

10.1.1: Review- Linear Equations

Linear regression for two variables is based on a linear equation with one independent variable. The equation has the form:

$$y = a + bx$$

where a and b are constant numbers. The variable x is the *independent variable*, and y is the *dependent variable*. Typically, you choose a value to substitute for the independent variable and then solve for the dependent variable.

✓ Example 10.1.1.1

The following examples are linear equations.

$$y = 3 + 2x$$

$$y = -0.01 + 1.2x$$

? Exercise 10.1.1.1

Is the following an example of a linear equation?

$$y = -0.125 - 3.5x$$

Answer

yes

The graph of a linear equation of the form $y = a + bx$ is a **straight line**. Any line that is not vertical can be described by this equation.

✓ Example 10.1.1.2

Graph the equation $y = -1 + 2x$.

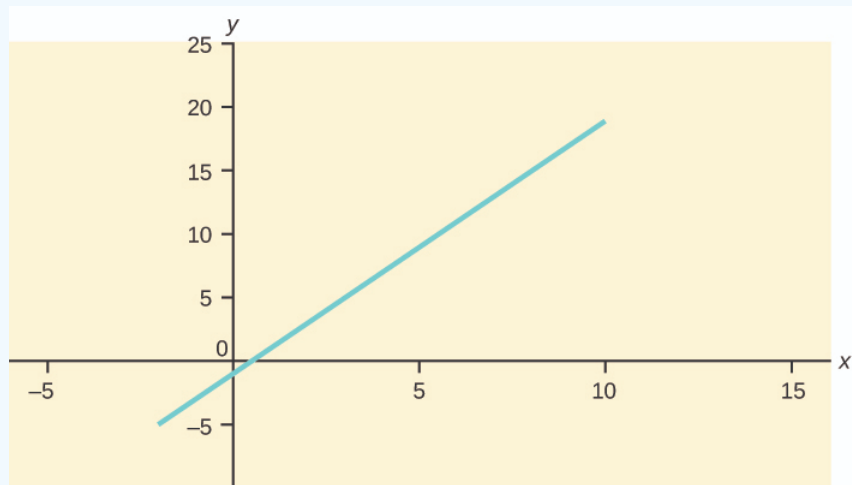


Figure 10.1.1.1.

? Exercise 10.1.1.2

Is the following an example of a linear equation? Why or why not?

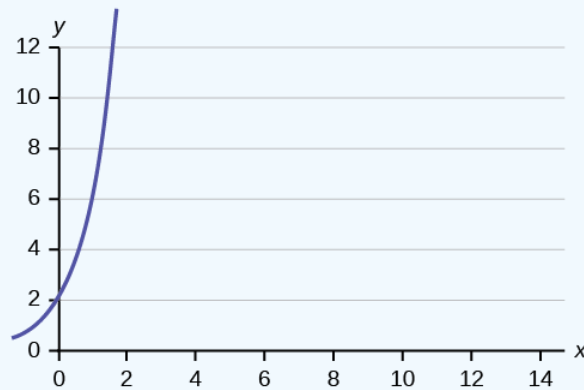


Figure 10.1.1.2.

Answer

No, the graph is not a straight line; therefore, it is not a linear equation.

✓ **Example 10.1.1.3**

Aaron's Word Processing Service (AWPS) does word processing. The rate for services is \$32 per hour plus a \$31.50 one-time charge. The total cost to a customer depends on the number of hours it takes to complete the job.

Find the equation that expresses the **total cost** in terms of the **number of hours** required to complete the job.

Answer

Let x = the number of hours it takes to get the job done.

Let y = the total cost to the customer.

The \$31.50 is a fixed cost. If it takes x hours to complete the job, then $(32)(x)$ is the cost of the word processing only. The total cost is: $y = 31.50 + 32x$

? **Exercise 10.1.1.3**

Emma's Extreme Sports hires hang-gliding instructors and pays them a fee of \$50 per class as well as \$20 per student in the class. The total cost Emma pays depends on the number of students in a class. Find the equation that expresses the total cost in terms of the number of students in a class.

