

## 5.2: B- Table of Integrals

### Basic Integrals

$$1. \int u^n du = \frac{u^{n+1}}{n+1} + C, \quad n \neq -1$$

$$2. \int \frac{du}{u} = \ln |u| + C$$

$$3. \int e^u du = e^u + C$$

$$4. \int a^u du = \frac{a^u}{\ln a} + C$$

$$5. \int \sin u du = -\cos u + C$$

$$6. \int \cos u du = \sin u + C$$

$$7. \int \sec^2 u du = \tan u + C$$

$$8. \int \csc^2 u du = -\cot u + C$$

$$9. \int \sec u \tan u du = \sec u + C$$

$$10. \int \csc u \cot u du = -\csc u + C$$

$$11. \int \tan u du = \ln |\sec u| + C$$

$$12. \int \cot u du = \ln |\sin u| + C$$

$$13. \int \sec u du = \ln |\sec u + \tan u| + C$$

$$14. \int \csc u du = \ln |\csc u - \cot u| + C$$

$$15. \int \frac{du}{\sqrt{a^2 - u^2}} = \sin^{-1} \left( \frac{u}{a} \right) + C$$

$$16. \int \frac{du}{a^2 + u^2} = \frac{1}{a} \tan^{-1} \left( \frac{u}{a} \right) + C$$

$$17. \int \frac{du}{u\sqrt{u^2 - a^2}} = \frac{1}{a} \sec^{-1} \frac{|u|}{a} + C$$

### Trigonometric Integrals

$$18. \int \sin^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$$

$$19. \int \cos^2 u du = \frac{1}{2}u + \frac{1}{4}\sin 2u + C$$

$$20. \int \tan^2 u du = \tan u - u + C$$

$$21. \int \cot^2 u du = -\cot u - u + C$$

22.  $\int \sin^3 u \, du = -\frac{1}{3}(2 + \sin^2 u) \cos u + C$
23.  $\int \cos^3 u \, du = \frac{1}{3}(2 + \cos^2 u) \sin u + C$
24.  $\int \tan^3 u \, du = \frac{1}{2} \tan^2 u + \ln |\cos u| + C$
25.  $\int \cot^3 u \, du = -\frac{1}{2} \cot^2 u - \ln |\sin u| + C$
26.  $\int \sec^3 u \, du = \frac{1}{2} \sec u \tan u + \frac{1}{2} \ln |\sec u + \tan u| + C$
27.  $\int \csc^3 u \, du = -\frac{1}{2} \csc u \cot u + \frac{1}{2} \ln |\csc u - \cot u| + C$
28.  $\int \sin^n u \, du = \frac{-1}{n} \sin^{n-1} u \cos u + \frac{n-1}{n} \int \sin^{n-2} u \, du$
29.  $\int \cos^n u \, du = \frac{1}{n} \cos^{n-1} u \sin u + \frac{n-1}{n} \int \cos^{n-2} u \, du$
30.  $\int \tan^n u \, du = \frac{1}{n-1} \tan^{n-1} u - \int \tan^{n-2} u \, du$
31.  $\int \cot^n u \, du = \frac{-1}{n-1} \cot^{n-1} u - \int \cot^{n-2} u \, du$
32.  $\int \sec^n u \, du = \frac{1}{n-1} \tan u \sec^{n-2} u + \frac{n-2}{n-1} \int \sec^{n-2} u \, du$
33.  $\int \csc^n u \, du = \frac{-1}{n-1} \cot u \csc^{n-2} u + \frac{n-2}{n-1} \int \csc^{n-2} u \, du$
34.  $\int \sin au \sin bu \, du = \frac{\sin(a-b)u}{2(a-b)} - \frac{\sin(a+b)u}{2(a+b)} + C$
35.  $\int \cos au \cos bu \, du = \frac{\sin(a-b)u}{2(a-b)} + \frac{\sin(a+b)u}{2(a+b)} + C$
36.  $\int \sin au \cos bu \, du = -\frac{\cos(a-b)u}{2(a-b)} - \frac{\cos(a+b)u}{2(a+b)} + C$
37.  $\int u \sin u \, du = \sin u - u \cos u + C$
38.  $\int u \cos u \, du = \cos u + u \sin u + C$
39.  $\int u^n \sin u \, du = -u^n \cos u + n \int u^{n-1} \cos u \, du$
40.  $\int u^n \cos u \, du = u^n \sin u - n \int u^{n-1} \sin u \, du$
41. 
$$\begin{aligned} \int \sin^n u \cos^m u \, du &= -\frac{\sin^{n-1} u \cos^{m+1} u}{n+m} + \frac{n-1}{n+m} \int \sin^{n-2} u \cos^m u \, du \\ &= \frac{\sin^{n+1} u \cos^{m-1} u}{n+m} + \frac{m-1}{n+m} \int \sin^n u \cos^{m-2} u \, du \end{aligned}$$

