

## 25.7: Image Formation by Mirrors

### Learning Objectives

By the end of this section, you will be able to:

- Illustrate image formation in a flat mirror.
- Explain with ray diagrams the formation of an image using spherical mirrors.
- Determine focal length and magnification given radius of curvature, distance of object and image.

We only have to look as far as the nearest bathroom to find an example of an image formed by a mirror. Images in flat mirrors are the same size as the object and are located behind the mirror. Like lenses, mirrors can form a variety of images. For example, dental mirrors may produce a magnified image, just as makeup mirrors do. Security mirrors in shops, on the other hand, form images that are smaller than the object. We will use the law of reflection to understand how mirrors form images, and we will find that mirror images are analogous to those formed by lenses.

Figure [Math Processing Error] helps illustrate how a flat mirror forms an image. Two rays are shown emerging from the same point, striking the mirror, and being reflected into the observer's eye. The rays can diverge slightly, and both still get into the eye. If the rays are extrapolated backward, they seem to originate from a common point behind the mirror, locating the image. (The paths of the reflected rays into the eye are the same as if they had come directly from that point behind the mirror.) Using the law of reflection -- the angle of reflection equals the angle of incidence -- we can see that the image and object are the same distance from the mirror. This is a virtual image, since it cannot be projected -- the rays only appear to originate from a common point behind the mirror. Obviously, if you walk behind the mirror, you cannot see the image, since the rays do not go there. But in front of the mirror, the rays behave exactly as if they had come from behind the mirror, so that is where the image is situated.

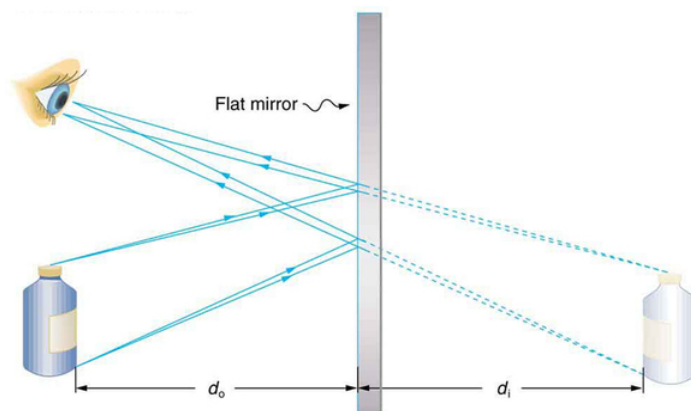


Figure [Math Processing Error]: Two sets of rays from common points on an object are reflected by a flat mirror into the eye of an observer. The reflected rays seem to originate from behind the mirror, locating the virtual image.

Now let us consider the focal length of a mirror -- for example, the concave spherical mirrors in Figure [Math Processing Error]. Rays of light that strike the surface follow the law of reflection. For a mirror that is large compared with its radius of curvature, as in Figure [Math Processing Error], we see that the reflected rays do not cross at the same point, and the mirror does not have a well-defined focal point. If the mirror had the shape of a parabola, the rays would all cross at a single point, and the mirror would have a well-defined focal point. But parabolic mirrors are much more expensive to make than spherical mirrors. The solution is to use a mirror that is small compared with its radius of curvature, as shown in Figure [Math Processing Error]. (This is the mirror equivalent of the thin lens approximation.) To a very good approximation, this mirror has a well-defined focal point at  $F$  that is the focal distance [Math Processing Error] from the center of the mirror. The focal length [Math Processing Error] of a concave mirror is positive, since it is a converging mirror.

