

## 29.8: A Catalyst Affects the Mechanism and Activation Energy

As can be seen from the Arrhenius equation, the magnitude of the activation energy,  $E_a$ , determines the value of the rate constant,  $k$ , at a given temperature and thus the overall reaction rate. Catalysts provide a means of reducing  $E_a$  and increasing the reaction rate. Catalysts are defined as substances that participate in a chemical reaction but are not changed or consumed. Instead they provide a new mechanism for a reaction to occur which has a lower activation energy than that of the reaction without the catalyst.

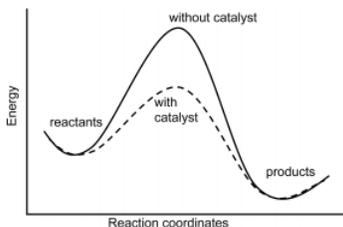
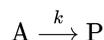


Figure 29.8.1 : Comparison of energy profiles with and without catalyst present.

*Homogeneous catalysis* refers to reactions in which the catalyst is in solution with at least one of the reactants whereas *heterogeneous catalysis* refers to reactions in which the catalyst is present in a different phase, usually as a solid, than the reactants. Figure 29.8.1 shows a comparison of energy profiles of a reaction in the absence and presence of a catalyst.

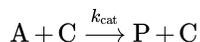
Consider a non-catalyzed elementary reaction



which proceeds at rate  $k$  at a certain temperature. The reaction rate can be expressed as

$$\frac{d[A]}{dt} = -k[A]$$

In the presence of a catalyst C, we can write the reaction as



and the reaction rate as

$$\frac{d[A]}{dt} = -k[A] - k_{\text{cat}}[A][C]$$

where the first term represents the uncatalyzed reaction and the second term represents the catalyzed reaction. Because the reaction rate of the catalyzed reaction is often magnitudes larger than that of the uncatalyzed reaction (i.e.  $k_{\text{cat}} \gg k$ ), the first term can often be ignored.

### Example of Homogenous Catalysis: Acid Catalysis

A common example of homogeneous catalysts are acids and bases. For example, given an overall reaction is  $S \rightarrow P$ . If  $k$  is the rate, then

$$\frac{d[P]}{dt} = k[S]$$

The purpose of an enzyme is to enhance the rate of production of the product P. The equations of the acid-catalyzed reaction are



The full set of kinetic equations is

$$\frac{d[S]}{dt} = -k_1 [S] [AH] + k_{-1} [SH^+] [A^-] \quad (29.8.4)$$

$$\frac{d[AH]}{dt} = -k_1 [S] [AH] + k_{-1} [SH^+] [A^-] - k_{-3} [AH] + k_3 [H_3O^+] [A^-] \quad (29.8.5)$$

$$\frac{d[SH^+]}{dt} = k_1 [S] [AH] - k_{-1} [SH^+] [A^-] - k_2 [SH^+] \quad (29.8.6)$$

$$\frac{d[A^-]}{dt} = k_1 [S] [AH] - k_{-1} [SH^+] [A^-] - k_2 [A^-] [H_3O^+] + k_{-3} [AH] \quad (29.8.7)$$

$$\frac{d[P]}{dt} = k_2 [SH^+] \quad (29.8.8)$$

$$\frac{d[H_3O^+]}{dt} = -k_2 [SH^+] - k_3 [H_3O^+] [A^-] + k_{-3} [AH] \quad (29.8.9)$$

We cannot easily solve these, as they are nonlinear. However, let us consider two cases  $k_2 \gg k_{-1} [A^-]$  and  $k_2 \ll k_{-1} [A^-]$ . In both cases,  $SH^+$  is consumed quickly, and we can apply a steady-state approximation:

$$\frac{d[SH^+]}{dt} = k_1 [S] [AH] - k_{-1} [A^-] [SH^+] - k_2 [SH^+] = 0$$

Rearranging in terms of  $SH^+$  yields

$$[SH^+] = \frac{k_1 [S] [AH]}{k_{-1} [A^-] + k_2}$$

and the rate of production of P can be written as

$$\frac{d[P]}{dt} = k_2 [SH^+] = \frac{k_1 k_2 [S] [AH]}{k_{-1} [A^-] + k_2}$$

In the case where  $k_2 \gg k_{-1} [A^-]$ , Equation 29.8.17 can be written as

$$\frac{d[P]}{dt} = k_1 [S] [AH]$$

which is known as a general acid-catalyzed reaction. On the other hand, if  $k_2 \ll k_{-1} [A^-]$ , we can use an equilibrium approximation to write the rate of production of P as

$$\frac{d[P]}{dt} = \frac{k_1 k_2 [S] [AH]}{k_{-1} [A^-]} = \frac{k_1 k_2}{k_{-1} K} [S] [H^+]$$

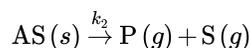
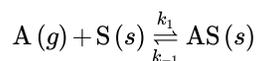
where  $K$  is the acid dissociation constant:

$$K = \frac{[A^-] [H^+]}{[AH]}$$

In this case, the reaction is hydrogen ion-catalyzed.