### Exponential and Logarithmic Integrals

42.  $\int u e^{au} \, du = \frac{1}{a^2} (au - 1) e^{au} + C$

43.  $\int u^n e^{au} du = \frac{1}{a} u^n e^{au} - \frac{n}{a} \int u^{n-1} e^{au} du$
44.  $\int e^{au} \sin bu du = \frac{e^{au}}{a^2 + b^2} (a \sin bu - b \cos bu) + C$
45.  $\int e^{au} \cos bu du = \frac{e^{au}}{a^2 + b^2} (a \cos bu + b \sin bu) + C$
46.  $\int \ln u du = u \ln u - u + C$
47.  $\int u^n \ln u du = \frac{u^{n+1}}{(n+1)^2} [(n+1) \ln u - 1] + C$
48.  $\int \frac{1}{u \ln u} du = \ln |\ln u| + C$

### Hyperbolic Integrals

49.  $\int \sinh u du = \cosh u + C$
50.  $\int \cosh u du = \sinh u + C$
51.  $\int \tanh u du = \ln \cosh u + C$
52.  $\int \coth u du = \ln |\sinh u| + C$
53.  $\int \operatorname{sech} u du = \tan^{-1} |\sinh u| + C$
54.  $\int \operatorname{csch} u du = \ln \left| \tanh \frac{1}{2} u \right| + C$
55.  $\int \operatorname{sech}^2 u du = \tanh u + C$
56.  $\int \operatorname{csch}^2 u du = -\coth u + C$
57.  $\int \operatorname{sech} u \tanh u du = -\operatorname{sech} u + C$
58.  $\int \operatorname{csch} u \coth u du = -\operatorname{csch} u + C$

### Inverse Trigonometric Integrals

59.  $\int \sin^{-1} u du = u \sin^{-1} u + \sqrt{1-u^2} + C$
60.  $\int \cos^{-1} u du = u \cos^{-1} u - \sqrt{1-u^2} + C$
61.  $\int \tan^{-1} u du = u \tan^{-1} u - \frac{1}{2} \ln(1+u^2) + C$
62.  $\int u \sin^{-1} u du = \frac{2u^2-1}{4} \sin^{-1} u + \frac{u\sqrt{1-u^2}}{4} + C$
63.  $\int u \cos^{-1} u du = \frac{2u^2-1}{4} \cos^{-1} u - \frac{u\sqrt{1-u^2}}{4} + C$
64.  $\int u \tan^{-1} u du = \frac{u^2+1}{2} \tan^{-1} u - \frac{u}{2} + C$

$$65. \int u^n \sin^{-1} u \, du = \frac{1}{n+1} \left[ u^{n+1} \sin^{-1} u - \int \frac{u^{n+1} du}{\sqrt{1-u^2}} \right], \quad n \neq -1$$

$$66. \int u^n \cos^{-1} u \, du = \frac{1}{n+1} \left[ u^{n+1} \cos^{-1} u + \int \frac{u^{n+1} du}{\sqrt{1-u^2}} \right], \quad n \neq -1$$

$$67. \int u^n \tan^{-1} u \, du = \frac{1}{n+1} \left[ u^{n+1} \tan^{-1} u - \int \frac{u^{n+1} du}{1+u^2} \right], \quad n \neq -1$$

### Integrals Involving $a^2 + u^2$ , $a > 0$

$$68. \int \sqrt{a^2 + u^2} \, du = \frac{u}{2} \sqrt{a^2 + u^2} + \frac{a^2}{2} \ln(u + \sqrt{a^2 + u^2}) + C$$

$$69. \int u^2 \sqrt{a^2 + u^2} \, du = \frac{u}{8} (a^2 + 2u^2) \sqrt{a^2 + u^2} - \frac{a^4}{8} \ln(u + \sqrt{a^2 + u^2}) + C$$

$$70. \int \frac{\sqrt{a^2 + u^2}}{u} \, du = \sqrt{a^2 + u^2} - a \ln \left| \frac{a + \sqrt{a^2 + u^2}}{u} \right| + C$$

