

## 19.6: Gibbs Energy

### Learning Objectives

- To understand the relationship between Gibbs free energy and work.

One of the major goals of chemical thermodynamics is to establish criteria for predicting whether a particular reaction or process will occur spontaneously. We have developed one such criterion, the change in entropy of the universe: if  $\Delta S_{\text{univ}} > 0$  for a process or a reaction, then the process will occur spontaneously as written. Conversely, if  $\Delta S_{\text{univ}} < 0$ , a process cannot occur spontaneously; if  $\Delta S_{\text{univ}} = 0$ , the system is at equilibrium. The sign of  $\Delta S_{\text{univ}}$  is a universally applicable and infallible indicator of the spontaneity of a reaction. Unfortunately, using  $\Delta S_{\text{univ}}$  requires that we calculate  $\Delta S$  for both a system and its surroundings. This is not particularly useful for two reasons: we are normally much more interested in the system than in the surroundings, and it is difficult to make quantitative measurements of the surroundings (i.e., the rest of the universe). A criterion of spontaneity that is based solely on the state functions of a system would be much more convenient and is provided by a new state function: the Gibbs free energy.

### Gibbs Free Energy and the Direction of Spontaneous Reactions

The Gibbs free energy ( $G$ ), often called simply free energy, was named in honor of J. Willard Gibbs (1838–1903), an American physicist who first developed the concept. It is defined in terms of three other state functions with which you are already familiar: enthalpy, temperature, and entropy:

$$G = H - TS \quad (19.6.1)$$

Because it is a combination of state functions,  $G$  is also a state function.

#### J. Willard Gibbs (1839–1903)

Born in Connecticut, Josiah Willard Gibbs attended Yale, as did his father, a professor of sacred literature at Yale, who was involved in the Amistad trial. In 1863, Gibbs was awarded the first engineering doctorate granted in the United States. He was appointed professor of mathematical physics at Yale in 1871, the first such professorship in the United States. His series of papers entitled “On the Equilibrium of Heterogeneous Substances” was the foundation of the field of physical chemistry and is considered one of the great achievements of the 19th century. Gibbs, whose work was translated into French by Le Chatelier, lived with his sister and brother-in-law until his death in 1903, shortly before the inauguration of the Nobel Prizes.

The criterion for predicting spontaneity is based on ( $\Delta G$ ), the change in  $G$ , at constant temperature and pressure. Although very few chemical reactions actually occur under conditions of constant temperature and pressure, most systems can be brought back to the initial temperature and pressure without significantly affecting the value of thermodynamic state functions such as  $G$ . At constant temperature and pressure,

$$\Delta G = \Delta H - T\Delta S \quad (19.6.2)$$

where all thermodynamic quantities are those of the system. Recall that at constant pressure,  $\Delta H = q$ , whether a process is reversible or irreversible, and  $T\Delta S = q_{\text{rev}}$ . Using these expressions, we can reduce Equation 19.6.2 to  $\Delta G = q - q_{\text{rev}}$ . Thus  $\Delta G$  is the difference between the heat released during a process (via a reversible or an irreversible path) and the heat released for the same process occurring in a reversible manner. Under the special condition in which a process occurs reversibly,  $q = q_{\text{rev}}$  and  $\Delta G = 0$ . As we shall soon see, if  $\Delta G$  is zero, the system is at equilibrium, and there will be no net change.

What about processes for which  $\Delta G \neq 0$ ? To understand how the sign of  $\Delta G$  for a system determines the direction in which change is spontaneous, we can rewrite the relationship between  $\Delta S$  and  $q_{\text{rev}}$ , discussed earlier.

$$\Delta S = \frac{q_{\text{rev}}}{T}$$

with the definition of  $\Delta H$  in terms of  $q_{\text{rev}}$

$$q_{\text{rev}} = \Delta H$$

to obtain

$$\Delta S_{\text{surr}} = -\frac{\Delta H_{\text{sys}}}{T} \quad (19.6.3)$$

Thus the entropy change of the surroundings is related to the enthalpy change of the system. We have stated that for a spontaneous reaction,  $\Delta S_{\text{univ}} > 0$ , so substituting we obtain

$$\Delta S_{\text{univ}} = \Delta S_{\text{sys}} + \Delta S_{\text{surr}} > 0 \quad (19.6.4)$$

$$= \Delta S_{\text{sys}} - \frac{\Delta H_{\text{sys}}}{T} > 0 \quad (19.6.5)$$

Multiplying both sides of the inequality by  $-T$  reverses the sign of the inequality; rearranging,

$$\Delta H_{\text{sys}} - T\Delta S_{\text{sys}} < 0$$

which is equal to  $\Delta G$  (Equation 19.6.2). We can therefore see that for a spontaneous process,  $\Delta G < 0$ .

