

13.7: The Gibbs Free Energy

Learning Objectives

- To understand the relationship between Gibbs free energy and work.

One of the major goals of chemical thermodynamics is to establish criteria for predicting whether a particular reaction or process will occur spontaneously. We have developed one such criterion, the change in entropy of the universe: if $\Delta S_{univ} > 0$ for a process or a reaction, then the process will occur spontaneously as written. Conversely, if $\Delta S_{univ} < 0$, a process cannot occur spontaneously; if $\Delta S_{univ} = 0$, the system is at equilibrium. The sign of ΔS_{univ} is a universally applicable and infallible indicator of the spontaneity of a reaction. Unfortunately, using ΔS_{univ} requires that we calculate ΔS for **both a system and its surroundings**. This is not particularly useful for two reasons: we are normally much more interested in the system than in the surroundings, and it is difficult to make quantitative measurements of the surroundings (i.e., the rest of the universe). A criterion of spontaneity that is based solely on the state functions of a system would be much more convenient and is provided by a new state function: the Gibbs free energy.

Gibbs Energy and Spontaneity

The Gibbs energy (also known as the *Gibbs function*) is defined as

$$G_{sys} = H_{sys} - TS_{sys} \quad (13.7.1)$$

in which S refers to the entropy of the *system*. Since H , T and S are all state functions, so is G . Thus for any change in state, we can expand Equation 13.7.1 to

$$\Delta G_{sys} = \Delta H_{sys} - T \Delta S_{sys} \quad (13.7.2)$$

How does this simple equation relate to the entropy change of the universe ΔS_{univ} that we know is the sole criterion for spontaneous change from the second law of thermodynamics? Starting with the definition

$$\Delta S_{univ} = \Delta S_{surr} + \Delta S_{sys} \quad (13.7.3)$$

we would first like to get rid of ΔS_{surr} . How can a chemical reaction (a change in the *system*) affect the entropy of the *surroundings*? Because most reactions are either exothermic or endothermic, they are accompanied by heat q_p across the system boundary (we are considering constant pressure processes). The enthalpy change of the reaction ΔH_{sys} is the "flow" of heat into the system from the surroundings under constant pressure, so the heat "withdrawn" from the surroundings will be $-q_p$.

From the thermodynamic definition of entropy, the change of the entropy of the surroundings will be

$$\Delta S_{surr} = -\frac{q_p}{T} = -\frac{\Delta H_{sys}}{T} \quad (13.7.4)$$

We can therefore rewrite Equation 13.7.3 as

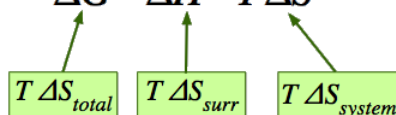
$$\Delta S_{univ} = \frac{-\Delta H_{sys}}{T} + \Delta S_{sys} \quad (13.7.5)$$

Multiplying through by $-T$, we obtain

$$-T \Delta S_{univ} = \Delta H_{sys} - T \Delta S_{sys} \quad (13.7.6)$$

which expresses the entropy change of the universe in terms of thermodynamic properties of the *system* exclusively.

If $-T \Delta S_{univ}$ is denoted by ΔG , then we have Equation 13.7.2 which defines the *Gibbs energy* change for the process.

$$\Delta G = \Delta H - T \Delta S$$


$T \Delta S_{total}$

$T \Delta S_{surr}$

$T \Delta S_{system}$

The criterion for predicting spontaneity is based on (ΔG), the change in G , at constant temperature and pressure. Although very few chemical reactions actually occur under conditions of constant temperature and pressure, most systems can be brought back to the initial temperature and pressure without significantly affecting the value of thermodynamic state functions such as G . At constant temperature and pressure,

$$\Delta G = \Delta H - T\Delta S \quad (13.7.7)$$

where all thermodynamic quantities are those of the system. Recall that at constant pressure, $\Delta H = q$, whether a process is reversible or irreversible, and

$$T\Delta S = q_{rev} \quad (13.7.8)$$

Using these expressions, we can reduce Equation 13.7.7 to

$$\Delta G = q - q_{rev} \quad (13.7.9)$$

Thus ΔG is the difference between the heat released during a process (via a reversible or an irreversible path) and the heat released for the same process occurring in a reversible manner. Under the special condition in which a process occurs reversibly, $q = q_{rev}$ and $\Delta G = 0$. As we shall soon see, if ΔG is zero, the system is at equilibrium, and there will be no net change.