$$71. \int \frac{\sqrt{a^2 + u^2}}{u^2} \, du = -\frac{\sqrt{a^2 + u^2}}{u} + \ln(u + \sqrt{a^2 + u^2}) + C$$

$$72. \int \frac{du}{\sqrt{a^2 + u^2}} = \ln(u + \sqrt{a^2 + u^2}) + C$$

$$73. \int \frac{u^2}{\sqrt{a^2 + u^2}} \, du = \frac{u}{2} (\sqrt{a^2 + u^2}) - \frac{a^2}{2} \ln(u + \sqrt{a^2 + u^2}) + C$$

$$74. \int \frac{du}{u\sqrt{a^2 + u^2}} = \frac{-1}{a} \ln \left| \frac{\sqrt{a^2 + u^2} + a}{u} \right| + C$$

$$75. \int \frac{du}{u^2 \sqrt{a^2 + u^2}} = -\frac{\sqrt{a^2 + u^2}}{a^2 u} + C$$

$$76. \int \frac{du}{(a^2 + u^2)^{3/2}} = \frac{u}{a^2 \sqrt{a^2 + u^2}} + C$$

### Integrals Involving $u^2 - a^2$ , $a > 0$

$$77. \int \sqrt{u^2 - a^2} \, du = \frac{u}{2} \sqrt{u^2 - a^2} - \frac{a^2}{2} \ln|u + \sqrt{u^2 - a^2}| + C$$

$$78. \int u^2 \sqrt{u^2 - a^2} \, du = \frac{u}{8} (2u^2 - a^2) \sqrt{u^2 - a^2} - \frac{a^4}{8} \ln|u + \sqrt{u^2 - a^2}| + C$$

$$79. \int \frac{\sqrt{u^2 - a^2}}{u} \, du = \sqrt{u^2 - a^2} - a \cos^{-1} \frac{a}{|u|} + C$$

$$80. \int \frac{\sqrt{u^2 - a^2}}{u^2} \, du = -\frac{\sqrt{u^2 - a^2}}{u} + \ln|u + \sqrt{u^2 - a^2}| + C$$

$$81. \int \frac{du}{\sqrt{u^2 - a^2}} = \ln|u + \sqrt{u^2 - a^2}| + C$$

$$82. \int \frac{u^2}{\sqrt{u^2 - a^2}} \, du = \frac{u}{2} \sqrt{u^2 - a^2} + \frac{a^2}{2} \ln|u + \sqrt{u^2 - a^2}| + C$$

$$83. \int \frac{du}{u^2 \sqrt{u^2 - a^2}} = \frac{\sqrt{u^2 - a^2}}{a^2 u} + C$$

$$84. \int \frac{du}{(u^2 - a^2)^{3/2}} = -\frac{u}{a^2 \sqrt{u^2 - a^2}} + C$$

### Integrals Involving $a^2 - u^2$ , $a > 0$

85.  $\int \sqrt{a^2 - u^2} \, du = \frac{u}{2} \sqrt{a^2 - u^2} + \frac{a^2}{2} \sin^{-1} \frac{u}{a} + C$
86.  $\int u^2 \sqrt{a^2 - u^2} \, du = \frac{u}{8} (2u^2 - a^2) \sqrt{a^2 - u^2} + \frac{a^4}{8} \sin^{-1} \frac{u}{a} + C$
87.  $\int \frac{\sqrt{a^2 - u^2}}{u} \, du = \sqrt{a^2 - u^2} - a \ln \left| \frac{a + \sqrt{a^2 - u^2}}{u} \right| + C$
88.  $\int \frac{\sqrt{a^2 - u^2}}{u^2} \, du = \frac{-1}{u} \sqrt{a^2 - u^2} - \sin^{-1} \frac{u}{a} + C$
89.  $\int \frac{u^2}{\sqrt{a^2 - u^2}} \, du = \frac{1}{2} \left( -u \sqrt{a^2 - u^2} + a^2 \sin^{-1} \frac{u}{a} \right) + C$
90.  $\int \frac{du}{u \sqrt{a^2 - u^2}} = -\frac{1}{a} \ln \left| \frac{a + \sqrt{a^2 - u^2}}{u} \right| + C$
91.  $\int \frac{du}{u^2 \sqrt{a^2 - u^2}} = -\frac{1}{a^2 u} \sqrt{a^2 - u^2} + C$
92.  $\int (a^2 - u^2)^{3/2} \, du = -\frac{u}{8} (2u^2 - 5a^2) \sqrt{a^2 - u^2} + \frac{3a^4}{8} \sin^{-1} \frac{u}{a} + C$
93.  $\int \frac{du}{(a^2 - u^2)^{3/2}} = -\frac{u}{a^2 \sqrt{a^2 - u^2}} + C$