The relationship between the entropy change of the surroundings and the heat gained or lost by the system provides the key connection between the thermodynamic properties of the system and the change in entropy of the universe. The relationship shown in Equation 19.6.2 allows us to predict spontaneity by focusing exclusively on the thermodynamic properties and temperature of the system. We predict that highly exothermic processes ( $\Delta H \ll 0$ ) that increase the disorder of a system ( $\Delta S_{\text{sys}} \gg 0$ ) would therefore occur spontaneously. An example of such a process is the decomposition of ammonium nitrate fertilizer. Ammonium nitrate was also used to destroy the Murrah Federal Building in Oklahoma City, Oklahoma, in 1995. For a system at constant temperature and pressure, we can summarize the following results:

- If  $\Delta G < 0$ , the process occurs spontaneously.
- If  $\Delta G = 0$ , the system is at equilibrium.
- If  $\Delta G > 0$ , the process is not spontaneous as written but occurs spontaneously in the reverse direction.

To further understand how the various components of  $\Delta G$  dictate whether a process occurs spontaneously, we now look at a simple and familiar physical change: the conversion of liquid water to water vapor. If this process is carried out at 1 atm and the normal boiling point of 100.00°C (373.15 K), we can calculate  $\Delta G$  from the experimentally measured value of  $\Delta H_{\text{vap}}$  (40.657 kJ/mol). For vaporizing 1 mol of water,  $\Delta H = 40,657 \text{ J}$ , so the process is highly endothermic. From the definition of  $\Delta S$  (Equation 19.6.3), we know that for 1 mol of water,

$$\begin{aligned} \Delta S_{\text{vap}} &= \frac{\Delta H_{\text{vap}}}{T_{\text{b}}} \\ &= \frac{40,657 \text{ J}}{373.15 \text{ K}} \\ &= 108.96 \text{ J/K} \end{aligned}$$

Hence there is an increase in the disorder of the system. At the normal boiling point of water,

$$\begin{aligned} \Delta G_{100^\circ\text{C}} &= \Delta H_{100^\circ\text{C}} - T\Delta S_{100^\circ\text{C}} \\ &= 40,657 \text{ J} - [(373.15 \text{ K})(108.96 \text{ J/K})] \\ &= 0 \text{ J} \end{aligned}$$

The energy required for vaporization offsets the increase in disorder of the system. Thus  $\Delta G = 0$ , and the liquid and vapor are in equilibrium, as is true of any liquid at its boiling point under standard conditions.

Now suppose we were to superheat 1 mol of liquid water to 110°C. The value of  $\Delta G$  for the vaporization of 1 mol of water at 110°C, assuming that  $\Delta H$  and  $\Delta S$  do not change significantly with temperature, becomes

$$\begin{aligned} \Delta G_{110^\circ\text{C}} &= \Delta H - T\Delta S \\ &= 40,657 \text{ J} - [(383.15 \text{ K})(108.96 \text{ J/K})] \\ &= -1091 \text{ J} \end{aligned}$$

At 110°C,  $\Delta G < 0$ , and vaporization is predicted to occur spontaneously and irreversibly.

We can also calculate  $\Delta G$  for the vaporization of 1 mol of water at a temperature below its normal boiling point—for example, 90°C—making the same assumptions:

$$\begin{aligned}\Delta G_{90^\circ\text{C}} &= \Delta H - T\Delta S \\ &= 40,657 \text{ J} - [(363.15 \text{ K})(108.96 \text{ J/K})] \\ &= 1088 \text{ J}\end{aligned}$$

At 90°C,  $\Delta G > 0$ , and water does not spontaneously convert to water vapor. When using all the digits in the calculator display in carrying out our calculations,  $\Delta G_{110^\circ\text{C}} = 1090 \text{ J} = -\Delta G_{90^\circ\text{C}}$ , as we would predict.

#### 📌 Relating Enthalpy and Entropy changes under Equilibrium Conditions

$\Delta G = 0$  only if  $\Delta H = T\Delta S$ .

We can also calculate the temperature at which liquid water is in equilibrium with water vapor. Inserting the values of  $\Delta H$  and  $\Delta S$  into the definition of  $\Delta G$  (Equation 19.6.2), setting  $\Delta G = 0$ , and solving for  $T$ ,

$$\begin{aligned}0 \text{ J} &= 40,657 \text{ J} - T(108.96 \text{ J/K}) \\ T &= 373.15 \text{ K}\end{aligned}$$

Thus  $\Delta G = 0$  at  $T = 373.15 \text{ K}$  and 1 atm, which indicates that liquid water and water vapor are in equilibrium; this temperature is called the normal boiling point of water. At temperatures greater than 373.15 K,  $\Delta G$  is negative, and water evaporates spontaneously and irreversibly. Below 373.15 K,  $\Delta G$  is positive, and water does not evaporate spontaneously. Instead, water vapor at a temperature less than 373.15 K and 1 atm will spontaneously and irreversibly condense to liquid water. Figure 19.6.1 shows how the  $\Delta H$  and  $T\Delta S$  terms vary with temperature for the vaporization of water. When the two lines cross,  $\Delta G = 0$ , and  $\Delta H = T\Delta S$ .

