

## 1.A: Electric Charges and Fields (Answer)

### Check Your Understanding

5.1. The force would point outward.

5.2. The net force would point  $58^\circ$  below the  $-x$ -axis.

5.3. 
$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

5.4. We will no longer be able to take advantage of symmetry. Instead, we will need to calculate each of the two components of the electric field with their own integral.

5.5. The point charge would be  $Q = \sigma ab$  where  $a$  and  $b$  are the sides of the rectangle but otherwise identical.

5.6. The electric field would be zero in between, and have magnitude  $\frac{\sigma}{\epsilon_0}$  everywhere else.

### Conceptual Questions

1. There are mostly equal numbers of positive and negative charges present, making the object electrically neutral.

3. a. yes;

b. yes

5. Take an object with a known charge, either positive or negative, and bring it close to the rod. If the known charged object is positive and it is repelled from the rod, the rod is charged positive. If the positively charged object is attracted to the rod, the rod is negatively charged.

7. No, the dust is attracted to both because the dust particle molecules become polarized in the direction of the silk.

9. Yes, polarization charge is induced on the conductor so that the positive charge is nearest the charged rod, causing an attractive force.

11. Charging by conduction is charging by contact where charge is transferred to the object. Charging by induction first involves producing a polarization charge in the object and then connecting a wire to ground to allow some of the charge to leave the object, leaving the object charged.

13. This is so that any excess charge is transferred to the ground, keeping the gasoline receptacles neutral. If there is excess charge on the gasoline receptacle, a spark could ignite it.

15. The dryer charges the clothes. If they are damp, the presence of water molecules suppresses the charge.

17. There are only two types of charge, attractive and repulsive. If you bring a charged object near the quartz, only one of these two effects will happen, proving there is not a third kind of charge.

19. a. No, since a polarization charge is induced. b. Yes, since the polarization charge would produce only an attractive force.

21. The force holding the nucleus together must be greater than the electrostatic repulsive force on the protons.

23. Either sign of the test charge could be used, but the convention is to use a positive test charge.

25. The charges are of the same sign.

27. At infinity, we would expect the field to go to zero, but because the sheet is infinite in extent, this is not the case. Everywhere you are, you see an infinite plane in all directions.

29. The infinite charged plate would have  $E = \frac{\sigma}{2\epsilon_0}$  everywhere. The field would point toward the plate if it were negatively charged and point away from the plate if it were positively charged. The electric field of the parallel plates would be zero between them if they had the same charge, and  $E = \frac{\sigma}{\epsilon_0}$  everywhere else. If the charges were opposite, the situation is reversed, zero outside the plates and  $E = \frac{\sigma}{\epsilon_0}$  between them.

31. yes; no

33. At the surface of Earth, the gravitational field is always directed in toward Earth's center. An electric field could move a charged particle in a different direction than toward the center of Earth. This would indicate an electric field is present.

35. 10

## Problems

37. a.  $2.00 \times 10^{-9} C \left( \frac{1}{1.602 \times 10^{-19}} e/C \right) = 1.248 \times 10^{10} \text{electrons}$ ;

b.  $0.500 \times 10^{-6} C \left( \frac{1}{1.602 \times 10^{-19}} e/C \right) = 3.121 \times 10^{12} \text{electrons}$

39.  $\frac{3.750 \times 10^{21} e}{6.242 \times 10^{18} e/C} = -600.8 C$

41. a.  $2.0 \times 10^{-9} C (6.242 \times 10^{18} e/C) = 1.248 \times 10^{10} e$ ;

b.  $9.109 \times 10^{-31} kg (1.248 \times 10^{10} e) = 1.137 \times 10^{-20} kg, \frac{1.137 \times 10^{-20} kg}{2.5 \times 10^{-3} kg} = 4.548 \times 10^{-18} \text{ or } 4.545 \times 10^{-16}$

43.  $5.00 \times 10^{-9} C (6.242 \times 10^{18} e/C) = 3.121 \times 10^{10} e$ ;  $3.121 \times 10^{10} e + 1.0000 \times 10^{12} e = 1.0312 \times 10^{12} e$ .

45. atomic mass of copper atom times  $1u = 1.055 \times 10^{-25} kg$ ; number of copper atoms =  $4.739 \times 10^{23} \text{atoms}$ ; number of electrons equals 29 times number of atoms or  $1.374 \times 10^{25} \text{electrons}$ ;  
 $\frac{2.00 \times 10^{-6} C (6.242 \times 10^{18} e/C)}{1.374 \times 10^{25} e} = 9.083 \times 10^{-13} \text{ or } 9.083 \times 10^{-11}$ .