What about processes for which $\Delta G \neq 0$? To understand how the sign of ΔG for a system determines the direction in which change is spontaneous, we can rewrite the relationship between ΔS and q_{rev} , discussed earlier.

$$\Delta S = \frac{q_{rev}}{T}$$

with the definition of ΔH in terms of q_{rev}

$$q_{rev} = \Delta H$$

to obtain

$$\Delta S_{surr} = -\frac{\Delta H_{sys}}{T} \quad (13.7.10)$$

Thus the entropy change of the surroundings is related to the enthalpy change of the system. We have stated that for a spontaneous reaction, $\Delta S_{univ} > 0$, so substituting we obtain

$$\begin{aligned} \Delta S_{univ} &= \Delta S_{sys} + \Delta S_{surr} > 0 \\ &= \Delta S_{sys} - \frac{\Delta H_{sys}}{T} > 0 \end{aligned}$$

Multiplying both sides of the inequality by $-T$ reverses the sign of the inequality; rearranging,

$$\Delta H_{sys} - T\Delta S_{sys} < 0 \quad (13.7.11)$$

which is equal to ΔG (Equation 13.7.7). We can therefore see that for a spontaneous process, $\Delta G_{sys} < 0$.

The relationship between the entropy change of the surroundings and the heat gained or lost by the system provides the key connection between the thermodynamic properties of the system and the change in entropy of the universe. The relationship shown in Equation 13.7.7 allows us to predict spontaneity by focusing exclusively on the thermodynamic properties and temperature of the system. We predict that highly exothermic processes ($\Delta H \ll 0$) that increase the entropy of a system ($\Delta S_{sys} \gg 0$) would therefore occur spontaneously. An example of such a process is the decomposition of ammonium nitrate fertilizer. Ammonium nitrate was also used to destroy the Murrah Federal Building in Oklahoma City, Oklahoma, in 1995. For a system at constant temperature and pressure, we can summarize the following results:

- If $\Delta G < 0$, the process occurs spontaneously.
- If $\Delta G = 0$, the system is at equilibrium.
- If $\Delta G > 0$, the process is not spontaneous as written but occurs spontaneously in the reverse direction.

To further understand how the various components of ΔG dictate whether a process occurs spontaneously, we now look at a simple and familiar physical change: the conversion of liquid water to water vapor.

✓ Example 13.7.1: Vaporizing Water

At Room Temperature (100 °C)

If the conversion of liquid water to water vapor is carried out at 1 atm and the normal boiling point of 100.00 °C (373.15 K), we can calculate ΔG from the experimentally measured value of ΔH_{vap} (40.657 kJ/mol). For vaporizing 1 mol of water, $\Delta H = 40,657 \text{ J}$, so the process is highly endothermic. From the definition of ΔS (Equation 13.7.10), we know that for 1 mol of water,

$$\begin{aligned}\Delta S_{\text{vap}} &= \frac{\Delta H_{\text{vap}}}{T_{\text{b}}} \\ &= \frac{40,657 \text{ J}}{373.15 \text{ K}} \\ &= 108.96 \text{ J/K}\end{aligned}$$

Hence there is an increase in the disorder of the system. At the normal boiling point of water,

$$\begin{aligned}\Delta G_{100^\circ\text{C}} &= \Delta H_{100^\circ\text{C}} - T\Delta S_{100^\circ\text{C}} \\ &= 40,657 \text{ J} - [(373.15 \text{ K})(108.96 \text{ J/K})] \\ &= 0 \text{ J}\end{aligned}$$

The energy required for vaporization offsets the increase in entropy of the system. Thus $\Delta G = 0$, and the liquid and vapor are in equilibrium, as is true of any liquid at its boiling point under standard conditions.

Above Room Temperature (110 °C)

Now suppose we were to superheat 1 mol of liquid water to 110°C. The value of ΔG for the vaporization of 1 mol of water at 110°C, assuming that ΔH and ΔS do not change significantly with temperature, becomes

$$\begin{aligned}\Delta G_{110^\circ\text{C}} &= \Delta H - T\Delta S \\ &= 40,657 \text{ J} - [(383.15 \text{ K})(108.96 \text{ J/K})] \\ &= -1,091 \text{ J}\end{aligned}$$

Since $\Delta G < 0$, the vaporization of water is predicted to occur spontaneously and irreversibly at 110 °C.

Below Room Temperature (90 °C)

We can also calculate ΔG for the vaporization of 1 mol of water at a temperature below its normal boiling point—for example, 90°C—making the same assumptions:

$$\begin{aligned}\Delta G_{90^\circ\text{C}} &= \Delta H - T\Delta S \\ &= 40,657 \text{ J} - [(363.15 \text{ K})(108.96 \text{ J/K})] \\ &= 1,088 \text{ J}\end{aligned}$$

Since $\Delta G > 0$, water does not spontaneously convert to water vapor at 90 °C. When using all the digits in the calculator display in carrying out our calculations, $\Delta G_{110^\circ\text{C}} = 1090 \text{ J} = -\Delta G_{90^\circ\text{C}}$, as we would predict.

Equilibrium Temperature

We can also calculate the temperature at which liquid water is in equilibrium with water vapor. Inserting the values of ΔH and ΔS into the definition of ΔG (Equation 13.7.7), setting $\Delta G = 0$, and solving for T ,

$$\begin{aligned}0 &= 40,657 \text{ J} - T(108.96 \text{ J/K}) \\ T &= 373.15 \text{ K}\end{aligned}$$

Thus $\Delta G = 0$ at $T = 373.15 \text{ K}$ and 1 atm, which indicates that liquid water and water vapor are in equilibrium; this temperature is called the normal boiling point of water.