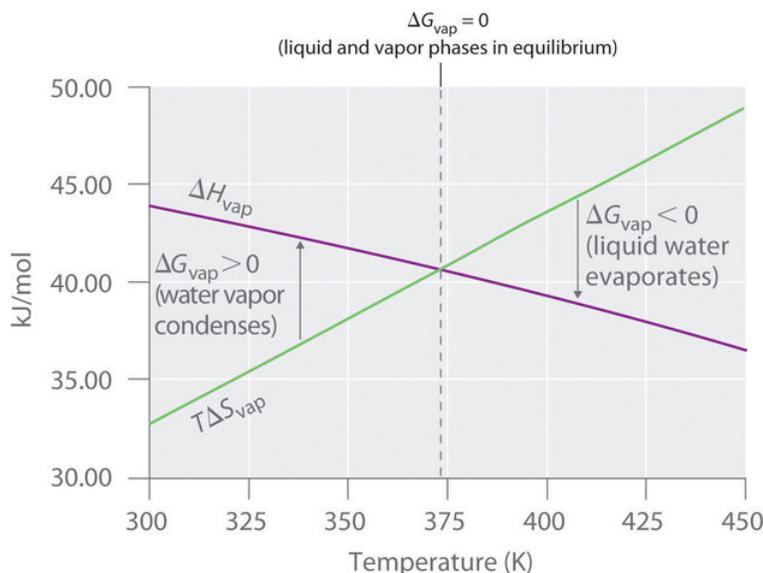


Figure 19.6.1: Temperature Dependence of  $\Delta H$  and  $T\Delta S$  for the Vaporization of Water. Both  $\Delta H$  and  $T\Delta S$  are temperature dependent, but the lines have opposite slopes and cross at 373.15 K at 1 atm, where  $\Delta H = T\Delta S$ . Because  $\Delta G = \Delta H - T\Delta S$ , at this temperature  $\Delta G = 0$ , indicating that the liquid and vapor phases are in equilibrium. The normal boiling point of water is therefore 373.15 K. Above the normal boiling point, the  $T\Delta S$  term is greater than  $\Delta H$ , making  $\Delta G < 0$ ; hence, liquid water evaporates spontaneously. Below the normal boiling point, the  $\Delta H$  term is greater than  $T\Delta S$ , making  $\Delta G > 0$ . Thus liquid water does not evaporate spontaneously, but water vapor spontaneously condenses to liquid.

Graph of kilojoule per mole against temperature. The purple line is the  $\Delta H$  vaporization. the green line is the  $T\Delta S$  vaporization.

A similar situation arises in the conversion of liquid egg white to a solid when an egg is boiled. The major component of egg white is a protein called albumin, which is held in a compact, ordered structure by a large number of hydrogen bonds. Breaking them requires an input of energy ( $\Delta H > 0$ ), which converts the albumin to a highly disordered structure in which the molecules aggregate as a disorganized solid ( $\Delta S > 0$ ). At temperatures greater than 373 K, the  $T\Delta S$  term dominates, and  $\Delta G < 0$ , so the conversion of a raw egg to a hard-boiled egg is an irreversible and spontaneous process above 373 K.



The Definition of Gibbs Free Energy: [The Definition of Gibbs Free Energy \(opens in new window\)](#) [youtu.be]

## The Relationship between $\Delta G$ and Work

In the previous subsection, we learned that the value of  $\Delta G$  allows us to predict the spontaneity of a physical or a chemical change. In addition, the magnitude of  $\Delta G$  for a process provides other important information. The change in free energy ( $\Delta G$ ) is equal to the maximum amount of work that a system can perform on the surroundings while undergoing a spontaneous change (at constant temperature and pressure):  $\Delta G = w_{\text{max}}$ . To see why this is true, let's look again at the relationships among free energy, enthalpy, and entropy expressed in Equation 19.6.2 We can rearrange this equation as follows:

$$\Delta H = \Delta G + T\Delta S \quad (19.6.6)$$

This equation tells us that when energy is released during an exothermic process ( $\Delta H < 0$ ), such as during the combustion of a fuel, some of that energy can be used to do work ( $\Delta G < 0$ ), while some is used to increase the entropy of the universe ( $T\Delta S > 0$ ). Only if the process occurs infinitely slowly in a perfectly reversible manner will the entropy of the universe be unchanged. (For more information on entropy and reversibility, see the previous section). Because no real system is perfectly reversible, the entropy of the universe increases during all processes that produce energy. As a result, no process that uses stored energy can ever be 100% efficient; that is,  $\Delta H$  will never equal  $\Delta G$  because  $\Delta S$  has a positive value.