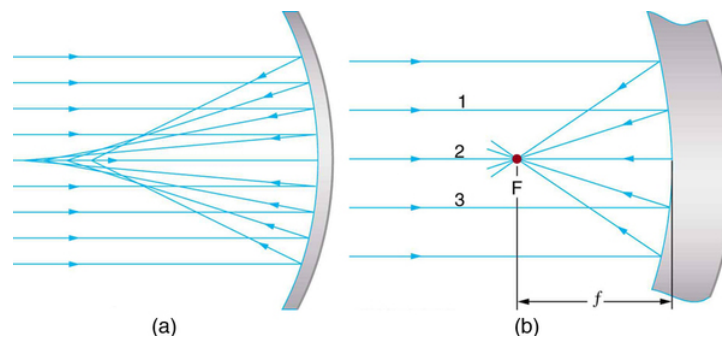


Figure [Math Processing Error]: (a) Parallel rays reflected from a large spherical mirror do not all cross at a common point. (b) If a spherical mirror is small compared with its radius of curvature, parallel rays are focused to a common point. The distance of the focal point from the center of the mirror is its focal length [Math Processing Error]. Since this mirror is converging, it has a positive focal length.

Just as for lenses, the shorter the focal length, the more powerful the mirror; thus, [Math Processing Error] for a mirror, too. A more strongly curved mirror has a shorter focal length and a greater power. Using the law of reflection and some simple trigonometry, it can be shown that the focal length is half the radius of curvature, or [Math Processing Error] where [Math Processing Error] is the radius of curvature of a spherical mirror. The smaller the radius of curvature, the smaller the focal length and, thus, the more powerful the mirror.

The convex mirror shown in Figure [Math Processing Error] also has a focal point. Parallel rays of light reflected from the mirror seem to originate from the point F at the focal distance [Math Processing Error] behind the mirror. The focal length and power of a convex mirror are negative, since it is a diverging mirror.

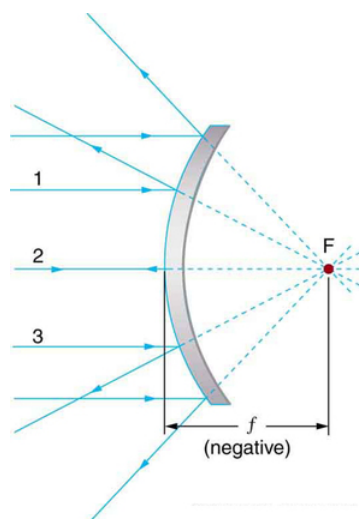


Figure [Math Processing Error]: Parallel rays of light reflected from a convex spherical mirror (small in size compared with its radius of curvature) seem to originate from a well-defined focal point at the focal distance [Math Processing Error] behind the mirror. Convex mirrors diverge light rays and, thus, have a negative focal length.

Ray tracing is as useful for mirrors as for lenses. The rules for ray tracing for mirrors are based on the illustrations just discussed:

#### Ray Tracing Rules

1. A ray approaching a concave converging mirror parallel to its axis is reflected through the focal point F of the mirror on the same side. (See rays 1 and 3 in Figure [Math Processing Error])
2. A ray approaching a convex diverging mirror parallel to its axis is reflected so that it seems to come from the focal point F behind the mirror. (See rays 1 and 3 in Figure [Math Processing Error]).
3. Any ray striking the center of a mirror is followed by applying the law of reflection; it makes the same angle with the axis when leaving as when approaching. (See ray 2 in Figures [Math Processing Error] and [Math Processing Error]).
4. A ray approaching a concave converging mirror through its focal point is reflected parallel to its axis. (The reverse of rays 1 and 3 in Figure [Math Processing Error]).

5. A ray approaching a convex diverging mirror by heading toward its focal point on the opposite side is reflected parallel to the axis. (The reverse of rays 1 and 3 in Figure [Math Processing Error]).

We will use ray tracing to illustrate how images are formed by mirrors, and we can use ray tracing quantitatively to obtain numerical information. But since we assume each mirror is small compared with its radius of curvature, we can use the thin lens equations for mirrors just as we did for lenses.

Consider the situation shown in Figure [Math Processing Error], concave spherical mirror reflection, in which an object is placed farther from a concave (converging) mirror than its focal length. That is, [Math Processing Error] is positive and [Math Processing Error], so that we may expect an image similar to the case 1 real image formed by a converging lens. Ray tracing in Figure 4 shows that the rays from a common point on the object all cross at a point on the same side of the mirror as the object. Thus a real image can be projected onto a screen placed at this location. The image distance is positive, and the image is inverted, so its magnification is negative. This is a *case 1 image for mirrors*. It differs from the case 1 image for lenses only in that the image is on the same side of the mirror as the object. It is otherwise identical.