47.  $244.00u (1.66 \times 10^{-27} kg/u) = 4.050 \times 10^{-25} kg$ ;  $\frac{4.00 kg}{4.050 \times 10^{-25} kg} = 9.877 \times 10^{24} \text{atoms}$

$9.877 \times 10^{24} (94) = 9.284 \times 10^{26} \text{protons}$ ;  $9.284 \times 10^{26} \text{protons}; 9.284 \times 10^{26} (1.602 \times 10^{-19} C/p) = 1.487 \times 10^8 C$

49. a. charge 1 is  $3\mu C$ ; charge 2 is  $12\mu C$ ,  $F_{31} = 2.16 \times 10^{-4} N$  to the left,

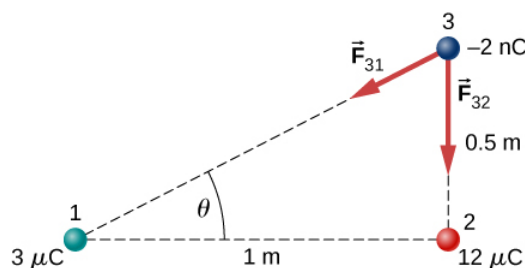
$F_{32} = 8.63 \times 10^{-4} N$  to the right,

$F_{net} = 6.47 \times 10^{-4} N$  to the right;

b.  $F_{31} = 2.16 \times 10^{-4} N$  to the right,

$F_{32} = 9.59 \times 10^{-5} N$  to the right,

$F_{net} = 3.12 \times 10^{-4} N$  to the right,



c.  $\vec{F}_{31x} = -2.76 \times 10^{-5} N \hat{i}$ ,

$\vec{F}_{31y} = -1.38 \times 10^{-5} N \hat{j}$ ,

$\vec{F}_{32y} = -8.63 \times 10^{-4} N \hat{j}$ ,

$\vec{F}_{net} = -2.76 \times 10^{-5} N \hat{i} - 8.77 \times 10^{-4} N \hat{j}$

51.  $F = 230.7 N$

53.  $F = 53.94 N$

55. The tension is  $T = 0.049 N$ . The horizontal component of the tension is  $0.0043 N$

$$d = 0.088m, q = 6.1 \times 10^{-8}C.$$

The charges can be positive or negative, but both have to be the same sign.

57. Let the charge on one of the spheres be  $rQ$ , where  $r$  is a fraction between 0 and 1. In the numerator of Coulomb's law, the term involving the charges is  $rQ(1-r)Q$ . This is equal to  $(r-r^2)Q^2$ . Finding the maximum of this term gives  $1-2r=0 \Rightarrow r=\frac{1}{2}$

59. Define right to be the positive direction and hence left is the negative direction, then  $F = -0.05N$

61. The particles form triangle of sides 13, 13, and 24 cm. The  $x$ -components cancel, whereas there is a contribution to the  $y$ -component from both charges 24 cm apart. The  $y$ -axis passing through the third charge bisects the 24-cm line, creating two right triangles of sides 5, 12, and 13 cm.  $F_y = 2.56N$  in the negative  $y$ -direction since the force is attractive. The net force from both charges is  $\vec{F}_{net} = -5.12N\hat{j}$

63. The diagonal is  $\sqrt{2}a$  and the components of the force due to the diagonal charge has a factor  $\cos\theta = \frac{1}{\sqrt{2}}$ ;

$$\vec{F}_{net} = [k\frac{q^2}{a^2} + k\frac{q^2}{2a^2}\frac{1}{\sqrt{2}}]\hat{i} - [k\frac{q^2}{a^2} + k\frac{q^2}{2a^2}\frac{1}{\sqrt{2}}]\hat{j}$$