### Integrals Involving $2au - u^2$ , $a > 0$

94.  $\int \sqrt{2au - u^2} \, du = \frac{u - a}{2} \sqrt{2au - u^2} + \frac{a^2}{2} \cos^{-1} \left( \frac{a - u}{a} \right) + C$
95.  $\int \frac{du}{\sqrt{2au - u^2}} = \cos^{-1} \left( \frac{a - u}{a} \right) + C$
96.  $\int u \sqrt{2au - u^2} \, du = \frac{2u^2 - au - 3a^2}{6} \sqrt{2au - u^2} + \frac{a^3}{2} \cos^{-1} \left( \frac{a - u}{a} \right) + C$
97.  $\int \frac{du}{u \sqrt{2au - u^2}} = -\frac{\sqrt{2au - u^2}}{au} + C$

### Integrals Involving $a + bu$ , $a \neq 0$

98.  $\int \frac{u}{a + bu} \, du = \frac{1}{b^2} (a + bu - a \ln |a + bu|) + C$
99.  $\int \frac{u^2}{a + bu} \, du = \frac{1}{2b^3} [(a + bu)^2 - 4a(a + bu) + 2a^2 \ln |a + bu|] + C$
100.  $\int \frac{du}{u(a + bu)} = \frac{1}{a} \ln \left| \frac{u}{a + bu} \right| + C$
101.  $\int \frac{du}{u^2(a + bu)} = -\frac{1}{au} + \frac{b}{a^2} \ln \left| \frac{a + bu}{u} \right| + C$
102.  $\int \frac{u}{(a + bu)^2} \, du = \frac{a}{b^2(a + bu)} + \frac{1}{b^2} \ln |a + bu| + C$
103.  $\int \frac{u}{u(a + bu)^2} \, du = \frac{1}{a(a + bu)} - \frac{1}{a^2} \ln \left| \frac{a + bu}{u} \right| + C$
104.  $\int \frac{u^2}{(a + bu)^2} \, du = \frac{1}{b^3} \left( a + bu - \frac{a^2}{a + bu} - 2a \ln |a + bu| \right) + C$

105.  $\int u\sqrt{a+bu} \, du = \frac{2}{15b^2}(3bu-2a)(a+bu)^{3/2} + C$
106.  $\int \frac{u}{\sqrt{a+bu}} \, du = \frac{2}{3b^2}(bu-2a)\sqrt{a+bu} + C$
107.  $\int \frac{u^2}{\sqrt{a+bu}} \, du = \frac{2}{15b^3}(8a^2+3b^2u^2-4abu)\sqrt{a+bu} + C$
108.  $\int \frac{du}{u\sqrt{a+bu}} = \begin{cases} \frac{1}{\sqrt{a}} \ln \left| \frac{\sqrt{a+bu}-\sqrt{a}}{\sqrt{a+bu}+\sqrt{a}} \right| + C, & \text{if } a > 0 \\ \frac{\sqrt{2}}{\sqrt{-a}} \tan^{-1} \sqrt{\frac{a+bu}{-a}} + C, & \text{if } a < 0 \end{cases}$
109.  $\int \frac{\sqrt{a+bu}}{u} \, du = 2\sqrt{a+bu} + a \int \frac{du}{u\sqrt{a+bu}}$
110.  $\int \frac{\sqrt{a+bu}}{u^2} \, du = -\frac{\sqrt{a+bu}}{u} + \frac{b}{2} \int \frac{du}{u\sqrt{a+bu}}$
111.  $\int u^n \sqrt{a+bu} \, du = \frac{2}{b(2n+3)} \left[ u^n(a+bu)^{3/2} - na \int u^{n-1} \sqrt{a+bu} \, du \right]$
112.  $\int \frac{u^n}{\sqrt{a+bu}} \, du = \frac{2u^n \sqrt{a+bu}}{b(2n+1)} - \frac{2na}{b(2n+1)} \int \frac{u^{n-1}}{\sqrt{a+bu}} \, du$
113.  $\int \frac{du}{u^n \sqrt{a+bu}} = -\frac{\sqrt{a+bu}}{a(n-1)u^{n-1}} - \frac{b(2n-3)}{2a(n-1)} \int \frac{du}{u^{n-1} \sqrt{a+bu}}$

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