = [CO]_i + \Delta[CO] = 0M + 0.148M = 0.148M$

We can check our work by substituting these values into the equilibrium constant expression:

$$K = \frac{[H_2O][CO]}{[H_2][CO_2]} = \frac{(0.148)^2}{(0.422)(0.484)} = 0.107$$

Because K is essentially the same as the value given in the problem, our calculations are confirmed.

? Exercise 14.5.4

The exercise in Example 14.5.1 showed the reaction of hydrogen and iodine vapor to form hydrogen iodide, for which $K = 54$ at 425°C . If a sample containing $0.200M H_2$ and $0.0450M I_2$ is allowed to equilibrate at 425°C , what is the final concentration of each substance in the reaction mixture?

Answer

$$[HI]_f = 0.0882M$$

$$[H_2]_f = 0.156M$$

$$[I_2]_f = 9.2 \times 10^{-4}M$$

In many situations it is not necessary to solve a quadratic (or higher-order) equation. Most of these cases involve reactions for which the equilibrium constant is either very small ($K \leq 10^{-3}$) or very large ($K \geq 10^3$), which means that the change in the concentration (defined as x) is essentially negligible compared with the initial concentration of a substance. Knowing this simplifies the calculations dramatically, as illustrated in Example 14.5.5

✓ Example 14.5.5

Atmospheric nitrogen and oxygen react to form nitric oxide:



with $K_p = 2.0 \times 10^{-31}$ at 25°C .

What is the partial pressure of NO in equilibrium with N_2 and O_2 in the atmosphere (at 1 atm) $P_{\text{N}_2} = 0.78 \text{ atm}$ and $P_{\text{O}_2} = 0.21 \text{ atm}$?

Given: balanced equilibrium equation and values of K_p , P_{O_2} , and P_{N_2}

Asked for: partial pressure of NO

Strategy:

- Construct a table and enter the initial partial pressures, the changes in the partial pressures that occur during the course of the reaction, and the final partial pressures of all substances.
- Write the equilibrium equation for the reaction. Then substitute values from the table to solve for the change in concentration (x).
- Calculate the partial pressure of NO. Check your answer by substituting values into the equilibrium equation and solving for K .

Solution

A Because we are given K_p and partial pressures are reported in atmospheres, we will use partial pressures. The initial partial pressure of O_2 is 0.21 atm and that of N_2 is 0.78 atm. If we define the change in the partial pressure of NO as $2x$, then the change in the partial pressure of O_2 and of N_2 is $-x$ because 1 mol each of N_2 and of O_2 is consumed for every 2 mol of NO produced. Each substance has a final partial pressure equal to the sum of the initial pressure and the change in that pressure at equilibrium.



ICE	P_{N_2}	P_{O_2}	P_{NO}
Initial	0.78	0.21	0
Change	$-x$	$-x$	$+2x$
Final	$(0.78 - x)$	$(0.21 - x)$	$2x$

B Substituting these values into the equation for the equilibrium constant,

$$K_p = \frac{(P_{\text{NO}})^2}{(P_{\text{N}_2})(P_{\text{O}_2})} = \frac{(2x)^2}{(0.78 - x)(0.21 - x)} = 2.0 \times 10^{-31}$$

In principle, we could multiply out the terms in the denominator, rearrange, and solve the resulting quadratic equation. In practice, it is far easier to recognize that an equilibrium constant of this magnitude means that the extent of the reaction will be very small; therefore, the x value will be negligible compared with the initial concentrations. If this assumption is correct, then to two significant figures, $(0.78 - x) = 0.78$ and $(0.21 - x) = 0.21$. Substituting these expressions into our original equation,

$$\frac{(2x)^2}{(0.78)(0.21)} = 2.0 \times 10^{-31}$$

$$\frac{4x^2}{0.16} = 2.0 \times 10^{-31}$$

$$x^2 = \frac{0.33 \times 10^{-31}}{4}$$

$$x = 9.1 \times 10^{-17}$$

C Substituting this value of x into our expressions for the final partial pressures of the substances,

- $P_{NO} = 2x \text{ atm} = 1.8 \times 10^{-16} \text{ atm}$
- $P_{N_2} = (0.78 - x) \text{ atm} = 0.78 \text{ atm}$
- $P_{O_2} = (0.21 - x) \text{ atm} = 0.21 \text{ atm}$

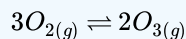
From these calculations, we see that our initial assumption regarding x was correct: given two significant figures, 2.0×10^{-16} is certainly negligible compared with 0.78 and 0.21. When can we make such an assumption? As a general rule, if x is less than about 5% of the total, or $10^{-3} > K > 10^3$, then the assumption is justified. Otherwise, we must use the quadratic formula or some other approach. The results we have obtained agree with the general observation that toxic NO , an ingredient of smog, does not form from atmospheric concentrations of N_2 and O_2 to a substantial degree at 25°C . We can verify our results by substituting them into the original equilibrium equation:

$$K_p = \frac{(P_{NO})^2}{(P_{N_2})(P_{O_2})} = \frac{(1.8 \times 10^{-16})^2}{(0.78)(0.21)} = 2.0 \times 10^{-31}$$

The final K_p agrees with the value given at the beginning of this example.

? Exercise 14.5.5

Under certain conditions, oxygen will react to form ozone, as shown in the following equation:



with $K_p = 2.5 \times 10^{-59}$ at 25°C . What ozone partial pressure is in equilibrium with oxygen in the atmosphere ($P_{O_2} = 0.21 \text{ atm}$)?