One of the major challenges facing engineers is to maximize the efficiency of converting stored energy to useful work or converting one form of energy to another. As indicated in Table 19.6.1, the efficiencies of various energy-converting devices vary widely. For example, an internal combustion engine typically uses only 25%–30% of the energy stored in the hydrocarbon fuel to perform work; the rest of the stored energy is released in an unusable form as heat. In contrast, gas–electric hybrid engines, now used in several models of automobiles, deliver approximately 50% greater fuel efficiency. A large electrical generator is highly efficient (approximately 99%) in converting mechanical to electrical energy, but a typical incandescent light bulb is one of the least efficient devices known (only approximately 5% of the electrical energy is converted to light). In contrast, a mammalian liver cell is a relatively efficient machine and can use fuels such as glucose with an efficiency of 30%–50%.

Table 19.6.1: Approximate Thermodynamic Efficiencies of Various Devices

Device	Energy Conversion	Approximate Efficiency (%)
large electrical generator	mechanical → electrical	99
chemical battery	chemical → electrical	90
home furnace	chemical → heat	65
small electric tool	electrical → mechanical	60
space shuttle engine	chemical → mechanical	50
mammalian liver cell	chemical → chemical	30–50
spinach leaf cell	light → chemical	30

Device	Energy Conversion	Approximate Efficiency (%)
internal combustion engine	chemical → mechanical	25–30
fluorescent light	electrical → light	20
solar cell	light → electricity	10–20
incandescent light bulb	electricity → light	5
yeast cell	chemical → chemical	2–4

## Standard Free-Energy Change

We have seen that there is no way to measure absolute enthalpies, although we can measure changes in enthalpy ( $\Delta H$ ) during a chemical reaction. Because enthalpy is one of the components of Gibbs free energy, we are consequently unable to measure absolute free energies; we can measure only changes in free energy. The standard free-energy change ( $\Delta G^\circ$ ) is the change in free energy when one substance or a set of substances in their standard states is converted to one or more other substances, also in their standard states. The standard free-energy change can be calculated from the definition of free energy, if the standard enthalpy and entropy changes are known, using Equation 19.6.7:

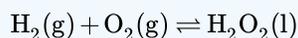
$$\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ \quad (19.6.7)$$

If  $\Delta S^\circ$  and  $\Delta H^\circ$  for a reaction have the same sign, then the sign of  $\Delta G^\circ$  depends on the relative magnitudes of the  $\Delta H^\circ$  and  $T\Delta S^\circ$  terms. It is important to recognize that a positive value of  $\Delta G^\circ$  for a reaction does not mean that no products will form if the reactants in their standard states are mixed; it means only that at equilibrium the concentrations of the products will be less than the concentrations of the reactants.

A positive  $\Delta G^\circ$  means that the equilibrium constant is less than 1.

### ✓ Example 19.6.1

Calculate the standard free-energy change ( $\Delta G^\circ$ ) at 25°C for the reaction



At 25°C, the standard enthalpy change ( $\Delta H^\circ$ ) is  $-187.78 \text{ kJ/mol}$ , and the absolute entropies of the products and reactants are:

- $S^\circ(\text{H}_2\text{O}_2) = 109.6 \text{ J/(mol}\cdot\text{K)}$ ,
- $S^\circ(\text{O}_2) = 205.2 \text{ J/(mol}\cdot\text{K)}$ , and
- $S^\circ(\text{H}_2) = 130.7 \text{ J/(mol}\cdot\text{K)}$ .

Is the reaction spontaneous as written?

**Given:** balanced chemical equation,  $\Delta H^\circ$  and  $S^\circ$  for reactants and products

**Asked for:** spontaneity of reaction as written

**Strategy:**

- Calculate  $\Delta S^\circ$  from the absolute molar entropy values given.
- Use Equation 19.6.7, the calculated value of  $\Delta S^\circ$ , and other data given to calculate  $\Delta G^\circ$  for the reaction. Use the value of  $\Delta G^\circ$  to determine whether the reaction is spontaneous as written.

**Solution**

A To calculate  $\Delta G^\circ$  for the reaction, we need to know  $\Delta H^\circ$ ,  $\Delta S^\circ$ , and  $T$ . We are given  $\Delta H^\circ$ , and we know that  $T = 298.15 \text{ K}$ . We can calculate  $\Delta S^\circ$  from the absolute molar entropy values provided using the “products minus reactants” rule:

$$\begin{aligned}\Delta S^\circ &= S^\circ(\text{H}_2\text{O}_2) - [S^\circ(\text{O}_2) + S^\circ(\text{H}_2)] \\ &= [1 \text{ mol H}_2\text{O}_2 \times 109.6 \text{ J}/(\text{mol} \cdot \text{K})] \\ &\quad - \{[1 \text{ mol H}_2 \times 130.7 \text{ J}/(\text{mol} \cdot \text{K})] + [1 \text{ mol O}_2 \times 205.2 \text{ J}/(\text{mol} \cdot \text{K})]\} \\ &= -226.3 \text{ J/K (per mole of H}_2\text{O}_2)\end{aligned}$$

As we might expect for a reaction in which 2 mol of gas is converted to 1 mol of a much more ordered liquid,  $\Delta S^\circ$  is very negative for this reaction.

