

3.E: Summarizing Distributions (Exercises)

General questions

Q1

Make up a dataset of 12 numbers with a positive skew. Use a statistical program to compute the skew. Is the mean larger than the median as it usually is for distributions with a positive skew? What is the value for skew? (relevant section & relevant section)

Q2

Repeat **Q1** only this time make the dataset have a negative skew. (relevant section & relevant section)

Q3

Make up three data sets with 5 numbers each that have: (relevant section & relevant section)

- the same mean but different standard deviations.
- the same mean but different medians.
- the same median but different means.

Q4

Find the mean and median for the following three variables: (relevant section)

| <i>A</i> | <i>B</i> | <i>C</i> | |
|----------|----------|----------|---------|
| 8 | 4 | 6 | |
| 5 | 4 | 2 | |
| 7 | 6 | 3 | |
| 1 | 3 | 4 | |
| 3 | 4 | 1 | (3.E.1) |

Q5

A sample of 30 distance scores measured in yards has a mean of 7, a variance of 16, and a standard deviation of 4.

- You want to convert all your distances from yards to feet, so you multiply each score in the sample by 3. What are the new mean, variance, and standard deviation?
- You then decide that you only want to look at the distance past a certain point. Thus, after multiplying the original scores by 3, you decide to subtract 4 feet from each of the scores. Now what are the new mean, variance, and standard deviation? (relevant section)

Q6

You recorded the time in seconds it took for 8 participants to solve a puzzle. These times appear below. However, when the data was entered into the statistical program, the score that was supposed to be 22.1 was entered as 21.2. You had calculated the following measures of central tendency: the mean, the median, and the mean trimmed 25%. Which of these measures of central tendency will change when you correct the recording error? (relevant section & relevant section)

| | |
|------|---------|
| 15.2 | |
| 18.8 | |
| 19.3 | |
| 19.7 | |
| 20.2 | |
| 21.8 | |
| 22.1 | |
| 29.4 | (3.E.2) |

Q7

For the test scores in question **Q6**, which measures of variability (range, standard deviation, variance) would be changed if the 22.1 data point had been erroneously recorded as 21.2? (relevant section)

Q8

You know the minimum, the maximum, and the 25th, 50th, and 75th percentiles of a distribution. Which of the following measures of central tendency or variability can you determine? (relevant section, relevant section & relevant section)

mean, median, mode, trimean, geometric mean,
range, interquartile range, variance, standard deviation

Q9

- Find the value (v) for which $\sum (X - v)^2$ is minimized.
- Find the value (v) for which $\sum |X - v|$ is minimized.

Q10

Your younger brother comes home one day after taking a science test. He says that someone at school told him that "60% of the students in the class scored above the median test grade." What is wrong with this statement? What if he said "60% of the students scored below the mean?" (relevant section)

Q11

An experiment compared the ability of three groups of participants to remember briefly-presented chess positions. The data are shown below. The numbers represent the number of pieces correctly remembered from three chess positions. Compare the performance of each group. Consider spread as well as central tendency. (relevant section, relevant section & relevant section)

| Non-players | Beginners | Tournament players |
|-------------|-----------|--------------------|
| 22.1 | 32.5 | 40.1 |
| 22.3 | 37.1 | 45.6 |
| 26.2 | 39.1 | 51.2 |
| 29.6 | 40.5 | 56.4 |
| 31.7 | 45.5 | 58.1 |
| 33.5 | 51.3 | 71.1 |
| 38.9 | 52.6 | 74.9 |
| 39.7 | 55.7 | 75.9 |
| 43.2 | 55.9 | 80.3 |
| 43.2 | 57.7 | 85.3 |

Q12

True/False: A bimodal distribution has two modes and two medians. (relevant section)

Q13

True/False: The best way to describe a skewed distribution is to report the mean. (relevant section)

Q14

True/False: When plotted on the same graph, a distribution with a mean of 50 and a standard deviation of 10 will look more spread out than will a distribution with a mean of 60 and a standard deviation of 5. (relevant section)

Q15

Compare the mean, median, trimean in terms of their sensitivity to extreme scores (relevant section).

Q16

If the mean time to respond to a stimulus is much higher than the median time to respond, what can you say about the shape of the distribution of response times? (relevant section)

Q17

A set of numbers is transformed by taking the log base 10 of each number. The mean of the transformed data is 1.65. What is the geometric mean of the untransformed data? (relevant section)

Q18

Which measure of central tendency is most often used for returns on investment?

Q19

The histogram is in balance on the fulcrum. What are the mean, median, and mode of the distribution (approximate where necessary)?

Questions from Case Studies

The following questions are from the Angry Moods (AM) case study.

Q20

(AM#4) Does Anger-Out have a positive skew, a negative skew, or no skew? (relevant section)

Q21

(AM#8) What is the range of the Anger-In scores? What is the interquartile range? (relevant section)

Q22

(AM#12) What is the overall mean Control-Out score? What is the mean Control-Out score for the athletes? What is the mean Control-Out score for the non-athletes? (relevant section)

Q23

(AM#15) What is the variance of the Control-In scores for the athletes? What is the variance of the Control-In scores for the non-athletes? (relevant section)

The following question is from the Flatulence (F) case study.

Q24

(F#2) Based on a histogram of the variable "perday", do you think the mean or median of this variable is larger? Calculate the mean and median to see if you are right. (relevant section & relevant section)

The following questions are from the Stroop (S) case study.

Q25

(S#1) Compute the mean for "words". (relevant section)

Q26

(S#2) Compute the mean and standard deviation for "colors". (relevant section & relevant section)

The following questions are from the Physicians' Reactions (PR) case study.

Q27

(PR#2) What is the mean expected time spent for the average-weight patients? What is the mean expected time spent for the overweight patients? (relevant section)

Q28

(PR#3) What is the difference in means between the groups? By approximately how many standard deviations do the means differ? (relevant section & relevant section)

The following question is from the Smiles and Leniency (SL) case study.

Q29

(SL#2) Find the mean, median, standard deviation, and interquartile range for the leniency scores of each of the four groups. (relevant section & relevant section)

The following questions are from the ADHD Treatment (AT) case study.

Q30

(AT#4) What is the mean number of correct responses of the participants after taking the placebo (0 mg/kg)? (relevant section)

Q31

(AT#7) What are the standard deviation and the interquartile range of the $d0$ condition? (relevant section)

Selected Answers

S4

Variable A: Mean = 4.8, Median = 5

S5

a. Mean = 21, Var = 144, SD = 12

S9

a. 5.2

S22

Non-athletes: 23.2

S23

Athletes: 20.5

S26

Mean = 20.2

S27

Ave. weight: 31.4

S29

False smile group:

Mean = 5.37

Median = 5.50

SD = 1.83

IQR = 3.0

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