At temperatures greater than 373.15 K, ΔG is negative, and water evaporates spontaneously and irreversibly. Below 373.15 K, ΔG is positive, and water does not evaporate spontaneously. Instead, water vapor at a temperature less than 373.15 K and 1

atm will spontaneously and irreversibly condense to liquid water. Figure 13.7.1 shows how the ΔH and $T\Delta S$ terms vary with temperature for the vaporization of water. When the two lines cross, $\Delta G = 0$, and $\Delta H = T\Delta S$.

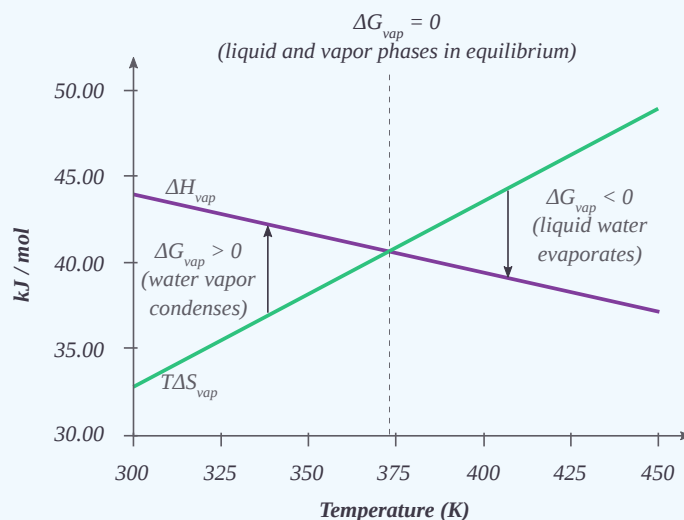


Figure 13.7.1: Temperature Dependence of ΔH and $T\Delta S$ for the Vaporization of Water. Both ΔH and $T\Delta S$ are temperature dependent, but the lines have opposite slopes and cross at 373.15 K at 1 atm, where $\Delta H = T\Delta S$. Because $\Delta G = \Delta H - T\Delta S$, at this temperature $\Delta G = 0$, indicating that the liquid and vapor phases are in equilibrium. The normal boiling point of water is therefore 373.15 K. Above the normal boiling point, the $T\Delta S$ term is greater than ΔH , making $\Delta G < 0$; hence, liquid water evaporates spontaneously. Below the normal boiling point, the ΔH term is greater than $T\Delta S$, making $\Delta G > 0$. Thus liquid water does not evaporate spontaneously, but water vapor spontaneously condenses to liquid. (CC BY-NC; Ümit Kaya)

A similar situation arises in the conversion of liquid egg white to a solid when an egg is boiled. The major component of egg white is a protein called albumin, which is held in a compact, ordered structure by a large number of hydrogen bonds. Breaking them requires an input of energy ($\Delta H > 0$), which converts the albumin to a highly disordered structure in which the molecules aggregate as a disorganized solid ($\Delta S > 0$). At temperatures greater than 373 K, the $T\Delta S$ term dominates, and $\Delta G < 0$, so the conversion of a raw egg to a hard-boiled egg is an irreversible and spontaneous process above 373 K.

Figure 13.7.1

ΔH	ΔS	$-T\Delta S$	ΔG
- (exothermic)	+ (products more disordered)	- (favors spontaneity)	- (spontaneous at all T)
- (exothermic)	- (products less disordered)	+ (opposes spontaneity)	- (spontaneous) at low T + (non-spontaneous) at high T "Enthalpically-driven process"
+ (endothermic)	+ (products more disordered)	- (favors spontaneity)	+ (non-spontaneous) at low T - (spontaneous) at high T "Entropically-driven process"
+ (endothermic)	- (products less disordered)	+ (opposes spontaneity)	+ (non-spontaneous at all T)

Enthalpically vs. Entropically Driving Reactions

Some textbooks and teachers say that the free energy, and thus the spontaneity of a reaction, depends on both the enthalpy and entropy changes of a reaction, and they sometimes even refer to reactions as "energy driven" or "entropy driven" depending on whether ΔH or the $T\Delta S$ term dominates. This is technically correct, but misleading because it disguises the important fact that ΔS_{total} , which this equation expresses in an indirect way, is the *only* criterion of spontaneous change.

Consider the following possible states for two different types of molecules with some attractive force:

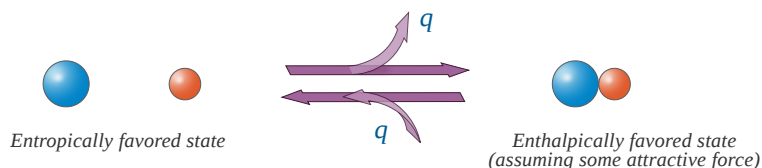


Figure 13.7.2: An enthalpic favored reaction. (CC BY-NC; Ümit Kaya)

There would appear to be greater entropy on the left (state 1) than on the right (state 2). Thus the entropic change for the reaction as written (i.e. going to the right) would be (-) in magnitude, and the energetic contribution to the free energy change would be (+) (i.e. unfavorable) for the reaction as written.

