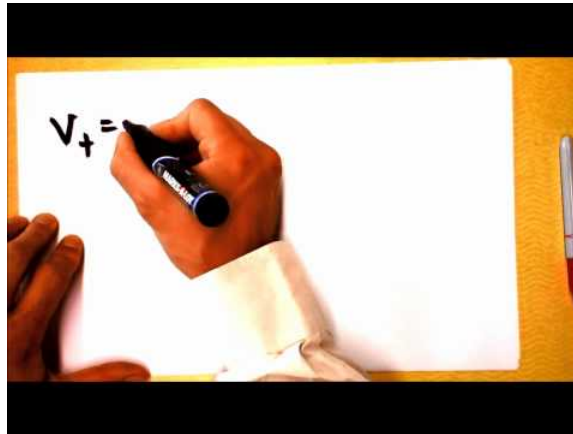
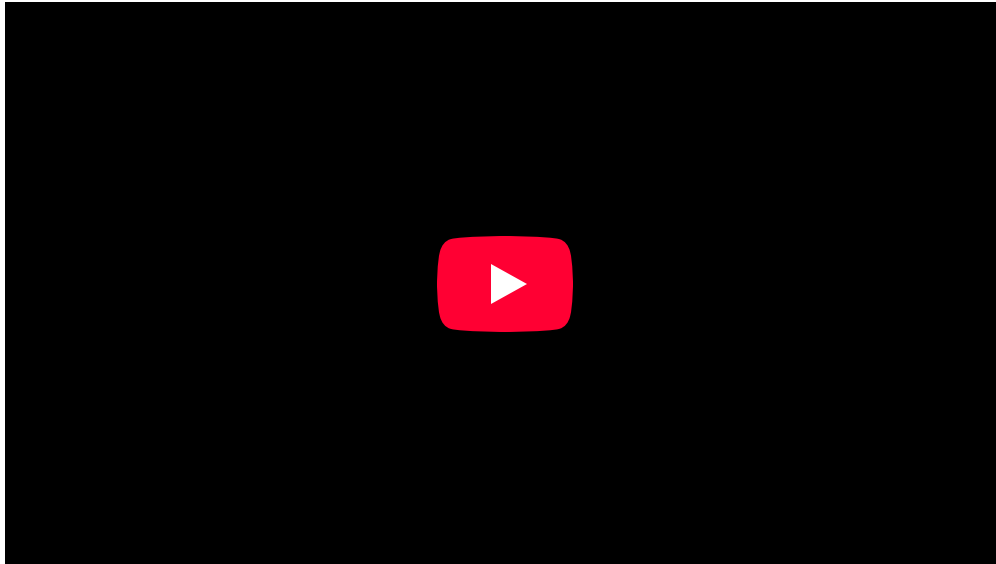


9.3: Rotational Kinematics

learning objectives

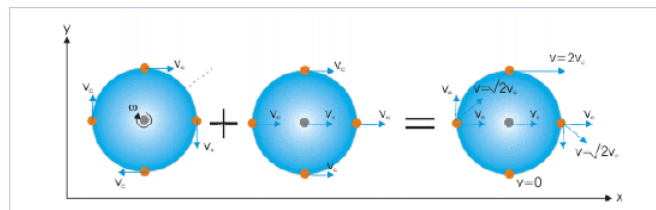
- Distinguish the two different motions in which rolling without slipping is broken down

Rolling without slipping generally occurs when an object rolls without skidding. To relate this to a real world phenomenon, we can consider the example of a wheel rolling on a flat, horizontal surface.



Connecting Linear and Rotational Motion! Rolling without Slipping!: How fast does the axle of a bike wheel move? How fast does the BOTTOM of a wheel move?

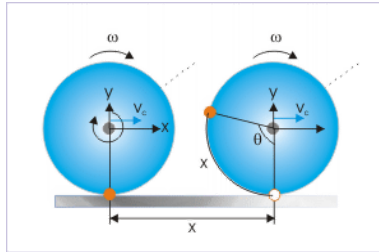
Rolling without slipping can be better understood by breaking it down into two different motions: 1) Motion of the center of mass, with linear velocity v (translational motion); and 2) rotational motion around its center, with angular velocity ω .