Answer

$$y = 50 + 20x$$

Slope and Y-Intercept of a Linear Equation

For the linear equation $y = a + bx$, b = slope and a = y -intercept. From algebra recall that the slope is a number that describes the steepness of a line, and the y -intercept is the y coordinate of the point $(0, a)$ where the line crosses the y -axis.

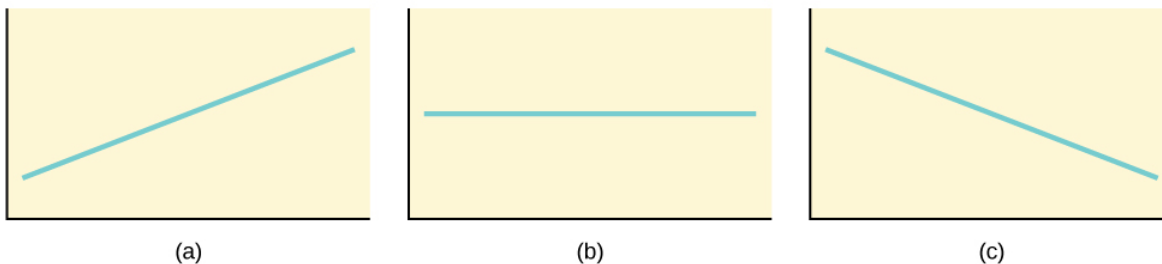


Figure 10.1.1.3: Three possible graphs of $y = a + bx$. (a) If $b > 0$, the line slopes upward to the right. (b) If $b = 0$, the line is horizontal. (c) If $b < 0$, the line slopes downward to the right.

✓ Example 10.1.1.4

Svetlana tutors to make extra money for college. For each tutoring session, she charges a one-time fee of \$25 plus \$15 per hour of tutoring. A linear equation that expresses the total amount of money Svetlana earns for each session she tutors is $y = 25 + 15x$.

What are the independent and dependent variables? What is the y -intercept and what is the slope? Interpret them using complete sentences.

Answer

The independent variable (x) is the number of hours Svetlana tutors each session. The dependent variable (y) is the amount, in dollars, Svetlana earns for each session.

The y -intercept is 25 ($a = 25$). At the start of the tutoring session, Svetlana charges a one-time fee of \$25 (this is when $x = 0$). The slope is 15 ($b = 15$). For each session, Svetlana earns \$15 for each hour she tutors.

? Exercise 10.1.1.4

Ethan repairs household appliances like dishwashers and refrigerators. For each visit, he charges \$25 plus \$20 per hour of work. A linear equation that expresses the total amount of money Ethan earns per visit is $y = 25 + 20x$.

What are the independent and dependent variables? What is the y -intercept and what is the slope? Interpret them using complete sentences.

Answer

The independent variable (x) is the number of hours Ethan works each visit. The dependent variable (y) is the amount, in dollars, Ethan earns for each visit.

The y -intercept is 25 ($a = 25$). At the start of a visit, Ethan charges a one-time fee of \$25 (this is when $x = 0$). The slope is 20 ($b = 20$). For each visit, Ethan earns \$20 for each hour he works.

Summary

The most basic type of association is a linear association. This type of relationship can be defined algebraically by the equations used, numerically with actual or predicted data values, or graphically from a plotted curve. (Lines are classified as straight curves.) Algebraically, a linear equation typically takes the form $y = mx + b$, where m and b are constants, x is the independent variable, y is the dependent variable. In a statistical context, a linear equation is written in the form $y = a + bx$, where a and b are the constants. This form is used to help readers distinguish the statistical context from the algebraic context. In the equation $y = a + bx$, the constant b that multiplies the x variable (b is called a coefficient) is called the **slope**. The constant a is called the y -intercept.

The **slope of a line** is a value that describes the rate of change between the independent and dependent variables. The **slope** tells us how the dependent variable (y) changes for every one unit increase in the independent (x) variable, on average. The **y -intercept** is used to describe the dependent variable when the independent variable equals zero.

Formula Review

$y = a + bx$ where a is the y -intercept and b is the slope. The variable x is the independent variable and y is the dependent variable.

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