In going to the right, there is an attractive force and the molecules adjacent to each other is a lower energy state (heat energy, q , is liberated). To go to the left, we have to overcome this attractive force (input heat energy) and the left direction is unfavorable with regard to heat energy q . The change in enthalpy is (-) in going to the right (q released), and this enthalpy change is negative (-) in going to the right (and (+) in going to the left). This reaction as written, is therefore, *enthalpically favorable* and *entropically unfavorable*. Hence, It is *enthalpically driven*.

From Table 13.7.1, it would appear that we might be able to get the reaction to go to the right at low temperatures (lower temperature would minimize the energetic contribution of the entropic change). Looking at the same process from an opposite direction:

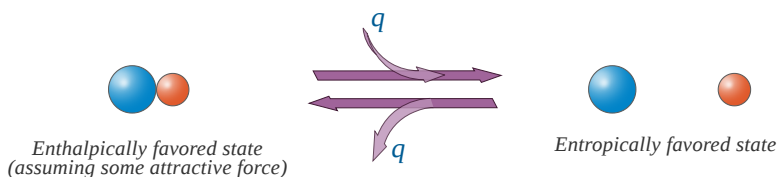


Figure 13.7.3: An entropically favored reaction. (CC BY-NC; Ümit Kaya)

This reaction as written, is *entropically favorable*, and *enthalpically unfavorable*; it is *entropically driven*. From Table 13.7.1, it would appear that we might be able to get the reaction to go to the right at high temperatures (high temperature would increase the energetic contribution of the entropic change).

The Relationship between ΔG and Work

In the previous subsection, we learned that the value of ΔG allows us to predict the spontaneity of a physical or a chemical change. In addition, the magnitude of ΔG for a process provides other important information. The change in Gibbs energy is equal to the maximum amount of work that a system can perform on the surroundings while undergoing a spontaneous change (at constant temperature and pressure):

$$\Delta G = w_{max} \quad (13.7.12)$$

To see why this is true, let's look again at the relationships among free energy, enthalpy, and entropy expressed in Equation 13.7.7. We can rearrange this equation as follows:

$$\Delta H = \Delta G + T\Delta S \quad (13.7.13)$$

This equation tells us that when energy is released during an exothermic process ($\Delta H < 0$), such as during the combustion of a fuel, some of that energy can be used to do work ($\Delta G < 0$), while some is used to increase the entropy of the universe ($T\Delta S > 0$). Only if the process occurs infinitely slowly in a perfectly reversible manner will the entropy of the universe be unchanged. Because no real system is perfectly reversible, the entropy of the universe increases during all processes that produce energy. As a result, no process that uses stored energy can ever be 100% efficient; that is, ΔH will never equal ΔG because ΔS has a positive value.

One of the major challenges facing engineers is to maximize the efficiency of converting stored energy to useful work or converting one form of energy to another. As indicated in Table 13.7.2 the efficiencies of various energy-converting devices vary widely. For example, an internal combustion engine typically uses only 25%–30% of the energy stored in the hydrocarbon fuel to perform work; the rest of the stored energy is released in an unusable form as heat. In contrast, gas–electric hybrid engines, now used in several models of automobiles, deliver approximately 50% greater fuel efficiency. A large electrical generator is highly efficient (approximately 99%) in converting mechanical to electrical energy, but a typical incandescent light bulb is one of the least efficient devices known (only approximately 5% of the electrical energy is converted to light). In contrast, a mammalian liver cell is a relatively efficient machine and can use fuels such as glucose with an efficiency of 30%–50%.

Table 13.7.2: Approximate Thermodynamic Efficiencies of Various Devices

Device	Energy Conversion	Approximate Efficiency (%)
large electrical generator	mechanical → electrical	99
chemical battery	chemical → electrical	90
home furnace	chemical → heat	65
small electric tool	electrical → mechanical	60
space shuttle engine	chemical → mechanical	50
mammalian liver cell	chemical → chemical	30–50
spinach cell	light → chemical	30
internal combustion engine	chemical → mechanical	25–30
fluorescent light	electrical → light	20
solar cell	light → electricity	10
incandescent light bulb	electricity → light	5
yeast cell	chemical → chemical	2–4

Standard Free-Energy Change

We have seen that there is no way to measure absolute enthalpies, although we can measure changes in enthalpy (ΔH) during a chemical reaction. Because enthalpy is one of the components of Gibbs free energy, we are consequently unable to measure absolute free energies; we can measure only changes in free energy. The standard free-energy change (ΔG°) is the change in free energy when one substance or a set of substances in their standard states is converted to one or more other substances, also in their standard states. The standard free-energy change can be calculated from the definition of free energy, if the standard enthalpy and entropy changes are known, using Equation 13.7.14

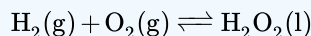
$$\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ \quad (13.7.14)$$

If ΔS° and ΔH° for a reaction have the same sign, then the sign of ΔG° depends on the relative magnitudes of the ΔH° and $T\Delta S^\circ$ terms. It is important to recognize that a positive value of ΔG° for a reaction does not mean that no products will form if the reactants in their standard states are mixed; it means only that at equilibrium the concentrations of the products will be less than the concentrations of the reactants.