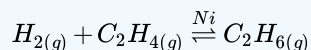
Answer

$$4.8 \times 10^{-31} \text{ atm}$$

Another type of problem that can be simplified by assuming that changes in concentration are negligible is one in which the equilibrium constant is very large ($K \geq 10^3$). A large equilibrium constant implies that the reactants are converted almost entirely to products, so we can assume that the reaction proceeds 100% to completion. When we solve this type of problem, we view the system as equilibrating from the products side of the reaction rather than the reactants side. This approach is illustrated in Example 14.5.6

✓ Example 14.5.6

The chemical equation for the reaction of hydrogen with ethylene (C_2H_4) to give ethane (C_2H_6) is as follows:



with $K = 9.6 \times 10^{18}$ at 25°C . If a mixture of 0.200 M H_2 and 0.155 M C_2H_4 is maintained at 25°C in the presence of a powdered nickel catalyst, what is the equilibrium concentration of each substance in the mixture?

Given: balanced chemical equation, K , and initial concentrations of reactants

Asked for: equilibrium concentrations

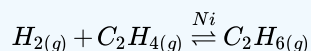
Strategy:

- Construct a table showing initial concentrations, concentrations that would be present if the reaction were to go to completion, changes in concentrations, and final concentrations.
- Write the equilibrium constant expression for the reaction. Then substitute values from the table into the expression to solve for x (the change in concentration).

C. Calculate the equilibrium concentrations. Check your answers by substituting these values into the equilibrium equation.

Solution:

A From the magnitude of the equilibrium constant, we see that the reaction goes essentially to completion. Because the initial concentration of ethylene (0.155 M) is less than the concentration of hydrogen (0.200 M), ethylene is the limiting reactant; that is, no more than 0.155 M ethane can be formed from 0.155 M ethylene. If the reaction were to go to completion, the concentration of ethane would be 0.155 M and the concentration of ethylene would be 0 M. Because the concentration of hydrogen is greater than what is needed for complete reaction, the concentration of unreacted hydrogen in the reaction mixture would be 0.200 M – 0.155 M = 0.045 M. The equilibrium constant for the forward reaction is very large, so the equilibrium constant for the reverse reaction must be very small. The problem then is identical to that in Example 14.5.5 If we define $-x$ as the change in the ethane concentration for the reverse reaction, then the change in the ethylene and hydrogen concentrations is $+x$. The final equilibrium concentrations are the sums of the concentrations for the forward and reverse reactions.



<i>IACE</i>	$[H_{2(g)}]$	$[C_2H_{4(g)}]$	$[C_2H_{6(g)}]$
Initial	0.200	0.155	0
Assuming 100% reaction	0.045	0	0.155
Change	$+x$	$+x$	$-x$
Final	$(0.045 + x)$	$(0 + x)$	$(0.155 - x)$

B Substituting values into the equilibrium constant expression,

$$K = \frac{[C_2H_6]}{[H_2][C_2H_4]} = \frac{0.155 - x}{(0.045 + x)x} = 9.6 \times 10^{18}$$

Once again, the magnitude of the equilibrium constant tells us that the equilibrium will lie far to the right as written, so the reverse reaction is negligible. Thus x is likely to be very small compared with either 0.155 M or 0.045 M, and the equation can be simplified [$(0.045 + x) = 0.045$ and $(0.155 - x) = 0.155$] as follows:

$$K = \frac{0.155}{0.045x} = 9.6 \times 10^{18}$$

$$x = 3.6 \times 10^{-19}$$

C The small x value indicates that our assumption concerning the reverse reaction is correct, and we can therefore calculate the final concentrations by evaluating the expressions from the last line of the table:

- $[C_2H_6]_f = (0.155 - x) \text{ M} = 0.155 \text{ M}$
- $[C_2H_4]_f = x \text{ M} = 3.6 \times 10^{-19} \text{ M}$
- $[H_2]_f = (0.045 + x) \text{ M} = 0.045 \text{ M}$

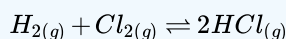
We can verify our calculations by substituting the final concentrations into the equilibrium constant expression:

$$K = \frac{[C_2H_6]}{[H_2][C_2H_4]} = \frac{0.155}{(0.045)(3.6 \times 10^{-19})} = 9.6 \times 10^{18}$$

This K value agrees with our initial value at the beginning of the example.

? Exercise 14.5.6

Hydrogen reacts with chlorine gas to form hydrogen chloride:



with $K_p = 4.0 \times 10^{31}$ at 47°C . If a mixture of $0.257\text{ M } H_2$ and $0.392\text{ M } Cl_2$ is allowed to equilibrate at 47°C , what is the equilibrium composition of the mixture?

Answer

$$[H_2]_f = 4.8 \times 10^{-32}\text{ M}$$

$$[Cl_2]_f = 0.135\text{ M}$$

$$[HCl]_f = 0.514\text{ M}$$

Summary

Various methods can be used to solve the two fundamental types of equilibrium problems:

1. those in which we calculate the concentrations of reactants and products at equilibrium and
2. those in which we use the equilibrium constant and the initial concentrations of reactants to determine the composition of the equilibrium mixture.

When an equilibrium constant is calculated from equilibrium concentrations, molar concentrations or partial pressures are substituted into the equilibrium constant expression for the reaction. Equilibrium constants can be used to calculate the equilibrium concentrations of reactants and products by using the quantities or concentrations of the reactants, the stoichiometry of the balanced chemical equation for the reaction, and a tabular format to obtain the final concentrations of all species at equilibrium.

14.5: Equilibrium Calculations for Gas-Phase and Heterogenous Reactions is shared under a [CC BY-NC-SA 4.0](#) license and was authored, remixed, and/or curated by LibreTexts.