65. a.  $E = 2.0 \times 10^{-2} \frac{N}{C}$  ;

b.  $F = 2.0 \times 10^{-19}N$

67. a.  $E = 2.88 \times 10^{11}N/C$ ;

b.  $E = 1.44 \times 10^{11}N/C$ ;

c.  $F = 4.61 \times 10^{-8}N$  on alpha particle

$F = 4.61 \times 10^{-8}N$  on electron

69.  $E = (-2.0\hat{i} + 3.0\hat{j})N$

71.  $F = 3.204 \times 10^{-14}N$ ,

$a = 3.517 \times 10^{16}m/s^2$

73.  $q = 2.78 \times 10^{-9}C$

75. a.  $E = 1.15 \times 10^{12}N/C$ ;

b.  $F = 1.47 \times 10^{-6}N$

77. If the  $q_2$  is to the right of  $q_1$ , the electric field vector from both charges point to the right.

a.  $E = 2.70 \times 10^6N/C$ ;

b.  $F = 54.0N$

79. There is  $45^\circ$  right triangle geometry. The  $x$ -components of the electric field at  $y = 3m$  cancel. The  $y$ -components give  $E(y = 3m) = 2.83 \times 10^3N/C$ .

At the origin we have a negative charge of magnitude  $q = -2.83 \times 10^{-6}C$

81.  $\vec{E}(z) = 3.6 \times 10^4N\hat{k}$

83.  $dE = \frac{1}{4\pi\epsilon_0} \frac{\lambda dx}{(x+a)^2}$ ,  $E = \frac{\lambda}{4\pi\epsilon_0} [\frac{1}{l+a} - \frac{1}{a}]$

85.  $\sigma = 0.02C/m^2$   $E = 2.26 \times 10^9N/C$

87. At  $P_1$ :  $\vec{E}(y) = \frac{1}{4\pi\epsilon_0} \frac{\lambda L}{y\sqrt{y^2 + \frac{L^2}{4}}} \hat{j} \Rightarrow \frac{1}{4\pi\epsilon_0} \frac{q}{\frac{a}{2}\sqrt{(\frac{a}{2})^2 + \frac{L^2}{4}}} \hat{j} = \frac{1}{\pi\epsilon_0} \frac{q}{a\sqrt{a^2 + L^2}} \hat{j}$

At  $P_2$ : Put the origin at the end of  $L$ .

$$dE = \frac{1}{4\pi\epsilon_0} \frac{\lambda dx}{(x+a)^2}, \vec{E} = -\frac{q}{4\pi\epsilon_0 l} \left[ \frac{1}{l+a} - \frac{1}{a} \right] \hat{i}$$

89. a.  $\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{2\lambda_x}{a} \hat{i} + \frac{1}{4\pi\epsilon_0} \frac{2\lambda_y}{b} \hat{j};$

b.  $\frac{1}{4\pi\epsilon_0} \frac{2(\lambda_x + \lambda_y)}{c} \hat{k}$

91. a.  $\vec{F} = 3.2 \times 10^{-17} N \hat{i},$

$$\vec{a} = 1.92 \times 10^{10} m/s^2 \hat{i};$$

b.  $\vec{F} = -3.2 \times 10^{-17} N \hat{i},$

$$\vec{a} = -3.51 \times 10^{13} m/s^2 \hat{i}$$

93.  $m = 6.5 \times 10^{-11} kg,$

$$E = 1.6 \times 10^7 N/C$$

95.  $E = 1.70 \times 10^6 N/C,$

$$F = 1.53 \times 10^{-3} NT \cos\theta = mgT \sin\theta = qE,$$

$$\tan\theta = 0.62 \Rightarrow \theta = 32.0^\circ,$$

This is independent of the length of the string.

97. circular arc  $dE_x(-\hat{i}) = \frac{1}{4\pi\epsilon_0} \frac{\lambda ds}{r^2} \cos\theta(-\hat{i}),$

$$\vec{E}_x = \frac{\lambda}{4\pi\epsilon_0 r} (-\hat{i}),$$

$$dE_y(-\hat{j}) = \frac{1}{4\pi\epsilon_0} \frac{\lambda ds}{r^2} \sin\theta(-\hat{j}),$$

$$\vec{E}_y = \frac{\lambda}{4\pi\epsilon_0 r} (-\hat{j});$$

$$\text{y-axis: } \vec{E}_x = \frac{\lambda}{4\pi\epsilon_0 r} (-\hat{i});$$

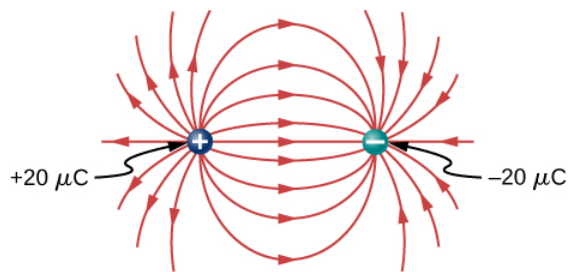
$$\text{x-axis: } \vec{E}_y = \frac{\lambda}{4\pi\epsilon_0 r} (-\hat{j}),$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r} (-\hat{i}) + \frac{\lambda}{2\pi\epsilon_0 r} (-\hat{j})$$