A positive ΔG° means that the equilibrium constant is less than 1.

✓ Example 13.7.1

Calculate the standard free-energy change (ΔG°) at 25°C for the reaction



At 25°C, the standard enthalpy change (ΔH°) is -187.78 kJ/mol , and the absolute entropies of the products and reactants are:

- $S^\circ(\text{H}_2\text{O}_2) = 109.6 \text{ J/(mol}\cdot\text{K)}$,
- $S^\circ(\text{O}_2) = 205.2 \text{ J/(mol}\cdot\text{K)}$, and
- $S^\circ(\text{H}_2) = 130.7 \text{ J/(mol}\cdot\text{K)}$.

Is the reaction spontaneous as written?

Given: balanced chemical equation, ΔH° and S° for reactants and products

Asked for: spontaneity of reaction as written

Strategy:

- Calculate ΔS° from the absolute molar entropy values given.
- Use Equation 13.7.14 the calculated value of ΔS° , and other data given to calculate ΔG° for the reaction.
- Use the value of ΔG° to determine whether the reaction is spontaneous as written.

Solution

A To calculate ΔG° for the reaction, we need to know ΔH° , ΔS° , and T. We are given ΔH° , and we know that $T = 298.15 \text{ K}$. We can calculate ΔS° from the absolute molar entropy values provided using the “products minus reactants” rule:

$$\begin{aligned}\Delta S^\circ &= S^\circ(\text{H}_2\text{O}_2) - [S^\circ(\text{O}_2) + S^\circ(\text{H}_2)] \\ &= [1 \text{ mol H}_2\text{O}_2 \times 109.6 \text{ J/(mol}\cdot\text{K)}] \\ &\quad - \{[1 \text{ mol H}_2 \times 130.7 \text{ J/(mol}\cdot\text{K)}] + [1 \text{ mol O}_2 \times 205.2 \text{ J/(mol}\cdot\text{K)}]\} \\ &= -226.3 \text{ J/K (per mole of H}_2\text{O}_2)\end{aligned}$$

As we might expect for a reaction in which 2 mol of gas is converted to 1 mol of a much more ordered liquid, ΔS° is very negative for this reaction.

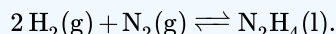
B Substituting the appropriate quantities into Equation 13.7.14

$$\begin{aligned}\Delta G^\circ &= \Delta H^\circ - T\Delta S^\circ \\ &= -187.78 \text{ kJ/mol} - (298.15 \text{ K})[-226.3 \text{ J/(mol}\cdot\text{K)} \times 1 \text{ kJ/1000 J}] \\ &= -187.78 \text{ kJ/mol} + 67.47 \text{ kJ/mol} \\ &= -120.31 \text{ kJ/mol}\end{aligned}$$

The negative value of ΔG° indicates that the reaction is spontaneous as written. Because ΔS° and ΔH° for this reaction have the same sign, the sign of ΔG° depends on the relative magnitudes of the ΔH° and $T\Delta S^\circ$ terms. In this particular case, the enthalpy term dominates, indicating that the strength of the bonds formed in the product more than compensates for the unfavorable ΔS° term and for the energy needed to break bonds in the reactants.

? Exercise 13.7.1

Calculate the standard free-energy change (ΔG°) at 25°C for the reaction



At 25°C, the standard enthalpy change (ΔH°) is 50.6 kJ/mol , and the absolute entropies of the products and reactants are S° (N_2H_4) = $121.2 \text{ J/(mol}\cdot\text{K)}$, $S^\circ(\text{N}_2) = 191.6 \text{ J/(mol}\cdot\text{K)}$, and $S^\circ(\text{H}_2) = 130.7 \text{ J/(mol}\cdot\text{K)}$. Is the reaction spontaneous as written?