Rolling Motion: Rolling motion is a combination of rotational and translational motion.

When an object is rolling on a plane without slipping, the point of contact of the object with the plane does not move. If we imagine a wheel moving forward by rolling on a plane at speed v , it must also be rotating about its axis at an angular speed ω since it is rolling.

The object's angular velocity ω is directly proportional to its velocity, because as we know, the faster we are driving in a car, the faster the wheels have to turn. So, to determine the exact relationship between linear velocity and angular velocity, we can imagine the scenario in which the wheel travels a distance of x while rotating through an angle θ .



Rolling Without Slipping: A body rolling a distance of x on a plane without slipping.

In mathematical terms, the length of the arc is equal to the angle of the segment multiplied by the object's radius, R . Therefore, we can say that the length of the arc of the wheel that has rotated an angle θ , is equal to $R\theta$. Furthermore, since the wheel is in constant contact with the ground, the length of the arc correlating to the angle is also equal to x . Therefore,

$$x = R\theta \quad (9.3.1)$$

Since x and θ depend on time, we can take the derivative of both sides to obtain:

$$\frac{dx}{dt} = R \frac{d\theta}{dt} \quad (9.3.2)$$

where $\frac{dx}{dt}$ is equal to the linear velocity v , and $\frac{d\theta}{dt}$ is equal to the angular velocity ω . We can then simplify this equation to:

$$v = \omega R \quad (9.3.3)$$

Key Points

- Rolling without slipping can be better understood by breaking it down into translational motion and rotational motion.
- When an object is rolling on a plane without slipping, the point of contact of the object with the plane does not move.
- A rolling object's velocity v is directly related to its angular velocity ω , and is mathematically expressed as $v = \omega R$, where R is the object's radius and v is its linear velocity.

Key Terms

- **angular velocity:** A vector quantity describing the motion of an object in circular motion; its magnitude is equal to the angular speed (ω) of the particle, and the direction is perpendicular to the plane of its circular motion.
- **linear velocity:** A vector quantity that denotes the rate of change of position with respect to time of the object's center of mass.

LICENSES AND ATTRIBUTIONS

CC LICENSED CONTENT, SHARED PREVIOUSLY

- Curation and Revision. **Provided by:** Boundless.com. **License:** [CC BY-SA: Attribution-ShareAlike](#)

CC LICENSED CONTENT, SPECIFIC ATTRIBUTION

- Kinematics. **Provided by:** Wikipedia. **Located at:** [en.Wikipedia.org/wiki/Kinematics%23Rolling_without_slipping](https://en.wikipedia.org/wiki/Kinematics%23Rolling_without_slipping). **License:** [CC BY-SA: Attribution-ShareAlike](#)
- Sunil Kumar Singh, Rolling Motion. September 17, 2013. **Provided by:** OpenStax CNX. **Located at:** <http://cnx.org/content/m14311/latest/>. **License:** [CC BY: Attribution](#)
- velocity. **Provided by:** Wiktionary. **Located at:** en.wiktionary.org/wiki/velocity. **License:** [CC BY-SA: Attribution-ShareAlike](#)
- Boundless. **Provided by:** Boundless Learning. **Located at:** www.boundless.com/physics/definition/angular-velocity. **License:** [CC BY-SA: Attribution-ShareAlike](#)

- Sunil Kumar Singh, Rolling Motion. November 8, 2012. **Provided by:** OpenStax CNX. **Located at:** <http://cnx.org/content/m14311/latest/>. **License:** [CC BY: Attribution](#)
 - Sunil Kumar Singh, Rolling Motion. November 8, 2012. **Provided by:** OpenStax CNX. **Located at:** <http://cnx.org/content/m14311/latest/>. **License:** [CC BY: Attribution](#)
 - Connecting Linear and Rotational Motion! Rolling without Slipping!. **Located at:** <http://www.youtube.com/watch?v=AuBuK1jVyGw>. **License:** [Public Domain: No Known Copyright](#). **License Terms:** Standard YouTube license
-

This page titled 9.3: Rotational Kinematics is shared under a [not declared](#) license and was authored, remixed, and/or curated by [Boundless](#).