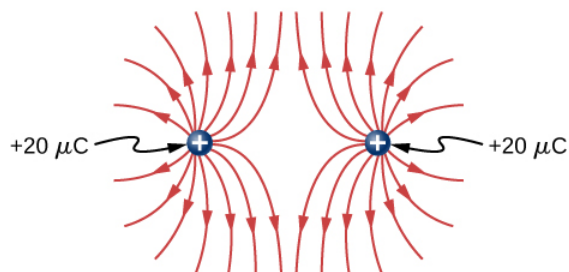
99. a.  $W = \frac{1}{2} m(v^2 - v_0^2), \frac{Qq}{4\pi\epsilon_0} \left( \frac{1}{r} - \frac{1}{r_0} \right) = \frac{1}{2} m(v^2 - v_0^2) \Rightarrow r_0 - r = \frac{4\pi\epsilon_0}{Qq} \frac{1}{2} m r r_0 (v^2 - v_0^2);$

b.  $r_0 - r$  is negative; therefore,  $v_0 > v, r \rightarrow \infty$ , and  $v \rightarrow 0: \frac{Qq}{4\pi\epsilon_0} \left( -\frac{1}{r_0} \right) = -\frac{1}{2} m v_0^2 \Rightarrow v_0 = \sqrt{\frac{Qq}{2\pi\epsilon_0 m r_0}}$

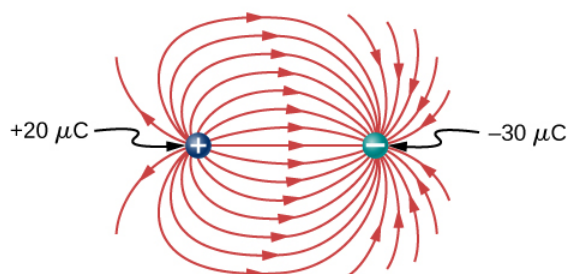
101.



(a)

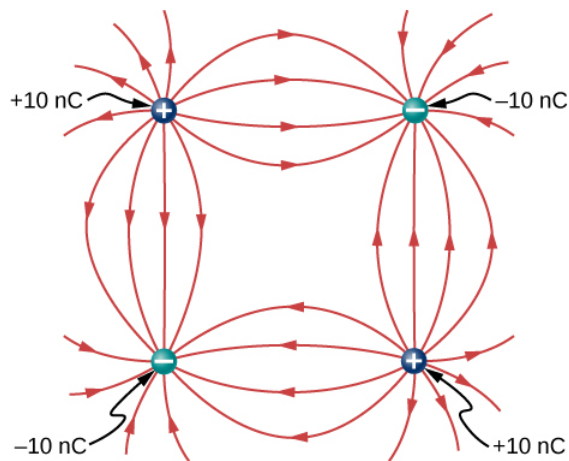


(b)



(c)

103.



$$105. E_x = 0, E_y = \frac{1}{4\pi\epsilon_0} \left[ \frac{2q}{(x^2 + a^2)} \right] \frac{a}{\sqrt{(x^2 + a^2)}} \Rightarrow x \gg a \Rightarrow \frac{1}{2\pi\epsilon_0} \frac{qa}{x^3}$$

$$E_y = \frac{q}{4\pi\epsilon_0} \left[ \frac{2ya + 2ya}{(y-a)^2(y+a)^2} \right] \Rightarrow y \gg a \Rightarrow \frac{1}{\pi\epsilon_0} \frac{qa}{y^3}$$

107. The net dipole moment of the molecule is the vector sum of the individual dipole moments between the two O-H. The separation O-H is 0.9578 angstroms:

$$\vec{p} = 1.889 \times 10^{-29} \text{ Cm } \hat{i}$$

### Additional Problems

$$109. \vec{F}_{net} = \left[ -8.99 \times 10^9 \frac{3.0 \times 10^{-6} (5.0 \times 10^{-6})}{(3.0 \text{ m})^2} - 8.99 \times 10^9 \frac{9.0 \times 10^{-6} (5.0 \times 10^{-6})}{(3.0 \text{ m})^2} \right] \hat{i}, -8.99 \times 10^9 \frac{6.0 \times 10^{-6} (5.0 \times 10^{-6})}{(3.0 \text{ m})^2} \hat{j} = -0.06 \text{ N } \hat{i} - 0.03 \text{ N } \hat{j}$$