Answer

149.5 kJ/mol; no

Tabulated values of standard free energies of formation allow chemists to calculate the values of ΔG° for a wide variety of chemical reactions rather than having to measure them in the laboratory. The standard free energy of formation (ΔG_f°) of a compound is the change in free energy that occurs when 1 mol of a substance in its standard state is formed from the component elements in their standard states. By definition, the standard free energy of formation of an element in its standard state is zero at 298.15 K. One mole of Cl_2 gas at 298.15 K, for example, has $\Delta G_f^\circ = 0$. The standard free energy of formation of a compound can be calculated from the standard enthalpy of formation (ΔH_f°) and the standard entropy of formation (ΔS_f°) using the definition of free energy:

$$\Delta G_f^\circ = \Delta H_f^\circ - T\Delta S_f^\circ \quad (13.7.15)$$

Using standard free energies of formation to calculate the standard free energy of a reaction is analogous to calculating standard enthalpy changes from standard enthalpies of formation using the familiar “products minus reactants” rule:

$$\Delta G_{\text{rxn}}^\circ = \sum m\Delta G_f^\circ(\text{products}) - \sum n\Delta G_f^\circ(\text{reactants}) \quad (13.7.16)$$

where m and n are the stoichiometric coefficients of each product and reactant in the balanced chemical equation. A very large negative ΔG° indicates a strong tendency for products to form spontaneously from reactants; it does not, however, necessarily indicate that the reaction will occur rapidly. To make this determination, we need to evaluate the kinetics of the reaction.

“Products minus Reactants” Rule

The ΔG° of a reaction can be calculated from tabulated ΔG_f° values ([Table T1](#)) using the “products minus reactants” rule.

Example 13.7.2

Calculate ΔG° for the reaction of isooctane with oxygen gas to give carbon dioxide and water. Use the following data:

- $\Delta G_f^\circ(\text{isooctane}) = -353.2 \text{ kJ/mol}$,
- $\Delta G_f^\circ(\text{CO}_2) = -394.4 \text{ kJ/mol}$, and
- $\Delta G_f^\circ(\text{H}_2\text{O}) = -237.1 \text{ kJ/mol}$.

Is the reaction spontaneous as written?

Given: balanced chemical equation and values of ΔG_f° for isooctane, CO_2 , and H_2O

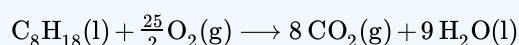
Asked for: spontaneity of reaction as written

Strategy:

Use the “products minus reactants” rule to obtain $\Delta G_{\text{rxn}}^\circ$, remembering that ΔG_f° for an element in its standard state is zero. From the calculated value, determine whether the reaction is spontaneous as written.

Solution

The balanced chemical equation for the reaction is as follows:



We are given ΔG_f° values for all the products and reactants except $\text{O}_2(\text{g})$. Because oxygen gas is an element in its standard state, $\Delta G_f^\circ(\text{O}_2)$ is zero. Using the “products minus reactants” rule,

$$\begin{aligned} \Delta G^\circ &= [8\Delta G_f^\circ(\text{CO}_2) + 9\Delta G_f^\circ(\text{H}_2\text{O})] - \left[1\Delta G_f^\circ(\text{C}_8\text{H}_{18}) + \frac{25}{2}\Delta G_f^\circ(\text{O}_2)\right] \\ &= [(8 \text{ mol})(-394.4 \text{ kJ/mol}) + (9 \text{ mol})(-237.1 \text{ kJ/mol})] \\ &\quad - \left[(1 \text{ mol})(-353.2 \text{ kJ/mol}) + \left(\frac{25}{2} \text{ mol}\right)(0 \text{ kJ/mol})\right] \\ &= -4935.9 \text{ kJ (per mol of C}_8\text{H}_{18}) \end{aligned}$$

Because ΔG° is a large negative number, there is a strong tendency for the spontaneous formation of products from reactants (though not necessarily at a rapid rate). Also notice that the magnitude of ΔG° is largely determined by the ΔG°_f of the stable products: water and carbon dioxide.

? Exercise 13.7.2

Calculate ΔG° for the reaction of benzene with hydrogen gas to give cyclohexane using the following data

- $\Delta G^\circ_f(\text{benzene}) = 124.5 \text{ kJ/mol}$
- $\Delta G^\circ_f(\text{cyclohexane}) = 217.3 \text{ kJ/mol}$.

Is the reaction spontaneous as written?

Answer

92.8 kJ; no

Calculated values of ΔG° are extremely useful in predicting whether a reaction will occur spontaneously if the reactants and products are mixed under standard conditions. We should note, however, that very few reactions are actually carried out under standard conditions, and calculated values of ΔG° may not tell us whether a given reaction will occur spontaneously under nonstandard conditions. What determines whether a reaction will occur spontaneously is the free-energy change (ΔG) under the actual experimental conditions, which are usually different from ΔG° . If the ΔH and $T\Delta S$ terms for a reaction have the same sign, for example, then it may be possible to reverse the sign of ΔG by changing the temperature, thereby converting a reaction that is not thermodynamically spontaneous, having $K_{eq} < 1$, to one that is, having a $K_{eq} > 1$, or vice versa. Because ΔH and ΔS usually do not vary greatly with temperature in the absence of a phase change, we can use tabulated values of ΔH° and ΔS° to calculate ΔG° at various temperatures, as long as no phase change occurs over the temperature range being considered.

In the absence of a phase change, neither ΔH nor ΔS vary greatly with temperature.