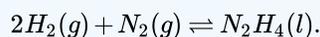
B Substituting the appropriate quantities into Equation 19.6.7,

$$\begin{aligned}\Delta G^\circ &= \Delta H^\circ - T\Delta S^\circ \\ &= -187.78 \text{ kJ/mol} - (298.15 \text{ K})[-226.3 \text{ J}/(\text{mol} \cdot \text{K}) \times 1 \text{ kJ}/1000 \text{ J}] \\ &= -187.78 \text{ kJ/mol} + 67.47 \text{ kJ/mol} \\ &= -120.31 \text{ kJ/mol}\end{aligned}$$

The negative value of  $\Delta G^\circ$  indicates that the reaction is spontaneous as written. Because  $\Delta S^\circ$  and  $\Delta H^\circ$  for this reaction have the same sign, the sign of  $\Delta G^\circ$  depends on the relative magnitudes of the  $\Delta H^\circ$  and  $T\Delta S^\circ$  terms. In this particular case, the enthalpy term dominates, indicating that the strength of the bonds formed in the product more than compensates for the unfavorable  $\Delta S^\circ$  term and for the energy needed to break bonds in the reactants.

### ? Exercise 19.6.1

Calculate the standard free-energy change ( $\Delta G^\circ$ ) at 25°C for the reaction



Is the reaction spontaneous as written at 25°C?

#### Hint

At 25°C, the standard enthalpy change ( $\Delta H^\circ$ ) is 50.6 kJ/mol, and the absolute entropies of the products and reactants are

- $S^\circ(\text{N}_2\text{H}_4) = 121.2 \text{ J}/(\text{mol} \cdot \text{K})$ ,
- $S^\circ(\text{N}_2) = 191.6 \text{ J}/(\text{mol} \cdot \text{K})$ , and
- $S^\circ(\text{H}_2) = 130.7 \text{ J}/(\text{mol} \cdot \text{K})$ .

#### Answer

149.5 kJ/mol

no, not spontaneous

[Video Solution](#)



Determining if a Reaction is Spontaneous: [Determining if a Reaction is Spontaneous](#) (opens in new window) [youtu.be] [\(opens in new window\)](#)

Tabulated values of standard free energies of formation allow chemists to calculate the values of  $\Delta G^\circ$  for a wide variety of chemical reactions rather than having to measure them in the laboratory. The standard free energy of formation ( $\Delta G_f^\circ$ ) of a compound is the change in free energy that occurs when 1 mol of a substance in its standard state is formed from the component elements in their standard states. By definition, the standard free energy of formation of an element in its standard state is zero at 298.15 K. One mole of  $\text{Cl}_2$  gas at 298.15 K, for example, has  $\Delta G_f^\circ = 0$ . The standard free energy of formation of a compound can be calculated from the standard enthalpy of formation ( $\Delta H_f^\circ$ ) and the standard entropy of formation ( $\Delta S_f^\circ$ ) using the definition of free energy:

$$\Delta G_f^\circ = \Delta H_f^\circ - T\Delta S_f^\circ \quad (19.6.8)$$

Using standard free energies of formation to calculate the standard free energy of a reaction is analogous to calculating standard enthalpy changes from standard enthalpies of formation using the familiar “products minus reactants” rule:

$$\Delta G_{rxn}^\circ = \sum m\Delta G_f^\circ(\text{products}) - \sum n\Delta G_f^\circ(\text{reactants}) \quad (19.6.9)$$

where  $m$  and  $n$  are the stoichiometric coefficients of each product and reactant in the balanced chemical equation. A very large negative  $\Delta G^\circ$  indicates a strong tendency for products to form spontaneously from reactants; it does not, however, necessarily indicate that the reaction will occur rapidly. To make this determination, we need to evaluate the kinetics of the reaction.

#### The “Products minus Reactants” Rule

The  $\Delta G^\circ$  of a reaction can be calculated from tabulated  $\Delta G_f^\circ$  values ([Table T1](#)) using the “products minus reactants” rule.

#### Example 19.6.2

Calculate  $\Delta G^\circ$  for the reaction of isooctane with oxygen gas to give carbon dioxide and water (described in Example 7). Use the following data:

- $\Delta G_f^\circ(\text{isooctane}) = -353.2 \text{ kJ/mol}$ ,
- $\Delta G_f^\circ(\text{CO}_2) = -394.4 \text{ kJ/mol}$ , and
- $\Delta G_f^\circ(\text{H}_2\text{O}) = -237.1 \text{ kJ/mol}$ . Is the reaction spontaneous as written?

**Given:** balanced chemical equation and values of  $\Delta G_f^\circ$  for isooctane,  $\text{CO}_2$ , and  $\text{H}_2\text{O}$

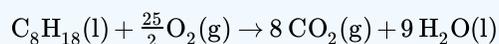
**Asked for:** spontaneity of reaction as written

**Strategy:**

Use the “products minus reactants” rule to obtain  $\Delta G_{rxn}^\circ$ , remembering that  $\Delta G_f^\circ$  for an element in its standard state is zero. From the calculated value, determine whether the reaction is spontaneous as written.