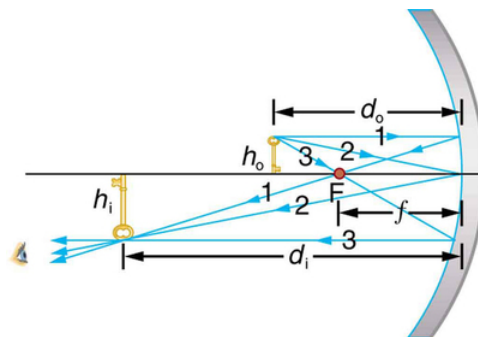


Figure [Math Processing Error]: A case 1 image for a mirror. An object is farther from the converging mirror than its focal length. Rays from a common point on the object are traced using the rules in the text. Ray 1 approaches parallel to the axis, ray 2 strikes the center of the mirror, and ray 3 goes through the focal point on the way toward the mirror. All three rays cross at the same point after being reflected, locating the inverted real image. Although three rays are shown, only two of the three are needed to locate the image and determine its height.

### Example [Math Processing Error]: A Concave Reflector

Electric room heaters use a concave mirror to reflect infrared (IR) radiation from hot coils. Note that IR follows the same law of reflection as visible light. Given that the mirror has a radius of curvature of 50.0 cm and produces an image of the coils 3.00 m away from the mirror, where are the coils?

#### Strategy and Concept

We are given that the concave mirror projects a real image of the coils at an image distance [Math Processing Error]. The coils are the object, and we are asked to find their location -- that is, to find the object distance [Math Processing Error]. We are also given the radius of curvature of the mirror, so that its focal length is [Math Processing Error] (positive since the mirror is concave or converging). Assuming the mirror is small compared with its radius of curvature, we can use the thin lens equations, to solve this problem.

#### Solution

Since [Math Processing Error] and [Math Processing Error] are known, thin lens equation can be used to find [Math Processing Error]:

[Math Processing Error]

Rearranging to isolate [Math Processing Error] gives

[Math Processing Error]

Entering known quantities gives a value for [Math Processing Error]:

[Math Processing Error]

This must be inverted to find [Math Processing Error]:

[Math Processing Error]

## Discussion

Note that the object (the filament) is farther from the mirror than the mirror's focal length. This is a case 1 image ([Math Processing Error] and [Math Processing Error] positive), consistent with the fact that a real image is formed. You will get the most concentrated thermal energy directly in front of the mirror and 3.00 m away from it. Generally, this is not desirable, since it could cause burns. Usually, you want the rays to emerge parallel, and this is accomplished by having the filament at the focal point of the mirror.

Note that the filament here is not much farther from the mirror than its focal length and that the image produced is considerably farther away. This is exactly analogous to a slide projector. Placing a slide only slightly farther away from the projector lens than its focal length produces an image significantly farther away. As the object gets closer to the focal distance, the image gets farther away. In fact, as the object distance approaches the focal length, the image distance approaches infinity and the rays are sent out parallel to one another.

## Example [Math Processing Error]: Solar Electric Generating System

One of the solar technologies used today for generating electricity is a device (called a parabolic trough or concentrating collector) that concentrates the sunlight onto a blackened pipe that contains a fluid. This heated fluid is pumped to a heat exchanger, where its heat energy is transferred to another system that is used to generate steam -- and so generate electricity through a conventional steam cycle. Figure [Math Processing Error] shows such a working system in southern California. Concave mirrors are used to concentrate the sunlight onto the pipe. The mirror has the approximate shape of a section of a cylinder. For the problem, assume that the mirror is exactly one-quarter of a full cylinder.

- If we wish to place the fluid-carrying pipe 40.0 cm from the concave mirror at the mirror's focal point, what will be the radius of curvature of the mirror?
- Per meter of pipe, what will be the amount of sunlight concentrated onto the pipe, assuming the insolation (incident solar radiation) is [Math Processing Error]?
- If the fluid-carrying pipe has a 2.00-cm diameter, what will be the temperature increase of the fluid per meter of pipe over a period of one minute? Assume all the solar radiation incident on the reflector is absorbed by the pipe, and that the fluid is mineral oil.