✓ Example 13.7.3

Calculate (a) ΔG° and (b) $\Delta G_{300^\circ\text{C}}$ for the reaction $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$, assuming that ΔH and ΔS do not change between 25°C and 300°C . Use these data:

- $S^\circ(\text{N}_2) = 191.6 \text{ J/(mol}\cdot\text{K)}$,
- $S^\circ(\text{H}_2) = 130.7 \text{ J/(mol}\cdot\text{K)}$,
- $S^\circ(\text{NH}_3) = 192.8 \text{ J/(mol}\cdot\text{K)}$, and
- $\Delta H^\circ_f(\text{NH}_3) = -45.9 \text{ kJ/mol}$.

Given: balanced chemical equation, temperatures, S° values, and ΔH°_f for NH_3

Asked for: ΔG° and ΔG at 300°C

Strategy:

- Convert each temperature to kelvins. Then calculate ΔS° for the reaction. Calculate ΔH° for the reaction, recalling that ΔH°_f for any element in its standard state is zero.
- Substitute the appropriate values into Equation 13.7.14 to obtain ΔG° for the reaction.
- Assuming that ΔH and ΔS are independent of temperature, substitute values into Equation 13.7.7 to obtain ΔG for the reaction at 300°C .

Solution

A To calculate ΔG° for the reaction using Equation 13.7.14, we must know the temperature as well as the values of ΔS° and ΔH° . At standard conditions, the temperature is 25°C , or 298 K . We can calculate ΔS° for the reaction from the absolute molar entropy values given for the reactants and the products using the “products minus reactants” rule:

$$\begin{aligned}\Delta S_{\text{rxn}}^{\circ} &= 2S^{\circ}(\text{NH}_3) - [S^{\circ}(\text{N}_2) + 3S^{\circ}(\text{H}_2)] \\ &= [2 \text{ mol NH}_3 \times 192.8 \text{ J}/(\text{mol} \cdot \text{K})] \\ &\quad - \{[1 \text{ mol N}_2 \times 191.6 \text{ J}/(\text{mol} \cdot \text{K})] + [3 \text{ mol H}_2 \times 130.7 \text{ J}/(\text{mol} \cdot \text{K})]\} \\ &= -198.1 \text{ J/K (per mole of N}_2\text{)}\end{aligned}$$

We can also calculate ΔH° for the reaction using the “products minus reactants” rule. The value of $\Delta H^{\circ}_f(\text{NH}_3)$ is given, and ΔH°_f is zero for both N_2 and H_2 :

$$\begin{aligned}\Delta H_{\text{rxn}}^{\circ} &= 2\Delta H^{\circ}_f(\text{NH}_3) - [\Delta H^{\circ}_f(\text{N}_2) + 3\Delta H^{\circ}_f(\text{H}_2)] \\ &= [2 \times (-45.9 \text{ kJ/mol})] - [(1 \times 0 \text{ kJ/mol}) + (3 \times 0 \text{ kJ/mol})] \\ &= -91.8 \text{ kJ (per mole of N}_2\text{)}\end{aligned}$$

B Inserting the appropriate values into Equation 13.7.14

$$\begin{aligned}\Delta G_{\text{rxn}}^{\circ} &= \Delta H^{\circ} - T\Delta S^{\circ} \\ &= (-91.8 \text{ kJ}) - (298 \text{ K})(-198.1 \text{ J/K})(1 \text{ kJ}/1000 \text{ J}) \\ &= -32.7 \text{ kJ (per mole of N}_2\text{)}\end{aligned}$$

C To calculate ΔG for this reaction at 300°C , we assume that ΔH and ΔS are independent of temperature (i.e., $\Delta H_{300^{\circ}\text{C}} = H^{\circ}$ and $\Delta S_{300^{\circ}\text{C}} = \Delta S^{\circ}$) and insert the appropriate temperature (573 K) into Equation 13.7.7:

$$\begin{aligned}\Delta G_{300^{\circ}\text{C}} &= \Delta H_{300^{\circ}\text{C}} - (573 \text{ K})(\Delta S_{300^{\circ}\text{C}}) \\ &= \Delta H^{\circ} - (573 \text{ K})\Delta S^{\circ} \\ &= (-91.8 \text{ kJ}) - (573 \text{ K})(-198.1 \text{ J/K})(1 \text{ kJ}/1000 \text{ J}) \\ &= 21.7 \text{ kJ (per mole of N}_2\text{)}\end{aligned}$$

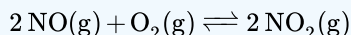
In this example, changing the temperature has a major effect on the thermodynamic spontaneity of the reaction. Under standard conditions, the reaction of nitrogen and hydrogen gas to produce ammonia is thermodynamically spontaneous, but in practice, it is too slow to be useful industrially. Increasing the temperature in an attempt to make this reaction occur more rapidly also changes the thermodynamics by causing the $-T\Delta S^{\circ}$ term to dominate, and the reaction is no longer spontaneous at high temperatures; that is, its K_{eq} is less than one. This is a classic example of the conflict encountered in real systems between thermodynamics and kinetics, which is often unavoidable.