**Solution**

The balanced chemical equation for the reaction is as follows:



We are given  $\Delta G^\circ_f$  values for all the products and reactants except  $\text{O}_2(\text{g})$ . Because oxygen gas is an element in its standard state,  $\Delta G^\circ_f(\text{O}_2)$  is zero. Using the “products minus reactants” rule,

$$\begin{aligned}\Delta G^\circ &= [8\Delta G^\circ_f(\text{CO}_2) + 9\Delta G^\circ_f(\text{H}_2\text{O})] - \left[1\Delta G^\circ_f(\text{C}_8\text{H}_{18}) + \frac{25}{2}\Delta G^\circ_f(\text{O}_2)\right] \\ &= [(8 \text{ mol})(-394.4 \text{ kJ/mol}) + (9 \text{ mol})(-237.1 \text{ kJ/mol})] \\ &\quad - \left[(1 \text{ mol})(-353.2 \text{ kJ/mol}) + \left(\frac{25}{2} \text{ mol}\right)(0 \text{ kJ/mol})\right] \\ &= -4935.9 \text{ kJ (per mol of C}_8\text{H}_{18})\end{aligned}$$

Because  $\Delta G^\circ$  is a large negative number, there is a strong tendency for the spontaneous formation of products from reactants (though not necessarily at a rapid rate). Also notice that the magnitude of  $\Delta G^\circ$  is largely determined by the  $\Delta G^\circ_f$  of the stable products: water and carbon dioxide.

### ? Exercise 19.6.2

Calculate  $\Delta G^\circ$  for the reaction of benzene with hydrogen gas to give cyclohexane using the following data

- $\Delta G^\circ_f(\text{benzene}) = 124.5 \text{ kJ/mol}$
- $\Delta G^\circ_f(\text{cyclohexane}) = 217.3 \text{ kJ/mol}$ .

Is the reaction spontaneous as written?

#### Answer

92.8 kJ; no

[Video Solution](#)



Calculating Grxn using Gf: [Calculating Grxn using Gf\(opens in new window\)](#) [youtu.be]

Calculated values of  $\Delta G^\circ$  are extremely useful in predicting whether a reaction will occur spontaneously if the reactants and products are mixed under standard conditions. We should note, however, that very few reactions are actually carried out under standard conditions, and calculated values of  $\Delta G^\circ$  may not tell us whether a given reaction will occur spontaneously under nonstandard conditions. What determines whether a reaction will occur spontaneously is the free-energy change ( $\Delta G$ ) under the actual experimental conditions, which are usually different from  $\Delta G^\circ$ . If the  $\Delta H$  and  $T\Delta S$  terms for a reaction have the same sign, for example, then it may be possible to reverse the sign of  $\Delta G$  by changing the temperature, thereby converting a reaction that is not thermodynamically spontaneous, having  $K_{\text{eq}} < 1$ , to one that is, having a  $K_{\text{eq}} > 1$ , or vice versa. Because  $\Delta H$  and  $\Delta S$  usually do

not vary greatly with temperature in the absence of a phase change, we can use tabulated values of  $\Delta H^\circ$  and  $\Delta S^\circ$  to calculate  $\Delta G^\circ$  at various temperatures, as long as no phase change occurs over the temperature range being considered.

In the absence of a phase change, neither  $\Delta H$  nor  $\Delta S$  vary greatly with temperature.

### ✓ Example 19.6.3

Calculate (a)  $\Delta G^\circ$  and (b)  $\Delta G_{300^\circ\text{C}}$  for the reaction  $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$ , assuming that  $\Delta H$  and  $\Delta S$  do not change between  $25^\circ\text{C}$  and  $300^\circ\text{C}$ . Use these data:

- $S^\circ(\text{N}_2) = 191.6 \text{ J}/(\text{mol}\cdot\text{K})$ ,
- $S^\circ(\text{H}_2) = 130.7 \text{ J}/(\text{mol}\cdot\text{K})$ ,
- $S^\circ(\text{NH}_3) = 192.8 \text{ J}/(\text{mol}\cdot\text{K})$ , and
- $\Delta H^\circ_f(\text{NH}_3) = -45.9 \text{ kJ}/\text{mol}$ .

**Given:** balanced chemical equation, temperatures,  $S^\circ$  values, and  $\Delta H^\circ_f$  for  $\text{NH}_3$

**Asked for:**  $\Delta G^\circ$  and  $\Delta G$  at  $300^\circ\text{C}$

**Strategy:**

- Convert each temperature to kelvins. Then calculate  $\Delta S^\circ$  for the reaction. Calculate  $\Delta H^\circ$  for the reaction, recalling that  $\Delta H^\circ_f$  for any element in its standard state is zero.
- Substitute the appropriate values into Equation 19.6.7 to obtain  $\Delta G^\circ$  for the reaction.
- Assuming that  $\Delta H$  and  $\Delta S$  are independent of temperature, substitute values into Equation 19.6.2 to obtain  $\Delta G$  for the reaction at  $300^\circ\text{C}$ .