111. Charges **Q** and **q** form a right triangle of sides 1 m and  $3 + \sqrt{3} \text{ m}$ . Charges **2Q** and **q** form a right triangle of sides 1 m and  $\sqrt{3} \text{ m}$ .

$$F_x = 0.049 \text{ N},$$

$$F_y = 0.09 \text{ N},$$

$$\vec{F}_{net} = 0.049 \text{ N } \hat{i} + 0.09 \text{ N } \hat{j}$$

$$113. W = 0.054 \text{ J}$$

$$115. \text{ a. } \vec{E} = \frac{1}{4\pi\epsilon_0} \left( \frac{q}{(2a)^2} - \frac{q}{a^2} \right) \hat{i};$$

$$\text{ b. } \vec{E} = \frac{\sqrt{3}}{4\pi\epsilon_0} \frac{q}{a^2} (-\hat{j});$$

$$\text{ c. } \vec{E} = \frac{2}{\pi\epsilon_0} \frac{q}{a^2} \frac{1}{\sqrt{2}} (-\hat{j})$$

$$117. \vec{E} = 6.4 \times 10^6 (\hat{i}) + 1.5 \times 10^7 (\hat{j}) \text{ N/C}$$

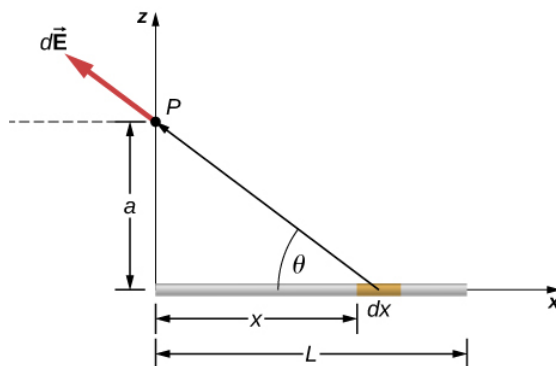
$$119. F = qE_0(1 + x/a) \quad W = \frac{1}{2} m(v^2 - v_0^2),$$

$$\frac{1}{2} m v^2 = qE_0 \left( \frac{15a}{2} \right) J$$

$$121. \text{ Electric field of wire at } \mathbf{x}: \vec{E}(x) = \frac{1}{4\pi\epsilon_0} \frac{2\lambda_y}{x} \hat{i},$$

$$dF = \frac{\lambda_y \lambda_x}{2\pi\epsilon_0} (\ln b - \ln a)$$

123.



$$dE_x = \frac{1}{4\pi\epsilon_0} \frac{\lambda dx}{(x^2 + a^2)} \frac{x}{\sqrt{x^2 + a^2}},$$

$$\vec{E}_x = \frac{\lambda}{4\pi\epsilon_0} \left[ \frac{1}{\sqrt{L^2 + a^2}} - \frac{1}{a} \right] \hat{i},$$

$$dE_z = \frac{1}{4\pi\epsilon_0} \frac{\lambda dx}{(x^2 + a^2)} \frac{a}{\sqrt{x^2 + a^2}},$$

$$\vec{E}_z = \frac{\lambda}{4\pi\epsilon_0 a} \frac{L}{\sqrt{L^2 + a^2}} \hat{k},$$

Substituting  $z$  for  $a$ , we have:

$$\vec{E}(z) = \frac{\lambda}{4\pi\epsilon_0} \left[ \frac{1}{\sqrt{L^2 + z^2}} - \frac{1}{z} \right] \hat{i} + \frac{\lambda}{4\pi\epsilon_0 z} \frac{L}{\sqrt{L^2 + z^2}} \hat{k}$$

**125.** There is a net force only in the  $y$ -direction. Let  $\theta$  be the angle the vector from  $\mathbf{dx}$  to  $\mathbf{q}$  makes with the  $x$ -axis. The components along the  $x$ -axis cancel due to symmetry, leaving the  $y$ -component of the force.

$$dF_y = \frac{1}{4\pi\epsilon_0} \frac{aq\lambda dx}{(x^2 + a^2)^{3/2}},$$

$$F_y = \frac{1}{2\pi\epsilon_0} \frac{q\lambda}{a} \left[ \frac{l/2}{((l/2)^2 + a^2)^{1/2}} \right]$$

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