? Exercise 13.7.3

Calculate

- ΔG° and
- $\Delta G_{750^{\circ}\text{C}}$

for the following reaction



which is important in the formation of urban smog. Assume that ΔH and ΔS do not change between 25.0°C and 750°C and use these data:

- $S^{\circ}(\text{NO}) = 210.8 \text{ J}/(\text{mol} \cdot \text{K})$,
- $S^{\circ}(\text{O}_2) = 205.2 \text{ J}/(\text{mol} \cdot \text{K})$,
- $S^{\circ}(\text{NO}_2) = 240.1 \text{ J}/(\text{mol} \cdot \text{K})$,
- $\Delta H^{\circ}_f(\text{NO}_2) = 33.2 \text{ kJ/mol}$, and
- $\Delta H^{\circ}_f(\text{NO}) = 91.3 \text{ kJ/mol}$.

Answer a

$-72.5 \text{ kJ/mol of O}_2$

Answer b

33.8 kJ/mol of O_2

The effect of temperature on the spontaneity of a reaction, which is an important factor in the design of an experiment or an industrial process, depends on the sign and magnitude of both ΔH° and ΔS° . The temperature at which a given reaction is at equilibrium can be calculated by setting $\Delta G^\circ = 0$ in Equation 13.7.14 as illustrated in Example 13.7.4

✓ Example 13.7.4

As you saw in Example 13.7.3 the reaction of nitrogen and hydrogen gas to produce ammonia is one in which ΔH° and ΔS° are both negative. Such reactions are predicted to be thermodynamically spontaneous at low temperatures but nonspontaneous at high temperatures. Use the data in Example 13.7.3 to calculate the temperature at which this reaction changes from spontaneous to nonspontaneous, assuming that ΔH° and ΔS° are independent of temperature.

Given: ΔH° and ΔS°

Asked for: temperature at which reaction changes from spontaneous to nonspontaneous

Strategy:

Set ΔG° equal to zero in Equation 13.7.14 and solve for T, the temperature at which the reaction becomes nonspontaneous.

Solution

In Example 13.7.3 we calculated that ΔH° is -91.8 kJ/mol of N_2 and ΔS° is -198.1 J/K per mole of N_2 , corresponding to $\Delta G^\circ = -32.7$ kJ/mol of N_2 at 25°C . Thus the reaction is indeed spontaneous at low temperatures, as expected based on the signs of ΔH° and ΔS° . The temperature at which the reaction becomes nonspontaneous is found by setting ΔG° equal to zero and rearranging Equation 13.7.14 to solve for T:

$$\begin{aligned}\Delta G^\circ &= \Delta H^\circ - T\Delta S^\circ = 0 \\ \Delta H^\circ &= T\Delta S^\circ \\ T &= \frac{\Delta H^\circ}{\Delta S^\circ} = \frac{(-91.8 \text{ kJ})(1000 \text{ J/kJ})}{-198.1 \text{ J/K}} = 463 \text{ K}\end{aligned}$$

This is a case in which a chemical engineer is severely limited by thermodynamics. Any attempt to increase the rate of reaction of nitrogen with hydrogen by increasing the temperature will cause reactants to be favored over products above 463 K.

? Exercise 13.7.4

As you found in the exercise in Example 13.7.3 ΔH° and ΔS° are both negative for the reaction of nitric oxide and oxygen to form nitrogen dioxide. Use those data to calculate the temperature at which this reaction changes from spontaneous to nonspontaneous.

Answer

792.6 K

Summary

- The change in Gibbs free energy, which is based solely on changes in state functions, is the criterion for predicting the spontaneity of a reaction.
- Free-energy change

$$\Delta G = \Delta H - T\Delta S$$

- Standard free-energy change

$$\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ$$

We can predict whether a reaction will occur spontaneously by combining the entropy, enthalpy, and temperature of a system in a new state function called Gibbs free energy (G). The change in free energy (ΔG) is the difference between the heat released during a process and the heat released for the same process occurring in a reversible manner. If a system is at equilibrium, $\Delta G = 0$. If the process is spontaneous, $\Delta G < 0$. If the process is not spontaneous as written but is spontaneous in the reverse direction, $\Delta G > 0$. At constant temperature and pressure, ΔG is equal to the maximum amount of work a system can perform on its surroundings while undergoing a spontaneous change. The standard free-energy change (ΔG°) is the change in free energy when one substance or a set of substances in their standard states is converted to one or more other substances, also in their standard states. The standard free energy of formation (ΔG°_f), is the change in free energy that occurs when 1 mol of a substance in its standard state is formed from the component elements in their standard states. Tabulated values of standard free energies of formation are used to calculate ΔG° for a reaction.

Contributors and Attributions

- Stephen Lower, Professor Emeritus ([Simon Fraser U.](#)) [Chem1 Virtual Textbook](#)
- Mike Blaber ([Florida State University](#))

13.7: The Gibbs Free Energy is shared under a [CC BY-NC-SA 4.0](#) license and was authored, remixed, and/or curated by LibreTexts.