### Solution

A To calculate  $\Delta G^\circ$  for the reaction using Equation 19.6.7, we must know the temperature as well as the values of  $\Delta S^\circ$  and  $\Delta H^\circ$ . At standard conditions, the temperature is  $25^\circ\text{C}$ , or  $298 \text{ K}$ . We can calculate  $\Delta S^\circ$  for the reaction from the absolute molar entropy values given for the reactants and the products using the “products minus reactants” rule:

$$\begin{aligned}\Delta S^\circ_{\text{rxn}} &= 2S^\circ(\text{NH}_3) - [S^\circ(\text{N}_2) + 3S^\circ(\text{H}_2)] \\ &= [2 \text{ mol NH}_3 \times 192.8 \text{ J}/(\text{mol}\cdot\text{K})] \\ &\quad - \{[1 \text{ mol N}_2 \times 191.6 \text{ J}/(\text{mol}\cdot\text{K})] + [3 \text{ mol H}_2 \times 130.7 \text{ J}/(\text{mol}\cdot\text{K})]\} \\ &= -198.1 \text{ J}/\text{K} \text{ (per mole of N}_2\text{)}\end{aligned}\tag{19.6.10}$$

We can also calculate  $\Delta H^\circ$  for the reaction using the “products minus reactants” rule. The value of  $\Delta H^\circ_f(\text{NH}_3)$  is given, and  $\Delta H^\circ_f$  is zero for both  $\text{N}_2$  and  $\text{H}_2$ :

$$\begin{aligned}\Delta H^\circ_{\text{rxn}} &= 2\Delta H^\circ_f(\text{NH}_3) - [\Delta H^\circ_f(\text{N}_2) + 3\Delta H^\circ_f(\text{H}_2)] \\ &= [2 \times (-45.9 \text{ kJ}/\text{mol})] - [(1 \times 0 \text{ kJ}/\text{mol}) + (3 \times 0 \text{ kJ}/\text{mol})] \\ &= -91.8 \text{ kJ} \text{ (per mole of N}_2\text{)}\end{aligned}$$

B Inserting the appropriate values into Equation 19.6.7

$$\Delta G^\circ_{\text{rxn}} = \Delta H^\circ - T\Delta S^\circ = (-91.8 \text{ kJ}) - (298 \text{ K})(-198.1 \text{ J}/\text{K})(1 \text{ kJ}/1000 \text{ J}) = -32.7 \text{ kJ} \text{ (per mole of N}_2\text{)}$$

C To calculate  $\Delta G$  for this reaction at  $300^\circ\text{C}$ , we assume that  $\Delta H$  and  $\Delta S$  are independent of temperature (i.e.,  $\Delta H_{300^\circ\text{C}} = \Delta H^\circ$  and  $\Delta S_{300^\circ\text{C}} = \Delta S^\circ$ ) and insert the appropriate temperature ( $573 \text{ K}$ ) into Equation 19.6.2

$$\begin{aligned}\Delta G_{300^\circ\text{C}} &= \Delta H_{300^\circ\text{C}} - (573 \text{ K})(\Delta S_{300^\circ\text{C}}) \\ &= \Delta H^\circ - (573 \text{ K})\Delta S^\circ \\ &= (-91.8 \text{ kJ}) - (573 \text{ K})(-198.1 \text{ J}/\text{K})(1 \text{ kJ}/1000 \text{ J}) \\ &= 21.7 \text{ kJ} \text{ (per mole of N}_2\text{)}\end{aligned}$$

In this example, changing the temperature has a major effect on the thermodynamic spontaneity of the reaction. Under standard conditions, the reaction of nitrogen and hydrogen gas to produce ammonia is thermodynamically spontaneous, but in practice, it is too slow to be useful industrially. Increasing the temperature in an attempt to make this reaction occur more rapidly also

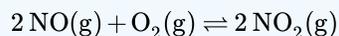
changes the thermodynamics by causing the  $-T\Delta S^\circ$  term to dominate, and the reaction is no longer spontaneous at high temperatures; that is, its  $K_{eq}$  is less than one. This is a classic example of the conflict encountered in real systems between thermodynamics and kinetics, which is often unavoidable.

### ? Exercise 19.6.3

Calculate

- $\Delta G^\circ$  and
- $\Delta G_{750^\circ C}$

for the following reaction



which is important in the formation of urban smog. Assume that  $\Delta H$  and  $\Delta S$  do not change between  $25.0^\circ\text{C}$  and  $750^\circ\text{C}$  and use these data:

- $S^\circ(\text{NO}) = 210.8 \text{ J}/(\text{mol}\cdot\text{K})$ ,
- $S^\circ(\text{O}_2) = 205.2 \text{ J}/(\text{mol}\cdot\text{K})$ ,
- $S^\circ(\text{NO}_2) = 240.1 \text{ J}/(\text{mol}\cdot\text{K})$ ,
- $\Delta H^\circ_f(\text{NO}_2) = 33.2 \text{ kJ}/\text{mol}$ , and
- $\Delta H^\circ_f(\text{NO}) = 91.3 \text{ kJ}/\text{mol}$ .