## Strategy

To solve an *Integrated Concept Problem* we must first identify the physical principles involved. Part (a) is related to the current topic. Part (b) involves a little math, primarily geometry. Part (c) requires an understanding of heat and density.

## Solution

(a) To a good approximation for a concave or semi-spherical surface, the point where the parallel rays from the sun converge will be at the focal point, so [Math Processing Error].

(b) The insolation is [Math Processing Error]. We must find the cross-sectional area [Math Processing Error] of the concave mirror, since the power delivered is [Math Processing Error]. The mirror in this case is a quarter-section of a cylinder, so the area for a length [Math Processing Error] of the mirror is [Math Processing Error]. The area for a length of 1.00 m is then

$$[Math Processing Error]$$

The insolation on the 1.00-m length of pipe is then

$$[Math Processing Error]$$

(c) The increase in temperature is given by [Math Processing Error]. the mass [Math Processing Error] of the mineral oil in the one-meter section of pipe is

$$[Math Processing Error]$$

Therefore, the increase in temperature in one minute is

$$[Math Processing Error]$$

## Discussion (c)

An array of such pipes in the California desert can provide a thermal output of 250 MW on a sunny day, with fluids reaching temperatures as high as [Math Processing Error] We are considering only one meter of pipe here, and ignoring heat losses along the pipe.



Figure [Math Processing Error]: Parabolic trough collectors are used to generate electricity in southern California. (credit: kjkolb, Wikimedia Commons)

What happens if an object is closer to a concave mirror than its focal length? This is analogous to a case 2 image for lenses ([Math Processing Error] and [Math Processing Error] positive), which is a magnifier. In fact, this is how makeup mirrors act as magnifiers. Figure [Math Processing Error] uses ray tracing to locate the image of an object placed close to a concave mirror. Rays from a common point on the object are reflected in such a manner that they appear to be coming from behind the mirror, meaning that the image is virtual and cannot be projected. As with a magnifying glass, the image is upright and larger than the object. This is a *case 2 image for mirrors* and is exactly analogous to that for lenses.

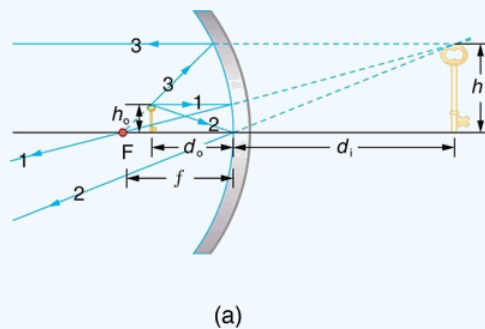
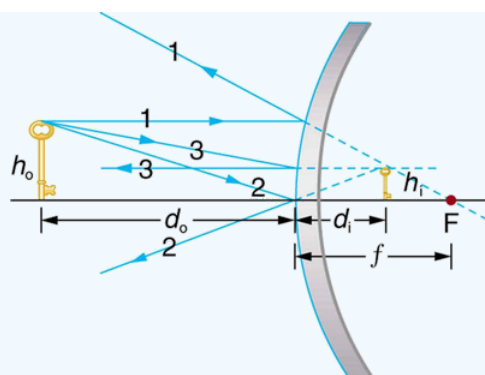


Figure [Math Processing Error]: (a) Case 2 images for mirrors are formed when a converging mirror has an object closer to it than its focal length. Ray 1 approaches parallel to the axis, ray 2 strikes the center of the mirror, and ray 3 approaches the mirror as if it came from the focal point. (b) A magnifying mirror showing the reflection. (credit: Mike Melrose, Flickr)

All three rays appear to originate from the same point after being reflected, locating the upright virtual image behind the mirror and showing it to be larger than the object. (b) Makeup mirrors are perhaps the most common use of a concave mirror to produce a larger, upright image.