## Example of Heterogeneous Catalysis: Surface Catalysis of Gas-Phase Reactions

Many gas-phase reactions are catalyzed on a solid surface. For a first-order, unimolecular reaction, the reaction mechanism can be written as



where the first step is reversible adsorption of the gas molecule, A, onto active sites on the catalyst surface, S, to form a transition state, AS, and the second step is the conversion of adsorbed A molecules to species P. Applying the steady-state approximation to species AS, we can write

$$\frac{d[AS]}{dt} = k_1 [A] [S] - k_{-1} [AS]_{ss} - k_2 [AS]_{ss} = 0$$

Because the concentration of total active sites on the catalyst surface is fixed at  $[S]_0$ , the concentration of adsorbed species on the catalyst surface,  $[AS]$  can be written as

$$[AS] = \theta [S]_0$$

and  $[S]$  can be written as

$$[S] = (1 - \theta) [S]_0$$

where  $\theta$  is the fractional surface coverage of species A on the catalyst surface. We can now write Equation 29.8.23 as

$$k_1 [A] (1 - \theta) [S]_0 - (k_{-1} + k_2) \theta [S]_0 = 0$$

Rearranging the above equation in terms of  $\theta$  yields

$$\theta = \frac{k_1 [A]}{k_1 [A] + k_{-1} + k_2}$$

The rate of production of P can be written as

$$\frac{d[P]}{dt} = k_2 [AS]_{ss} = k_2 \theta [S]_0 = \frac{k_1 k_2}{k_1 [A] + k_{-1} + k_2} [A] [S]_0$$

From the above equation, we can observe the importance of having high surface areas for catalytic reactions.

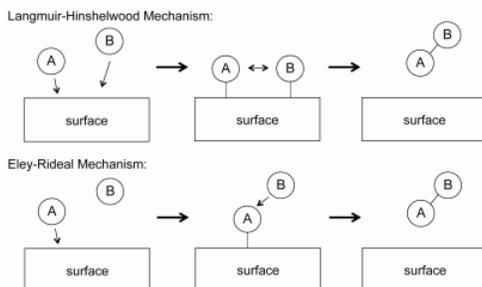
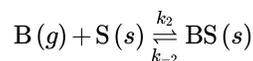
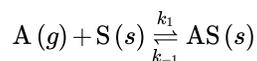


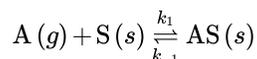
Figure 29.8.2 : Illustrations of the Langmuir-Hinshelwood and Eley-Rideal mechanisms for heterogeneous catalysis of bimolecular gas-phase reactions.

For bimolecular gas-phase reactions, two generally-used mechanisms to explain reactions kinetics are the Langmuir-Hinshelwood and Eley-Rideal mechanisms, shown in Figure 29.8.2 . In the Langmuir-Hinshelwood mechanism, A and B both adsorb onto the catalyst surface, at which they react to form a product. The reaction mechanism is



The rate law for the Langmuir-Hinshelwood mechanism can be derived in a similar manner to that for unimolecular catalytic reactions by assuming that the total number of active sites on the catalyst surface is fixed. In the Eley-Rideal mechanism, only one species adsorbs onto the catalyst surface. An example of such a reaction is the partial oxidation of ethylene into ethylene oxide, as shown in Figure 29.8.3 . In this reaction, diatomic oxygen adsorbs onto the catalytic surface where it reacts with ethylene molecules in the gas phase.

The reactions for the Eley-Rideal mechanism can be written as



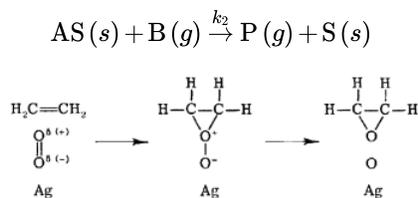


Figure 29.8.3 : Illustrations of the reaction mechanism for the partial oxidation of ethylene to ethylene oxide. [Reproduced from Kilty, PA and WMH Sachtler. Catal. Rev., 10, 1]

Assuming that  $k_{-1} \gg k_1$ , we can apply a steady-state approximation to species AS:

$$\frac{d[AS]}{dt} = 0 = k_1 [A] [S] - k_{-1} [AS]_{ss} - k_2 [AS]_{ss} [B]$$

As in the case of unimolecular catalyzed reactions, we can express the concentrations of AS and S in terms of a fraction of the total number of active sites,  $S_0$  and rewrite the above equation as

$$0 = k_1 [A] (1 - \theta) [S]_0 - k_{-1} [S]_0 - k_2 \theta [S]_0 [B]$$

Solving for  $\theta$  yields

$$\theta = \frac{k_1 [A]}{k_1 [A] + k_{-1} + k_2 [B]}$$

Furthermore, if  $k_2 \ll k_1$  and  $k_{-1}$ , we can simplify  $\theta$  to

$$\theta = \frac{k_1 [A]}{k_1 [A] + k_{-1}}$$

The rate of production of P can be expressed as

$$\frac{d[P]}{dt} = k_2 [AS]_{ss} [B] = k_2 \theta [S]_0 [B] = \frac{k_1 k_2 [A]}{k_1 [A] + k_{-1}} [S]_0 [B]$$

We can also write the above expression in terms of the equilibrium constant,  $K$ , which is equal to  $k_1/k_{-1}$

$$\frac{d[P]}{dt} = K k_2 [B] \frac{K [A]}{K [A] + 1}$$

## Contributors and Attributions

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