**Answer a**

$-72.5 \text{ kJ}/\text{mol}$  of  $\text{O}_2$

**Answer b**

$33.8 \text{ kJ}/\text{mol}$  of  $\text{O}_2$

The effect of temperature on the spontaneity of a reaction, which is an important factor in the design of an experiment or an industrial process, depends on the sign and magnitude of both  $\Delta H^\circ$  and  $\Delta S^\circ$ . The temperature at which a given reaction is at equilibrium can be calculated by setting  $\Delta G^\circ = 0$  in Equation 19.6.7, as illustrated in Example 19.6.4

### ✓ Example 19.6.4

As you saw in Example 19.6.3 the reaction of nitrogen and hydrogen gas to produce ammonia is one in which  $\Delta H^\circ$  and  $\Delta S^\circ$  are both negative. Such reactions are predicted to be thermodynamically spontaneous at low temperatures but nonspontaneous at high temperatures. Use the data in Example 9.5.3 to calculate the temperature at which this reaction changes from spontaneous to nonspontaneous, assuming that  $\Delta H^\circ$  and  $\Delta S^\circ$  are independent of temperature.

**Given:**  $\Delta H^\circ$  and  $\Delta S^\circ$

**Asked for:** temperature at which reaction changes from spontaneous to nonspontaneous

**Strategy:**

Set  $\Delta G^\circ$  equal to zero in Equation 19.6.7 and solve for T, the temperature at which the reaction becomes nonspontaneous.

**Solution**

In Example 19.6.3 we calculated that  $\Delta H^\circ$  is  $-91.8 \text{ kJ}/\text{mol}$  of  $\text{N}_2$  and  $\Delta S^\circ$  is  $-198.1 \text{ J}/\text{K}$  per mole of  $\text{N}_2$ , corresponding to  $\Delta G^\circ = -32.7 \text{ kJ}/\text{mol}$  of  $\text{N}_2$  at  $25^\circ\text{C}$ . Thus the reaction is indeed spontaneous at low temperatures, as expected based on the signs of  $\Delta H^\circ$  and  $\Delta S^\circ$ . The temperature at which the reaction becomes nonspontaneous is found by setting  $\Delta G^\circ$  equal to zero and rearranging Equation 19.6.7 to solve for T:

$$\begin{aligned}\Delta G^\circ &= \Delta H^\circ - T\Delta S^\circ = 0 \\ \Delta H^\circ &= T\Delta S^\circ \\ T &= \frac{\Delta H^\circ}{\Delta S^\circ} = \frac{(-91.8 \text{ kJ})(1000 \text{ J/kJ})}{-198.1 \text{ J/K}} = 463 \text{ K}\end{aligned}$$

This is a case in which a chemical engineer is severely limited by thermodynamics. Any attempt to increase the rate of reaction of nitrogen with hydrogen by increasing the temperature will cause reactants to be favored over products above 463 K.

#### ? Exercise 19.6.4

As you found in the exercise in Example 19.6.3,  $\Delta H^\circ$  and  $\Delta S^\circ$  are both negative for the reaction of nitric oxide and oxygen to form nitrogen dioxide. Use those data to calculate the temperature at which this reaction changes from spontaneous to nonspontaneous.

#### Answer

792.6 K

[Video Solution](#)

### Summary

- The change in Gibbs free energy, which is based solely on changes in state functions, is the criterion for predicting the spontaneity of a reaction.
- Free-energy change:

$$\Delta G = \Delta H - T\Delta S$$

- Standard free-energy change:

$$\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ$$

We can predict whether a reaction will occur spontaneously by combining the entropy, enthalpy, and temperature of a system in a new state function called Gibbs free energy (G). The change in free energy ( $\Delta G$ ) is the difference between the heat released during a process and the heat released for the same process occurring in a reversible manner. If a system is at equilibrium,  $\Delta G = 0$ . If the process is spontaneous,  $\Delta G < 0$ . If the process is not spontaneous as written but is spontaneous in the reverse direction,  $\Delta G > 0$ . At constant temperature and pressure,  $\Delta G$  is equal to the maximum amount of work a system can perform on its surroundings while undergoing a spontaneous change. The standard free-energy change ( $\Delta G^\circ$ ) is the change in free energy when one substance or a set of substances in their standard states is converted to one or more other substances, also in their standard states. The standard free energy of formation ( $\Delta G^\circ_f$ ), is the change in free energy that occurs when 1 mol of a substance in its standard state is formed from the component elements in their standard states. Tabulated values of standard free energies of formation are used to calculate  $\Delta G^\circ$  for a reaction.

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