A convex mirror is a diverging mirror ([Math Processing Error] is negative) and forms only one type of image. It is a *case 3 image* -- one that is upright and smaller than the object, just as for diverging lenses. Figure [Math Processing Error] uses ray tracing to illustrate the location and size of the case 3 image for mirrors. Since the image is behind the mirror, it cannot be projected and is thus a virtual image. It is also seen to be smaller than the object.



(a)



(b)

Figure [Math Processing Error]: uses ray tracing to illustrate the location and size of the case 3 image for mirrors. Since the image is behind the mirror, it cannot be projected and is thus a virtual image. It is also seen to be smaller than the object.

### Example [Math Processing Error]: Image in a Convex Mirror

A keratometer is a device used to measure the curvature of the cornea, particularly for fitting contact lenses. Light is reflected from the cornea, which acts like a convex mirror, and the keratometer measures the magnification of the image. The smaller the magnification, the smaller the radius of curvature of the cornea. If the light source is 12.0 cm from the cornea and the image's magnification is 0.0320, what is the cornea's radius of curvature?

#### Strategy

If we can find the focal length of the convex mirror formed by the cornea, we can find its radius of curvature (the radius of curvature is twice the focal length of a spherical mirror). We are given that the object distance is [Math Processing Error] and that [Math Processing Error]. We first solve for the image distance [Math Processing Error], and then for [Math Processing Error].

#### Solution

[Math Processing Error]. Solving this expression for [Math Processing Error] gives

[Math Processing Error]

Entering known values yields

[Math Processing Error]

[Math Processing Error]

Substituting known values,

[Math Processing Error]

This must be inverted to find [Math Processing Error].

[Math Processing Error]

The radius of curvature is twice the focal length, so that



[Math Processing Error]

#### Discussion:

Although the focal length [Math Processing Error] of a convex mirror is defined to be negative, we take the absolute value to give us a positive value for [Math Processing Error].

The radius of curvature found here is reasonable for a cornea. The distance from cornea to retina in an adult eye is about 2.0 cm. In practice, many corneas are not spherical, complicating the job of fitting contact lenses. Note that the image distance here is negative, consistent with the fact that the image is behind the mirror, where it cannot be projected. In this section's Problems and Exercises, you will show that for a fixed object distance, the smaller the radius of curvature, the smaller the magnification.

The three types of images formed by mirrors (cases 1, 2, and 3) are exactly analogous to those formed by lenses, as summarized in the table at the end of "Image Formation by Lenses." It is easiest to concentrate on only three types of images -- then remember that concave mirrors act like convex lenses, whereas convex mirrors act like concave lenses.

#### TAKE-HOME EXPERIMENT: CONCAVE MIRRORS CLOSE TO HOME

Find a flashlight and identify the curved mirror used in it. Find another flashlight and shine the first flashlight onto the second one, which is turned off. Estimate the focal length of the mirror. You might try shining a flashlight on the curved mirror behind the headlight of a car, keeping the headlight switched off, and determine its focal length.

#### Problem-Solving Strategy for Mirrors

- Step 1. Examine the situation to determine that image formation by a mirror is involved.
- Step 2. Refer to the "Problem-Solving Strategies for Lenses." The same strategies are valid for mirrors as for lenses with one qualification-- use the ray tracing rules for mirrors listed earlier in this section.

### Summary

- The characteristics of an image formed by a flat mirror are: (a) The image and object are the same distance from the mirror, (b) The image is a virtual image, and (c) The image is situated behind the mirror.
- Image length is half the radius of curvature. [Math Processing Error]
- A convex mirror is a diverging mirror and forms only one type of image, namely a virtual image.

### Glossary

#### converging mirror

a concave mirror in which light rays that strike it parallel to its axis converge at one or more points along the axis

#### diverging mirror

a convex mirror in which light rays that strike it parallel to its axis bend away (diverge) from its axis

#### law of reflection

angle of reflection equals the angle of incidence

This page titled [25.7: Image Formation by Mirrors](#) is shared under a [CC BY 4.0](#) license and was authored, remixed, and/or curated by [OpenStax](#) via [source content](#) that was edited to the style and standards of the LibreTexts platform.